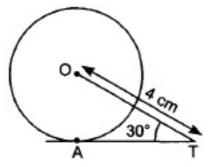
CBSE Test Paper 03 Chapter 9 Some Applications of Trigonometry

- 1. If the height of the tower is $\sqrt{3}$ times of the length of its shadow, then the angle of elevation of the sun is (1)
 - a. 15°
 - b. 30°
 - c. 60°
 - d. 45°
- 2. A ramp for disabled people in a hospital must slope at not more than 30°. If the height of the ramp has to be 1 m, then the length of the ramp be **(1)**
 - a. 3 m
 - b. 1 m
 - c. 2 m
 - d. $\sqrt{3}$ m
- 3. In a right triangle ABC, $\angle C~=~90^\circ$. If AC = $\sqrt{3}\,$ BC and $\angle B~=\phi,$ then find its value (1)
 - a. 45°
 - b. 30°
 - c. None of these
 - d. 60°
- 4. The angle of elevation of the top of a hill at the foot of a tower is 60° and the angle of elevation of the top of the tower from the foot of the hill is 30°. If the tower is 50m high, then the height of the hill is **(1)**
 - a. $50\sqrt{3}$ m
 - b. 150m
 - c. $150\sqrt{3}$ m
 - d. 100 $\sqrt{3}$ m
- 5. A kite is flying at a height of 90 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60° . The length of the string, assuming that there is no slack in the string is **(1)**

- a. $90\sqrt{3}$ m
- b. $60\sqrt{3}$ m
- c. 90 m
- d. 45 m
- 6. At some time of the day the length of the shadow of a tower is equal to its height. Find the sun's altitude at that time. **(1)**
- 7. If the elevation of the sun at a given time is 30°, then find the length of the shadow cast by a tower of 150 feet height at that time. **(1)**
- 8. A circus artist is climbing from the ground along a rope stretched from the top of a vertical pole and tied at the ground. The height of the pole is 12 m and the angle made by the rope with ground level is 30^o. Calculate the distance covered by the artist in climbing to the top of the pole. (1)
- 9. In figure, AT is a tangent to the circle with centre O such that OT = 4 cm and $\angle OTA = 30^{\circ}$. Find AT. **(1)**



- 10. A tower stands vertically on the ground. From a point on the ground which is 20 m away from the foot of the tower, the angle of elevation of the top of the tower is found to be 60° . Find the height of the tower. **(1)**
- 11. A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle 30° with it. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree. (2)
- 12. A kite is flying at a height of 90 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60^o. Find the length of the string assuming that there is no slack in the

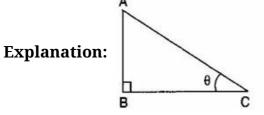
string. $\sqrt{3}=17.32]$ (2)

- 13. Two ships are approaching a light house from opposite directions. The angle of depression of two ships from top of the light house are 30^o and 45^o. If the distance between two ships is 100 m. Find the height of light-house. (2)
- 14. A tree breaks due to the storm and the broken part bends so that the top of the tree touches the ground making an angle of 30^o with the ground. The distance from the foot of the tree to the point where the top touches the ground is 10 metres. Find the height of the tree. **(3)**
- 15. The angle of elevation of an aeroplane from a point on the ground is 60° . After a flight of 15 seconds, the angle of elevation changes to 30° . If the aeroplane is flying at a constant height of $1500\sqrt{3}$ m, find the speed of the plane in km/hr. (3)
- 16. At a point on level ground, the angle of an elevation of a vertical tower is found to be such that its tangent is $\frac{5}{12}$ on walking 192 m towards the tower, the tangent of the angle of elevation is $\frac{3}{4}$. Find the height of the tower. (3)
- 17. A flagstaff stands on the top of a 5 m high tower. From a point on the ground, the angle of elevation of the top of the flagstaff is 60^o and from the same point, the angle of elevation of the top of the tower is 45^o. Find the height of the flagstaff. (3)
- 18. The angle of elevation of a cliff from a fixed point is θ . After going up a distance of k metres towards the top of the cliff at an angle of ϕ , it is found that the angle of elevation is α . Show that the height of the cliff is $\frac{k(\cos \phi \sin \phi \cot \alpha)}{\cot \theta \cot \alpha}$ metres. (4)
- 19. The horizontal distance between two towers is 140 m. The angle of elevation of the top of the first tower, when seen from the top of the second tower is 30°. If the height of the second tower is 60 m, find the height of the first tower. (4)
- 20. The angle of elevation of a cloud from a point 120 m above a lake is 30° and the angle of depression of its reflection in the lake is 60° . Find the height of the cloud. **(4)**

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Solution

1. c. 60°



Let the length of the shadow be x meters. Then the height of the tower be $\sqrt{3}x$ meter. $\therefore \tan \theta = \frac{AB}{BC} \Rightarrow \tan \theta = \frac{\sqrt{3}x}{x}$ $\Rightarrow \tan \theta = \sqrt{3} \Rightarrow \tan \theta = \tan 60^{\circ}$ $\Rightarrow \theta = 60^{\circ}$

2. c. 2 m

Explanation: Let height of the ramp be AB = 1 m, the slope of the ramp AC and angle of elevation = $heta=30^\circ$

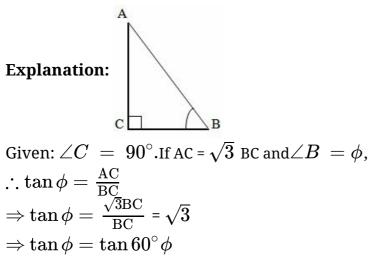
In triangle ABC,

$$\sin 30^{\circ} = \frac{AB}{AC}$$

 $\Rightarrow \frac{1}{2} = \frac{1}{AC}$
 $\Rightarrow AC = 2$ meters

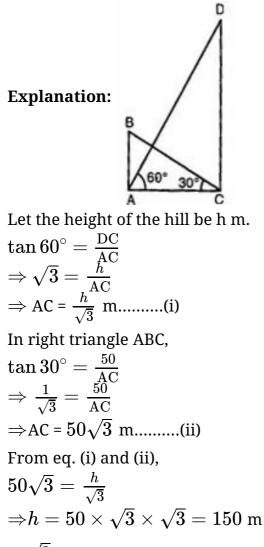
Therefore, the length of the ramp is 2 m.

3. d. 60°

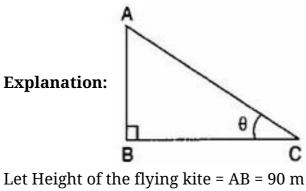


$$\Rightarrow \phi = 60^{\circ}$$

4. b. 150m



5. b. $60\sqrt{3}$ m



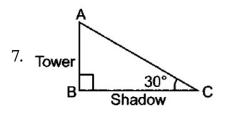
Let Height of the flying kite = AB = 90 m And the angle of elevation = $\theta = 60^{\circ}$ And the length of the string = AC $\therefore \sin 60^{\circ} = \frac{AB}{AC}$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{90}{\text{AC}}$$
$$\Rightarrow \text{AC} = \frac{90 \times 2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 60\sqrt{3} \text{ m}$$

6. Tower

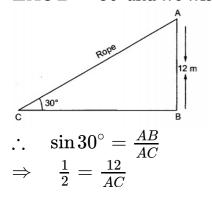
given, the length of the shadow of a tower is equal to its height i.e. AB=BC

In right riangle ABC $an heta = rac{AB}{BC}$ $\Rightarrow an heta = 1$ $\Rightarrow heta = 45^{\circ}$



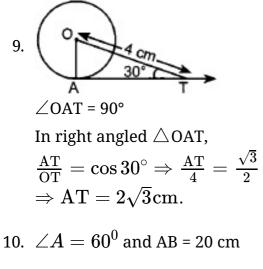
height of the tower = 150 feets In right $\triangle ABC$ $\tan \theta = \frac{AB}{BC}$ $\frac{150}{BC} = \frac{1}{\sqrt{3}}$ BC = $150\sqrt{3}$ feet

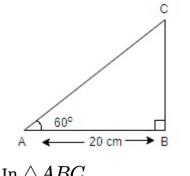
8. Clearly, distance covered by the artist is equal to the length of the rope AC. Let AB be the vertical pole of height 12 m. It is given that $\angle ACB = 30^{\circ}$. Thus, in right-angled triangle ABC, we have Perpendicular AB = 12 m, $\angle ACB = 30^{\circ}$ and we wish to find hypotenuse AC.



$$\Rightarrow \quad AC = 24 \mathrm{m}$$

Hence, the distance covered by the circus artist is 24 m.





$$\tan \Box ABC,$$

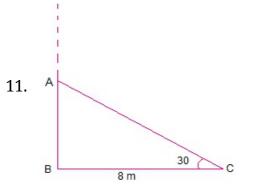
$$\tan \theta = \frac{P}{B} = \frac{CB}{AB} = \frac{CB}{20}$$

$$\Rightarrow \tan 60^{\circ} = \frac{CB}{20}$$

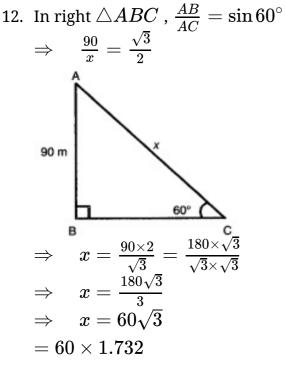
$$\Rightarrow \sqrt{3} = \frac{CB}{20} [\because \tan 60^{\circ} = \sqrt{3}]$$

$$\Rightarrow CB = 20\sqrt{3}$$

Therefore, Height of tower = $20\sqrt{3}~m$

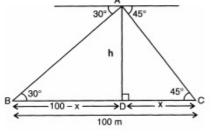


Let AC be the broken part of the tree. ... Total height of the tree = AB + AC In right \triangle ABC, $\cos 30^{\circ} = \frac{BC}{AC}$ $\Rightarrow \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{2} = \frac{8}{AC}$ $\Rightarrow AC = \frac{16}{\sqrt{3}}$ Also, $\tan 30^{\circ} = \frac{AB}{BC}$ $\Rightarrow \frac{1}{\sqrt{3}} = \frac{AB}{8}$ $\Rightarrow AB = \frac{8}{\sqrt{3}}$ Total height of the tree = AB + AC = $\frac{16}{\sqrt{3}} + \frac{8}{\sqrt{3}} = \frac{24}{\sqrt{3}}$



Hence length of string = 103.92 m.

13. Let AD be the height (h) of the light house and BC is the distance between two ships



Given, BC = 100 m, BD = 100 - x, DC = x (let) In riangle ADC ,tan $45^\circ = rac{h}{DC}$

$$\Rightarrow DC = h.$$

$$\Rightarrow x = h...(i)$$

In \triangle ABD, $\tan 30^{\circ} = \frac{h}{100 - DC}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{100 - x}$$

$$\Rightarrow 100 - x = h\sqrt{3}$$

$$\Rightarrow 100 - h = h\sqrt{3} [By (i)]$$

$$\Rightarrow 100 = h + h\sqrt{3}$$

$$\Rightarrow 100 = h(1 + \sqrt{3})$$

$$\Rightarrow h = \frac{100}{1 + \sqrt{3}}$$

Rationalising numerator and deno

Rationalising numerator and denominator

$$\Rightarrow h = \frac{100}{(\sqrt{3}+1)} \times \frac{(\sqrt{3}-1)}{(\sqrt{3}-1)} \Rightarrow h = \frac{100(\sqrt{3}-1)}{3-1} = 50(\sqrt{3}-1) = 50(1.732 - 1) = 50 \times 0.732 = 36.6 m Height of light house = 36.6 m.$$

14. Let AB be the tree broken at point D, so that AD takes the position DC.

Let DB = x m, AD = DC = y m
In
$$\triangle DBC$$
, we have $\cos 30^{\circ} = \frac{10}{y}$
 $\Rightarrow \frac{\sqrt{3}}{2} = \frac{10}{y} \Rightarrow y = \frac{20}{\sqrt{3}}$(i)
Again in \triangle DBC, we have $\sin 30^{\circ} = \frac{x}{y}$
 $\Rightarrow \frac{1}{2} = \frac{x}{\frac{20}{\sqrt{3}}}$ [From (i)]
 $\Rightarrow 2\sqrt{3}x = 20 \Rightarrow x = \frac{20}{2\sqrt{3}} = \frac{10}{\sqrt{3}}$

- : height of the tree = x + y = $\left(\frac{20}{\sqrt{3}} + \frac{10}{\sqrt{3}}\right)$ m = $\frac{30}{\sqrt{3}}$ m = $10\sqrt{3}$ m : height of the tree = $10\sqrt{3}$ m
- 15. Let A and B be the two positions of the aeroplane.

Let
$$AC \perp OX$$
 and $BD \perp OX$. Then,
 $\angle COA = 60^{\circ}, \angle DOB = 30^{\circ}$
and $AC = BD = 1500\sqrt{3}m$.
From right $\triangle OCA$, we have
 $\frac{OC}{AC} = \cot 60^{\circ} = \frac{1}{\sqrt{3}}$
 $\Rightarrow \frac{OC}{1500\sqrt{3}} = \frac{1}{\sqrt{3}} \Rightarrow OC = 1500m$
From right $\triangle ODB$, we have
 $\frac{OD}{BD} = \cot 30^{\circ} = \sqrt{3} \Rightarrow \frac{OD}{1500\sqrt{3m}} = \sqrt{3}$
 $\Rightarrow OD = (1500 \times 3)m = 4500m$.
 $\therefore CD = (OD - OC) = (4500 - 1500)m = 3000m$.
Thus, the aeroplane covers 300m in 15 seconds.
 \therefore speed of the aeroplance $= \left(\frac{3000}{15} \times \frac{60 \times 60}{1000}\right) \text{ km/hr}$

= 720 km /hr.

16.
$$\alpha$$
 β

Suppose height of tower is h meter

In
$$riangle ABD$$

 $aneta=rac{h}{x}=rac{3}{4}$ (i)
In $riangle ABC$

$$\tan \alpha = \frac{h}{192+x}$$

$$\Rightarrow \frac{h}{192+x} = \frac{5}{12}$$
.....(ii)
(i) + (ii)
$$\frac{\frac{h}{x}}{\frac{h}{192+x}} = \frac{\frac{3}{4}}{\frac{5}{12}}$$

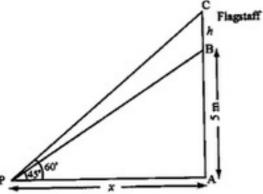
$$\Rightarrow x = 240$$

Putting the value of x in equation 1 to find the value of h(height of tower)

h = 180 m Hence, the height of the tower = 180 m

17. Let the height of flagstaff = h m = CB

height of tower = 5 m = AB Height of top of flagstaff from ground = (h + 5) m = AC Let distance of point P from tower = x Using $\triangle PAB$, $\frac{x}{5} = \cot 45^0 \rightarrow \frac{x}{5} = 1 \implies x = 5m$ Using $\triangle PAC$, $\frac{x}{h+5} = \cot 60^\circ$ $\Rightarrow \frac{x}{h+5} = \frac{1}{\sqrt{3}}$ $\Rightarrow x = \frac{h+5}{\sqrt{3}}$(ii) From (i) and (ii), we get $\frac{h+5}{\sqrt{3}} = 5$ $\Rightarrow h + 5 = 5\sqrt{3}$ $\therefore h = 5\sqrt{3} - 5$ $= 5(1.73 \cdot 1) = 5 \times .73 = 3.65$ m \therefore the height of the flagstaff is 3.65 m approx.



18. Let AB be the cliff and O be the fixed point such that the angle of elevation of the cliff

from O is θ i.e., $\angle AOB = \theta$. Let $\angle AOC = \phi$ and OC = k metres. From C draw CD and CE perpendiculars on AB and OA respectively. Then, $\angle DCB = \alpha$. Let h be the height of the cliff AB.

In riangle OCE, we have

$$\begin{array}{c} & & \\ & &$$

19. Let AB and CD be two towers of height h metres and 60 metres respectively such that

the distance AC between them is 140 m. The angle of elevation of top B of tower AB as seen from D (top of tower CD) is 30°.

