

**Topic :** Definite Integration

**Type of Questions**

**M.M., Min.**

**Single choice Objective ('-1' negative marking)** Q.1,2,3,4,5,6,7,8    (3 marks, 3 min.) [24, 24]  
**Multiple choice objective ('-1' negative marking)** Q.9    (5 marks, 4 min.) [5, 4]

1. A particular solution of  $\frac{dy}{dx} = \frac{x(2\log x + 1)}{\sin y + y \cos y}$  is -  
 (A)  $y \sin y = x \log x$     (B)  $y^2 \sin y = x \log x$     (C)  $y \sin y = x^2 \log x$     (D) none of these
  
2. The solution of differential equation  $(1 + y^2) + \left(x - 2e^{\tan^{-1} y}\right) \frac{dy}{dx} = 0$  is  
 (A)  $(x - 2) = k e^{2\tan^{-1} y}$     (B)  $x e^{\tan^{-1} y} = e^{2\tan^{-1} y} + k$   
 (C)  $x e^{\tan^{-1} y} = \tan^{-1} y + k$     (D)  $x e^{2\tan^{-1} y} = e^{2\tan^{-1} y} + k$
  
3. The solution of the differential equation  $x^2 \frac{dy}{dx} \cdot \cos\left(\frac{1}{x}\right) - y \sin\left(\frac{1}{x}\right) = -1$ , where  $y \rightarrow -1$  as  $x \rightarrow \infty$  is.  
 (A)  $y = \sin \frac{1}{x} + \cos \frac{1}{x}$     (B)  $y = \frac{x+1}{x \sin(1/x)}$   
 (C)  $y = \sin \frac{1}{x} - \cos \frac{1}{x}$     (D)  $y = \frac{x+1}{x \cos(1/x)}$
  
4. Solution of the differential equation  $(x^2 + y^3)(2x^2 dx + 3y dy) = 12x dx + 18y^2 dy$  is  
 (A)  $\frac{2}{3}x^3 + \frac{3}{2}y^2 = 6 \ln(x^2 + y^3) + c$     (B)  $x^2 + y^3 = 9 \ln(x^2 + y^3) + c$   
 (C)  $\frac{2}{3}x^3 + \frac{3}{2}y^2 = 6 \ln(x^3 + y^2) + c$     (D)  $x^3 + y^2 = 6 \ln(x^2 + y^3) + c$
  
5. Solution of differential equation  $(2x \ln y) dx + \left(\frac{x^2}{y} + 3y^2\right) dy = 0$  is  
 (A)  $x^2 \ln y + y^3 = c$     (B)  $x \ln y + y^2 = c$     (C)  $x^2 \ln y + y^2 = c$     (D) none of these
  
6. If solution of the differential equation  $\frac{dy}{dx} = \frac{1}{x \cos y + \sin 2y}$  is  $x = ce^{\sin y} - k(1 + \sin y)$ , then  $k =$   
 (A) 1    (B) 2    (C) 3    (D) 5
  
7. A curve passes through the point  $(2a, a)$  and is such that sum of subtangent and abscissa is equal to  $a$ . Its equation is  
 (A)  $(x - a)^2 = a^3$     (B)  $(x - a)^2 y = a^3$     (C)  $(x - a)y = a^2$     (D) none of these
  
8. If  $[\cdot]$  represents the greatest integer function, then  $\int_4^{10} \frac{[x^2]}{[x^2 - 28x + 196] + [x^2]} dx$  is equal to -  
 (A) 0    (B) 1    (C) 3    (D) None of these
  
9. Which of the following equation(s) is/are linear differential equation.  
 (A)  $\frac{dy}{dx} + \frac{y}{x} = \ln x$     (B)  $y \left( \frac{dy}{dx} \right) + 4x = 0$     (C)  $dx + dy = 0$     (D)  $\frac{d^2y}{dx^2} = \cos x$

# **Answers Key**

- 1.** (C)      **2.** (B)      **3.** (C)      **4.** (A)
- 5.** (A)      **6.** (B)      **7.** (C)      **8.** (C)
- 9.** (A)(C) (D)