

APPLIED MATHEMATICS

Grade XII



CENTRAL BOARD OF SECONDARY EDUCATION

Shiksha Sadan, 17, Rouse Avenue, New Delhi-110002

Dedicated to:



Sh. Pramod Kumar T.K.

(15th April 1971 to 25th May 2021)

**Joint Secretary (Academics)
Central Board of Secondary Education**

You will always be in our memories...

Applied Mathematics

Class XII

Student Support Material



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भारत का संविधान

उद्देशिका

हम, भारत के लोग, भारत को एक सम्पूर्ण ¹प्रभुत्व-संपन्न समाजवादी पंथनिरपेक्ष लोकतंत्रात्मक गणराज्य बनाने के लिए, तथा उसके समस्त नागरिकों को:

सामाजिक, आर्थिक और राजनैतिक न्याय,

विचार, अभिव्यक्ति, विश्वास, धर्म

और उपासना की स्वतंत्रता,

प्रतिष्ठा और अवसर की समता

प्राप्त कराने के लिए

तथा उन सब में व्यक्ति की गरिमा

²और राष्ट्र की एकता और अखंडता

सुनिश्चित करने वाली बंधुता बढ़ाने के लिए

दृढसंकल्प होकर अपने इस संविधान में आज तारीख 26 नवम्बर, 1949 ई० को एतद्वारा इस संविधान को अंगीकृत, अधिनियमित और आत्मार्पित करते हैं।

1. संविधान (बयालीसवां संशोधन) अधिनियम, 1976 को धारा 2 द्वारा (3.1.1977) से “प्रभुत्व-संपन्न लोकतंत्रात्मक गणराज्य” के स्थान पर प्रतिस्थापित।

2. संविधान (बयालीसवां संशोधन) अधिनियम, 1976 को धारा 2 द्वारा (3.1.1977) से “राष्ट्र की एकता” के स्थान पर प्रतिस्थापित।

भाग 4 क

मूल कर्तव्य

51 क. मूल कर्तव्य—भारत के प्रत्येक नागरिक का यह कर्तव्य होगा कि वह—

- (क) संविधान का पालन करे और उसके आदर्शों, संस्थाओं, राष्ट्र ध्वज और राष्ट्रगान का आदर करें;
- (ख) स्वतंत्रता के लिए हमारे राष्ट्रीय आंदोलन को प्रेरित करने वाला उच्च आदर्शों को हृदय में संजोए रखे और उनका पालन करे;
- (ग) भारत की प्रभुता, एकता और अखंडता की रक्षा करे और उसे अक्षुण्ण रखे;
- (घ) देश की रक्षा करे और आह्वान किए जाने पर राष्ट्र की सेवा करे;
- (ङ) भारत के सभी लोगों में समरसता और समान भ्रातृत्व की भावना का निर्माण करे जो धर्म, भाषा और प्रदेश या वर्ग पर आधारित सभी भेदभाव से परे हों, ऐसी प्रथाओं का त्याग करे जो स्त्रियों के सम्मान के विरुद्ध हैं;
- (च) हमारी सामाजिक संस्कृति की गौरवशाली परंपरा का महत्त्व समझे और उसका परिक्षण करे;
- (छ) प्राकृतिक पर्यावरण की जिसके अंतर्गत वन, झील, नदी, और वन्य जीव हैं, रक्षा करे और उसका संवर्धन करे तथा प्राणी मात्र के प्रति दयाभाव रखे;
- (ज) वैज्ञानिक दृष्टिकोण, मानववाद और ज्ञानार्जन तथा सुधार की भावना का विकास करे;
- (झ) सार्वजनिक संपत्ति को सुरक्षित रखे और हिंसा से दूर रहे;
- (ञ) व्यक्तिगत और सामूहिक गतिविधियों से सभी क्षेत्रों में उत्कर्ष की ओर बढ़ने का सतत प्रयास करे जिससे राष्ट्र निरंतर बढ़ते हुए प्रयत्न और उपलब्धि की नई उंचाईयों को छू ले;

¹(ट) यदि माता-पिता या संरक्षक है, छह वर्ष से चौदह वर्ष तक की आयु वाले अपने, यथास्थिति, बालक या प्रतिपाल्य के लिए शिक्षा के अवसर प्रदान करे।

THE CONSTITUTION OF INDIA

PREAMBLE

WE, THE PEOPLE OF INDIA, having solemnly resolve to constitute India into a ¹**SOVEREIGN SOCIALIST SECULAR DEMOCRATIC REPUBLIC** and to secure to all its citizens :

JUSTICE, social, economic and political;

LIBERTY of thought, expression, belief, faith and worship;

EQUALITY of status and of opportunity; and to promote among them all

FRATERNITY assuring the dignity of the individual and the² unity and integrity of the Nation;

IN OUR CONSTITUENT ASSEMBLY this twenty-sixth day of November, 1949, do **HEREBY ADOPT, ENACT AND GIVE TO OURSELVES THIS CONSTITUTION.**

1. Subs, by the Constitution (Forty-Second Amendent) Act. 1976, sec. 2 for "Sovereign Democratic Republic" (w.e.f. 3.1.1977)

2. Subs, by the Constitution (Forty-Second Amendent) Act. 1976, sec. 2 for "unity of the Nation" (w.e.f. 3.1.1977)

THE CONSTITUTION OF INDIA

Chapter IV A

FUNDAMENTAL DUTIES

ARTICLE 51 A

Fundamental Duties - It shall be the duty of every citizen of India-

- (a) to abide by the Constitution and respect its ideals and institutions, the National Flag and the National Anthem;
- (b) to cherish and follow the noble ideals which inspired our national struggle for freedom;
- (c) to uphold and protect the sovereignty, unity and integrity of India;
- (d) to defend the country and render national service when called upon to do so;
- (e) to promote harmony and the spirit of common brotherhood amongst all the people of India transcending religious, linguistic and regional or sectional diversities; to renounce practices derogatory to the dignity of women;
- (f) to value and preserve the rich heritage of our composite culture;
- (g) to protect and improve the natural environment including forests, lakes, rivers, wild life and to have compassion for living creatures;
- (h) to develop the scientific temper, humanism and the spirit of inquiry and reform;
- (i) to safeguard public property and to abjure violence;
- (j) to strive towards excellence in all spheres of individual and collective activity so that the national constantly rises to higher levels of endeavour and achievement;
- ¹(k) who is parent or guardian to provide opportunities for education to his/her child or, as the case may be, ward between age 6 and 14 years.

1. Subs. By the Constitution Sec. 04 (Eighty-Six Amendment) Act, 2002

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Note to the Users

Mathematical ideas have become more relevant with advances in technology, economy and social structure. A mathematically skilled workforce is necessary to make informed decisions in their personal lives, keeping in mind the strong and ever-growing mathematical influence over our lives.

Mathematics skills are essential in all fields be it art, literature or social sciences. This necessitates the creation of a mathematics curriculum that maps the country's need and spirit by using the rich and diverse landscape of illuminated mathematical contexts in India.

The present application-centric and problem-driven course of Applied Mathematics has been developed around key mathematical ideas with potential applications in entrance exams and practical life.

The course is divided into different units each focusing on numerical, algebraic or stoical applications. The scope of the course ranges from mathematical applications in the field of finance (including business and economics), pharmaceutical industry, hospitality and entertainment industry, advertisement and marketing sector, healthcare services including counselling service, agricultural sector, government-aided programs such as resources distribution, traffic management systems including air traffic management, infrastructure development, archaeological studies and studies on historiography, real-time data analysis and much more. Core mathematical ideas are presented keeping in mind these contexts.

The course aims to develop mathematical thinking skills by reasoning quantitative; constructing viable mathematical arguments; constructing new mathematical knowledge using problem-solving and learning to model with mathematics.

This student support material is divided into different units including a unit on the use of a spreadsheet for mathematical applications. Sequencing of units is done naturally starting from Quantification and Numerical applications, Algebraic Thinking, Calculus, Probability, Inferential statistics, Index Numbers Financial Mathematics and Linear Programming.

Each unit is divided into several sections having discrete exercises. Efforts are made to develop concepts around meaningful applications to foster inquisitiveness in learners. Teachers are encouraged to extend/adapt these examples to initiate investigations and stimulating discourse in the classrooms.

This support material should not be considered a textbook and teachers should avoid teaching the content as given in this material. It only gives certain directions to approach various topics. Teachers are advised to use multiple examples from sources such as newspapers, magazines and other online resources to help students reconcile different approaches to problem-solving and refining mathematical arguments.

We hope that this book will provide students with a real sense of the application of mathematics in different spheres of work and life. It is an invitation to reinvent mathematics and empower us to make more logical and informed decisions in our lives.

We look forward to suggestions from teachers, students and the whole learning community to make this book more adaptable for the Indian classroom. You may share your feedback to subhash_garg@cbseshiksha.in.

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