

Time: 45 minutes

Maximum Marks: 200

General Instructions: As given in Practice Paper – 1.

## Section-A

Choose the correct option:

1. The matrix  $\begin{bmatrix} 0 & 5 & -7 \\ -5 & 0 & 11 \\ 7 & -11 & 0 \end{bmatrix}$  is known as  
(a) Upper triangular matrix (b) Skew symmetric matrix  
(c) Symmetric matrix (d) Diagonal matrix
2. If  $A = \begin{bmatrix} 1 & 2 \\ 4 & 2 \end{bmatrix}$ , then the value of  $k$  if  $|2A| = k|A|$  is  
(a) 4 (b) -4 (c) 3 (d) 0
3. If  $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$  and  $A(\text{adj } A) = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$ , then the value of  $k$  is  
(a) 1 (b) -1 (c) 0 (d) 2
4. If  $f(x) = e^x$  then  $f''(5)$  is equal to  
(a)  $e$  (b)  $e^5$  (c)  $e^4$  (d) None of these
5. Let the parabolas  $y = x^2 + ax + b$  and  $y = x(c - x)$  touch each other at the point (1, 0). Then  
(a)  $a = -3$  (b)  $b = 1$  (c)  $c = 2$  (d)  $b = -2$
6. The value of  $\int \frac{2x \, dx}{\sqrt{1 - x^2 - x^4}}$  equals  
(a)  $\sin^{-1}\left(\frac{2x^2+1}{\sqrt{5}}\right) + C$  (b)  $\cos^{-1}\left(\frac{2x^2+1}{\sqrt{5}}\right) + C$   
(c)  $\log\left(\frac{2x^2+1}{\sqrt{5}}\right) + C$  (d)  $\sin^{-1}\left(\frac{2x^2-1}{\sqrt{5}}\right) + C$
7. The value of  $\int \frac{\cos x \, dx}{\sqrt{\sin^2 x - 2 \sin x - 3}}$  equals

(a)  $\log|(\sin x - 1) + \sqrt{\sin^2 x - 2\sin x - 3}| + C$

(b)  $\log|(\sin x - 1) - \sqrt{\sin^2 x - 2\sin x - 3}| + C$

(c)  $\log|(\sin x + 1) + \sqrt{\sin^2 x + 2\sin x - 3}| + C$

(d)  $\log|\sin x - 2| + C$

8. The integral value of  $\int_0^{\frac{\pi}{2}} \frac{\tan x \, dx}{1 + m^2 \tan^2 x}$  is

(a)  $\frac{\log m}{m^2 - 1}$

(b)  $\log\left(\frac{m^2 - m}{2}\right)$

(c)  $\log 3m$

(d) 0

9.  $\int_1^{\sqrt{3}} \frac{dx}{1+x^2}$  is equal to

(a)  $\frac{\pi}{3}$

(b)  $\frac{2\pi}{3}$

(c)  $\frac{\pi}{6}$

(d)  $\frac{\pi}{12}$

10. The area of the region included between the parabola  $y = \frac{3x^2}{4}$  and the line  $3x - 2y + 12 = 0$  is

(a) 20 sq. units

(b) 12 sq. units

(c) 8 sq. units

(d) 27 sq. units

11. The differential equation of the family of curves  $x^2 + y^2 - 2ay = 0$ , where  $a$  is arbitrary constant, is

(a)  $(x^2 - y^2) y' = 2xy$

(b)  $2(x^2 + y^2) y' = xy$

(c)  $2(x^2 - y^2) y' = xy$

(d)  $(x^2 + y^2) y' = 2xy$

12. The general solution of  $(2y - 1) dx - (2x + 3) dy = 0$  is

(a)  $\frac{2x - 1}{2y + 3} = k$

(b)  $\frac{2y + 1}{2x - 3} = k$

(c)  $\frac{2x + 3}{2y - 1} = k$

(d)  $\frac{2x - 1}{2y - 1} = k$

13. Which of the following is not a convex set?

(a)  $\{(x, y) | 2x + 5y < 7\}$

(b)  $\{(x, y) | x^2 + y^2 \leq 4\}$

(c)  $\{x : |x| = 5\}$

(d)  $\{(x, y) | 3x^2 + 2y^2 \leq 6\}$

14. Suppose a random variable  $X$  follows the binomial distribution with parameters  $n$  and  $p$ , where  $0 < p < 1$ . If  $P(X = r)/P(X = n - r)$  is independent of  $n$  and  $r$ , then  $p$  equals to

(a)  $\frac{1}{2}$

(b)  $\frac{11}{3}$

(c)  $\frac{2}{5}$

(d)  $\frac{3}{7}$

15. For the binomial distribution  $B\left(6, \frac{1}{3}\right)$ , the variance is

(a)  $\frac{4}{3}$

(b) 2

(c) 4

(d) None of these

### Section-B (BI)

16. If a relation  $R$  on the set  $\{1, 2, 3\}$  be defined by  $R = \{(1, 2)\}$ , then  $R$  is

(a) Reflexive

(b) Transitive

(c) Symmetric

(d) None of these

17. Let  $*$  be binary operation on  $\mathbb{R}$  given by  $a * b = b - a + 1$  then  $(5 * 4)$  is equal to

(a) 1

(b) 0

(c) 2

(d) None of these

18. Let the function  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = 2x + \sin x$  for  $x \in \mathbb{R}$ . Then  $f$  is

(a) one-one but not onto

(b) onto but not one-one

(c) neither one-one nor onto

(d) one-one and onto

19. Let  $f(x) = \begin{cases} x+1, & x \leq 1 \\ 2x+1, & 1 < x \leq 2 \end{cases}$  and  $g(x) = \begin{cases} x^2, & -1 \leq x < 2 \\ x+2, & 2 \leq x \leq 3 \end{cases}$  then  $f \circ g(x)$  is

(a)  $f \circ g(x) = \begin{cases} x^2, & -1 \leq x < 2 \\ x+2, & 2 \leq x < 3 \end{cases}$

(b)  $f \circ g(x) = \begin{cases} x^2+1, & -1 \leq x < 2 \\ x+2, & 2 \leq x \leq 3 \end{cases}$

$$(c) f \circ g(x) = \begin{cases} x^2 + 1, & x \leq 1 \\ 2x^2 + 1, & 1 < x \leq \sqrt{2} \end{cases}$$

$$(d) f \circ g(x) = \begin{cases} x^2, & -1 \leq x < 2 \\ x + 2, & 2 \leq x \leq 3 \end{cases}$$

20. Let  $f: R - \left\{-\frac{4}{3}\right\} \rightarrow R$  be a function defined as  $f(x) = \frac{4x}{3x+4}$ . The inverse of  $f$  is the map  $g: \text{Range } f \rightarrow R - \left\{-\frac{4}{3}\right\}$  given by

$$(a) g(y) = \frac{3y}{3-4y}$$

$$(b) g(y) = \frac{4y}{4-3y}$$

$$(c) g(y) = \frac{4y}{3-4y}$$

$$(d) g(y) = \frac{3y}{4-3y}$$

21. The value of  $\sec^{-1}\left(\sec\frac{4\pi}{3}\right)$  is

$$(a) \frac{\pi}{3}$$

$$(b) \frac{2\pi}{3}$$

$$(c) \frac{4\pi}{3}$$

$$(d) \frac{-\pi}{3}$$

22. The value of  $\cos^{-1}(-1) + \sin^{-1}(1)$  is

$$(a) \frac{-3\pi}{2}$$

$$(b) \frac{\pi}{2}$$

$$(c) \pi$$

$$(d) \frac{3\pi}{2}$$

23. If  $\sin^{-1}\frac{5}{x} + \sin^{-1}\frac{12}{x} = \frac{\pi}{2}$ , then value of  $x$  is

$$(a) 13$$

$$(b) -13$$

$$(c) \pm 13$$

$$(d) 26$$

24. The value of  $\cos(2\cos^{-1}x + \sin^{-1}x)$  at  $x = \frac{1}{3}$  is

$$(a) \frac{-2\sqrt{2}}{3}$$

$$(b) \frac{2\sqrt{3}}{5}$$

$$(c) \frac{\pm 2\sqrt{2}}{3}$$

$$(d) 0$$

25. The number of all possible matrices of order  $2 \times 3$  with each entry 1 or -1 is

$$(a) 32$$

$$(b) 12$$

$$(c) 6$$

$$(d) 64$$

26. If  $A$  is of order  $m \times n$  and  $B$  is of order  $p \times q$ , then  $AB$  is defined only if

$$(a) m = q$$

$$(b) m = p$$

$$(c) n = p$$

$$(d) n = q$$

27. The determinant  $\begin{vmatrix} b^2 - ab & b - c & bc - ac \\ ab - a^2 & a - b & b^2 - ab \\ bc - ac & c - a & ab - a^2 \end{vmatrix}$  equals to

$$(a) abc(b-c)(c-a)(a-b)$$

$$(b) (b-c)(c-a)(a-b)$$

$$(c) (a+b+c)(b-c)(c-a)(a-b)$$

$$(d) \text{None of these}$$

28. If  $A = \begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$  be such that  $A^{-1} = KA$ , then value of  $K$  is

$$(a) \frac{1}{19}$$

$$(b) 1$$

$$(c) -19$$

$$(d) \frac{-1}{19}$$

29. The values of  $a$  so that the function  $f(x)$  defined by

$$f(x) = \begin{cases} \frac{\sin^2 ax}{x^2}, & x \neq 0 \\ 1, & x = 0 \end{cases} \text{ may be continuous at } x = 0 \text{ is}$$

$$(a) \pm 1$$

$$(b) 1$$

$$(c) -1$$

$$(d) \text{None of these}$$

30. The value of  $\log_x 2$  with respect to  $x$  is

$$(a) \frac{-1}{(\log_2 x)^2} \times \frac{1}{x \log_e 2}$$

$$(b) 0$$

$$(c) \frac{1}{\log x}$$

$$(d) \frac{1}{\log 2}$$

31. If  $f(x) = x^2 + 2x + 7$  then value of  $f'(3)$  is  
 (a) 18 (b) 8 (c) 10 (d) 3
32. The set of points where the function  $f$  given by  $f(x) = |2x - 1| \sin x$  is differentiable is  
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \left\{\frac{1}{2}\right\}$  (c)  $(0, \infty)$  (d) none of these
33. The minimum value of  $f(x) = 3 \cos^2 x + 4 \sin^2 x + \cos \frac{x}{2} + \sin \frac{x}{2}$  is  
 (a) 4 (b)  $3 + \sqrt{2}$  (c)  $4 + \sqrt{2}$  (d) none of these
34. The value of  $\int \frac{x dx}{(x^2 + 1)(x - 1)}$  equals to  
 (a)  $\frac{1}{2} \log|x - 1| - \frac{1}{4} \log|x^2 + 1| + \frac{1}{2} \tan^{-1} x + C$  (b)  $\frac{1}{2} \log|x + 1| + \frac{1}{4} \log|x^2 - 1| + \frac{1}{2} \tan^{-1} x + C$   
 (c)  $\log|x - 1| + \frac{1}{4} \log|x^2 + 1| + \frac{1}{2} \tan^{-1} x + C$  (d)  $\tan^{-1} \left( \frac{(x + 1)^2}{x} \right) + C$
35.  $\int_0^{\frac{2}{3}} \frac{dx}{4 + 9x^2}$  is equal to  
 (a)  $\frac{\pi}{6}$  (b)  $\frac{\pi}{12}$  (c)  $\frac{\pi}{24}$  (d)  $\frac{\pi}{4}$
36.  $\int_{\frac{1}{3}}^1 \frac{(x - x^3)^{1/3} dx}{x^4}$  is equal to  
 (a) 6 (b) 0 (c) 3 (d) 4
37. The area of a minor segment of the circle  $x^2 + y^2 = a^2$  cut off by the line  $x = \frac{a}{2}$  is  
 (a)  $\frac{a^2}{12} (4\pi - 3\sqrt{3})$  sq. units (b)  $\frac{a^2}{4} (4\pi - 3)$  sq. units  
 (c)  $\frac{a^2}{12} \times (3\pi - 4)$  sq. units (d) None of these
38. The solution of differential equation  $\frac{dy}{dx} + \frac{y}{x} = \sin x$  is  
 (a)  $x(y + \cos x) = \sin x + C$  (b)  $x(y - \cos x) = \sin x + C$   
 (c)  $xy \cos x = \sin x + C$  (d)  $x(y + \cos x) = \cos x + C$
39. The general solution of the differential equation of the type  $\frac{dx}{dy} + Px = Q$  is given by  
 (a)  $ye^{\int Pdy} = \int (Qe^{\int Pdy}) dy + C$  (b)  $ye^{\int Pdx} = \int (Qe^{\int Pdx}) dx + C$   
 (c)  $xe^{\int Pdy} = \int (Qe^{\int Pdy}) dy + C$  (d)  $xe^{\int Pdx} = \int Qe^{\int Pdx} dx + C$
40. The value of  $\lambda$  for which the volume of tetrahedron, whose vertices have position vector  $\hat{i} - 5\hat{j} + 9\hat{k}$ ,  $-\hat{i} - 2\hat{j} + 7\hat{k}$ ,  $4\hat{i} - \hat{j} + \lambda\hat{k}$  and  $7\hat{i} - 4\hat{j} + 7\hat{k}$  is 6 cubic units, is  
 (a) 7 (b) 6 (c) 8 (d) 9
41. If  $\vec{\alpha} + \vec{\beta} + \vec{\gamma} = a\vec{\delta}$ ,  $\vec{\beta} + \vec{\gamma} + \vec{\delta} = b\vec{\alpha}$  and  $\vec{\alpha}, \vec{\beta}, \vec{\gamma}$  are non coplanar and  $\vec{\alpha}$  is not parallel to  $\vec{\delta}$  then the value of  $\vec{\alpha} + \vec{\beta} + \vec{\gamma} + \vec{\delta}$  is  
 (a) 2 (b) 3 (c) 1 (d) 0

42. If  $\vec{a}, \vec{b}, \vec{c}$  are the position vectors of vertices  $A, B$  and  $C$  of a triangle then the area of the triangle is given by

- (a)  $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$  (b)  $\frac{1}{2}[\vec{a} \vec{b} \vec{c}]$  (c)  $\frac{1}{2}|\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}|$  (d) None of these

43. If  $D, E$  and  $F$  are mid points of the sides  $BC, CA$  and  $AB$  respectively of a triangle  $ABC$ , then  $\vec{AD} + \vec{BE} + \vec{CF}$  is equal to

- (a) 0 (b) 1 (c) 2 (d) None of these

44. The intercepts made by the plane  $2x - 3y + 5z + 4 = 0$  on the coordinate axes are

- (a)  $-2, \frac{4}{3}$  and  $-\frac{4}{5}$  (b)  $-2, -\frac{4}{3}$  and  $\frac{4}{5}$  (c)  $\frac{4}{3}, -\frac{4}{3}$  and  $\frac{7}{3}$  (d)  $-2, -\frac{4}{3}$  and  $-\frac{4}{5}$

45. The angle between the line  $(5\hat{i} - \hat{j} - 4\hat{k}) + \lambda(2\hat{i} - \hat{j} + \hat{k})$  and the plane  $\vec{r} \cdot (3\hat{i} - 4\hat{j} - \hat{k}) + 5 = 0$  is

- (a)  $\sin^{-1}\left(\frac{5}{2\sqrt{91}}\right)$  (b)  $\sin^{-1}\left(\frac{9}{2\sqrt{39}}\right)$  (c)  $\sin^{-1}\left(\frac{7}{3\sqrt{80}}\right)$  (d) None of these

46. The vector equation of the line  $\frac{x-5}{3} = \frac{y+4}{7} = \frac{z-6}{2}$  is

- (a)  $\vec{r} = (5\hat{i} - 4\hat{j} + 6\hat{k}) + \lambda(3\hat{i} + 7\hat{j} + 2\hat{k})$  (b)  $\vec{r} = (5\hat{i} - 3\hat{j} - 2\hat{k}) + \lambda(2\hat{i} + 6\hat{j} - 3\hat{k})$   
(c)  $\vec{r} = (5\hat{i} - 3\hat{j} - 2\hat{k}) + \lambda(3\hat{i} - 7\hat{j} - 2\hat{k})$  (d) None of the above

47. If  $O$  is the origin and  $A$  is  $(a, b, c)$ , then the direction cosines of the line  $OA$  and the equation of plane through  $A$  at right angle to  $OA$  is

- (a)  $ax + by + cz = a^2 + b^2 + c^2$  (b)  $ax + by + cz = a^2 + b^2 + c^2$   
(c)  $ax - by + cz = a^2 + b^2 - c^2$  (d) None of these

48. Let  $A$  and  $B$  be two events. If  $P(A) = 0.2, P(B) = 0.4, P(A \cup B) = 0.6$ , then  $P(A/B)$  is equal to

- (a) 0.8 (b) 0.3 (c) 0 (d) 0.5

49. Let  $A$  and  $B$  be two events such that  $P(A) = 0.6, P(B) = 0.2$  and  $P(A/B) = 0.5$  then  $P(A'/B')$  equals

- (a)  $\frac{1}{10}$  (b)  $\frac{3}{10}$  (c)  $\frac{3}{8}$  (d)  $\frac{6}{7}$

50. Let  $X$  be a discrete random variable. The probability distribution of  $X$  is given below.

$X$	30	10	-10
$P(X)$	$\frac{1}{5}$	$\frac{3}{10}$	$\frac{1}{2}$

$E(X)$  equals to

- (a) 6 (b) 4 (c) 3 (d) -5