

CBSE Test Paper 02
CH-10 Straight Lines

1. If (x, y) are the coordinates of point in the plane, then $\begin{vmatrix} 3 & 4 & 2 \\ 5 & 8 & 2 \\ x & y & 2 \end{vmatrix} = 0$ represents
- a. a straight line parallel to x axis
 - b. a straight line
 - c. a circle
 - d. none of these
2. A line L passes through the points $(1, 1)$ and $(2, 0)$ and another line M which is perpendicular to L passes through the point $(\frac{1}{2}, 0)$. The area of the triangle formed by these lines with y axis is :
- a. $\frac{25}{8}$
 - b. $\frac{25}{16}$
 - c. none of these
 - d. $\frac{25}{4}$
3. The line which passes through the point $(0, 1)$ and perpendicular to the line $x - 2y + 11 = 0$ is
- a. none of these
 - b. $2x + y - 1 = 0$
 - c. $2x - y + 1 = 0$
 - d. $2x - y + 3 = 0$
4. The equation $y - y_1 = m(x - x_1), m \in R$, represents all lines through the point

(x_1, y_1) except the line

- a. parallel to Y axis
- b. parallel to the line $x - y = 0$
- c. none of these
- d. parallel to X axis

5. Two opposite vertices of a rectangle are $(1, 3)$, $(5, 1)$. If the equation of a diagonal of this rectangle is $y = 2x + c$, then the value of c is

- a. 2
- b. -4
- c. -9
- d. 1

6. Fill in the blanks:

If a line is parallel to y-axis at a distance 'b' from y-axis then its equation is _____.

7. Fill in the blanks:

If a line is at a distance 'a' and parallel to x-axis, then the equation of the line is _____.

8. Find the slope of line, whose inclination is 30° .

9. Find the new coordinates of point $(3, -5)$, if the origin is shifted to the point $(-3, -2)$.

10. If two poles standing at the points $A(1, -2)$ and $B(-3, 5)$, then find the distance between the poles.

11. Find the equations of the line which have slope $\frac{1}{2}$ and cuts off an intercept

- i. -5 on Y-axis and
- ii. 4 on X-axis.

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12. Find the equation of the line joining the point (3,5) to the point of intersection of the lines $4x + y - 1 = 0$ and $7x - 3y - 35 = 0$.
 13. Find the direction in which a straight line must be drawn through the point (-1, 2) so that its point of intersection with the line $x + y = 4$ may be at a distance of 3 units from this point.
 14. Find the area of the triangle formed by the lines $y - x = 0$, $x + y = 0$ and $x - k = 0$.
 15. In the $\triangle ABC$ with vertices A(2, 3), B(4, -1) and C(1, 2), find the equation and length of altitude from the vertex A.

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Solution

1. (b) a straight line

Explanation:

The given determinant can be written as $2 \begin{vmatrix} 3 & 4 & 1 \\ 5 & 8 & 1 \\ x & y & 1 \end{vmatrix} = 0$

On expansion we get

$$2[3(8-y) - 4(5-x) + 1(5y-8x)]$$

On simplifying the equation $2(-4x+2y+4) = 0$ represents a straight line.

2. (b) 25/16

Explanation:

The equation of the line joining the two points (x_1, y_1) and (x_2, y_2) is

$$\frac{y-y_1}{y_2-y_1} = \frac{x-x_1}{x_2-x_1}$$

The given points are $(1,1)$ and $(2,0)$

On substituting the values we get

$$\frac{y-1}{0-1} = \frac{x-1}{2-1}$$

On simplifying we get,

$$x+y-2=0$$

The line which is perpendicular to this line is $x-y+k=0$

Since it passes through $(1/2, 0)$

$$(1/2) - 0 = k$$

This implies $k = -1/2$

Hence the equation of this line is $x - y - 1/2 = 0$

On solving these two lines we get the point of intersection as $(5/4, 3/4)$

The point which line $x + y - 2 = 0$ cuts the Y axis is $(0, 2)$ and the point which the line $x - y - 1/2 = 0$ cuts the Y axis is $(0, -1/2)$

Hence the area of the triangle = $[1/2] \times [5/4] \times [5/4] = 25/16$ sq units

3. (b) $2x + y - 1 = 0$

Explanation: The line which is perpendicular to the given line is $2x + y + k = 0$

Since it passes through $(0, 1)$

$$2(0) + 1 + k = 0$$

This implies $k = -1$

Hence the equation of the required line is $2x + y - 1 = 0$

4. (a) parallel to Y axis

Explanation:

The vertical lines which are parallel to Y axis has undefined slopes. Hence the slope of the line 'm' will be undefined.

Therefore the above equation of the line will represent all lines through (x_1, y_1) except the line parallel to Y-axis

5. (b) -4

Explanation: Slope of the line joining the given points $(1, 3)$ and $(5, 1)$ is $\frac{1-3}{5-1} = -1/2$

Hence the line having slope $-1/2$ is $y = [-1/2]x + c$

If the diagonal is $y = 2x + c$, then $c = -4$

6. $x = \pm b$

7. $y = \pm a$

8. Let θ be the inclination of a line with X-axis, then its slope = $\tan \theta$

$$\theta = 30^\circ$$

$$\Rightarrow \text{Slope} = \tan 30^\circ$$

$$= \frac{1}{\sqrt{3}}$$

9. The coordinates of the new origin are $h = -3$ and $k = -2$ and the original coordinates are given to be $x = 3, y = -5$.

Let new coordinates of the point be (X, Y) . Then,

$$X = (x - h) = 3 - (-3)$$

$$= 6 \text{ and}$$

$$Y = y - k = -5 - (-2) = -3$$

Hence, the coordinates of the point $(3, -5)$ in the new system are $(6, -3)$.

10. Given points are $A(1, -2)$ and $B(-3, 5)$.

Now, distance between two poles

$$\begin{aligned} &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{(-3 - 1)^2 + (5 + 2)^2} = \sqrt{(-4)^2 + (7)^2} \\ &= \sqrt{16 + 49} = \sqrt{65} \end{aligned}$$

11. Given, $m = \text{slope of the line} = \frac{1}{2}$

and $c = \text{intercept of the line on Y-axis} = -5$

Hence, required equation of the line is

$$y = \frac{1}{2}x - 5 \Rightarrow x - 2y - 10 = 0$$

Also, $d = \text{intercept of the line on X-axis} = 4$.

Hence, required equation of the line is,

$$y = \frac{1}{2}(x - 4) \Rightarrow x - 2y - 4 = 0$$

12. Let $P(x, y)$ be the point of intersection of the lines $4x + y - 1 = 0$ and $7x - 3y - 35 = 0$.

$$\text{Now, } y = 1 - 4x$$

Thus, $7x - 3(1 - 4x) - 35 = 0$ [putting the value of y]

$$7x - 3 + 12x - 35 = 0$$

$$19x - 38$$

$$x = 2$$

$$\Rightarrow y = 1 - 4x - 1 - 8 = -7$$

\therefore Let P (2, -7) and Q (3, 5)

The equation of the line PQ is

$$y - y_1 = m(x - x_1)$$

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - (-7) = \frac{5 - (-7)}{3 - 2} (x - 2)$$

$$y + 7 = 12(x - 2)$$

$$y - 12x = -31$$

$$12x - y - 31 = 0$$

13. Let the required line makes an angle θ with the positive direction of x-axis. Then equation of line is

$$\frac{x - (-1)}{\cos \theta} = \frac{y - 2}{\sin \theta} = r \Rightarrow \frac{x + 1}{\cos \theta} = \frac{y - 2}{\sin \theta} = r$$

It is given that $r = 3$

$$\therefore \frac{x + 1}{\cos \theta} = \frac{y - 2}{\sin \theta} = 3$$

$$\therefore x + 1 = 3 \cos \theta \Rightarrow x = 3 \cos \theta - 1$$

$$\text{and } y - 2 = 3 \sin \theta \Rightarrow y = 3 \sin \theta + 2$$

Since this point on the line $x + y = 4$

$$\therefore 3 \cos \theta - 1 + 3 \sin \theta + 2 = 4$$

$$\therefore 3 \cos \theta + 3 \sin \theta = 3 \Rightarrow \cos \theta + \sin \theta = 1$$

Squaring both sides, we have

$$\cos^2 \theta + \sin^2 \theta + 2 \sin \theta \cos \theta = 1$$

$$\Rightarrow 1 + \sin 2\theta = 1 \Rightarrow \sin 2\theta = 0 \Rightarrow 2\theta = 0 \Rightarrow \theta = 0$$

Which shows that required line is parallel to x-axis .

14. The equation of lines are

$$y - x = 0 \dots\dots(i)$$

$$x + y = 0 \dots\dots(ii)$$

$$x - k = 0 \dots\dots(iii)$$

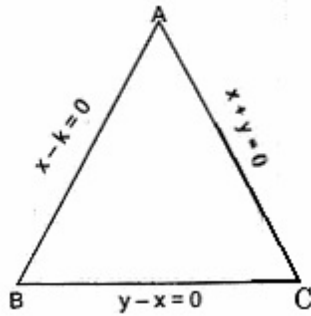
By solving (i) and (ii), we get the coordinates of point C.

\therefore Coordinate of C are (0, 0).

By solving (ii) and (iii), we get the coordinates of point A.

∴ Coordinate of A are (k, -k).

By solving (i) and (iii), we get the coordinates of point B.



∴ coordinates of B are (k, k)

$$\begin{aligned}\therefore \text{Area of } \triangle ABC &= \frac{1}{2} \begin{vmatrix} k & -k & 1 \\ k & k & 1 \\ 0 & 0 & 1 \end{vmatrix} \\ &= \frac{1}{2} [(k^2 + k^2 + (0 - 0)) + (0 - 0)] \\ &= \frac{1}{2} \times 2k^2 \\ &= k^2 \text{ sq. unit}\end{aligned}$$

15. Given, vertices of a $\triangle ABC$ are A(2, 3), B(4, -1) and C(1, 2)

We know that altitude from a vertex of a triangle is perpendicular to the opposite side.

∴ Line AD \perp line BC.

Then, the slope of AD \times Slope of BC = -1

$$\Rightarrow m \times \frac{y_2 - y_1}{x_2 - x_1} = -1$$

$$\Rightarrow m \times \frac{2+1}{1-4} = -1 \quad [\because x_1 = 4, y_1 = -1, x_2 = 1, y_2 = 2]$$

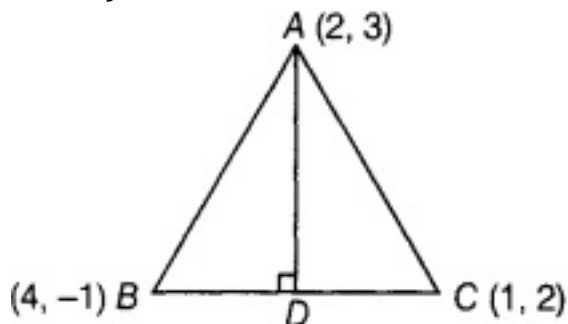
$$\Rightarrow m \times \frac{3}{-3} = -1 \Rightarrow m = 1$$

Hence, equation of AD, by using $y - y_1 = m(x - x_1)$ is

$$y - 3 = 1(x - 2)$$

$$\Rightarrow x - y - 2 + 3 = 0$$

$$\Rightarrow x - y + 1 = 0$$



Now, equation of BC by using $y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$

is $y + 1 = \frac{2+1}{1-4}(x - 4)$ [$\because x_1 = 4, y_1 = -1, x_2 = 1, y_2 = 2$]

$$\Rightarrow y + 1 = \frac{3}{-3}(x - 4)$$

$$\Rightarrow y + 1 = -x + 4$$

$$\Rightarrow x + y - 3 = 0$$

Now, length of AD = Perpendicular distance from (2, 3) to the line BC

$$= \left| \frac{2+3-3}{\sqrt{1^2+1^2}} \right| = \frac{2}{\sqrt{2}} = \sqrt{2} \text{ unit}$$