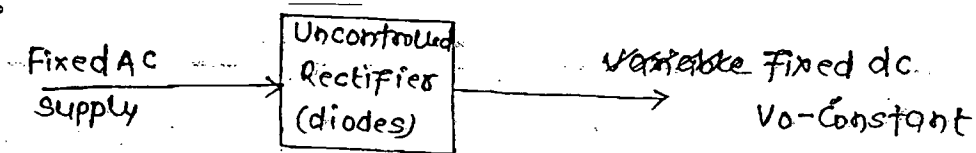
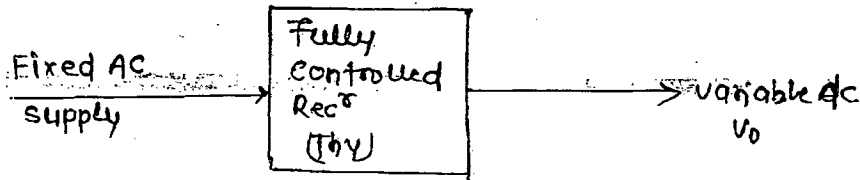


Phase Controlled Rectifier

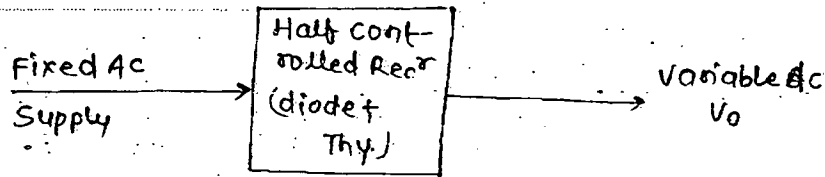
* Uncontrolled Rectifier →



Fully controlled Rectifier → (Full Converter) 2 quadrant operations



Half controlled Rectifier → (Semi Converter) one quadrant operation.

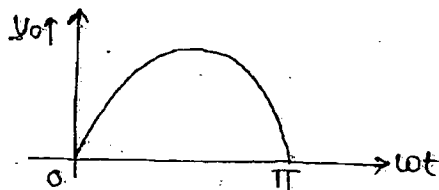


Classification of Converter based on pulse no. of the converter →

Pulse no. 'm' → pulse no. gives the no. of the o/p pulse for 1 cycle AC source voltage.

(1) One pulse con^r →

1- ϕ half wave rect.

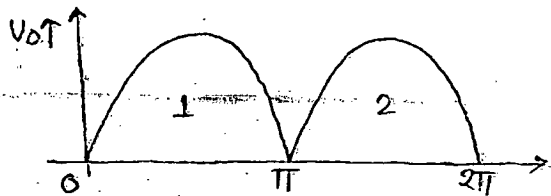


$$T_o = \frac{2\pi}{m} = \frac{2\pi}{1} \Rightarrow T_o = 2\pi \text{ rad.}$$

$$f_o = f_s$$

(2) Two pulse con^r →

1- ϕ full wave rec^r



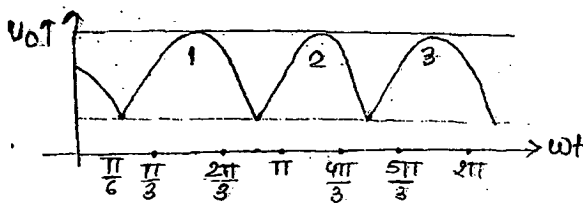
$$T_o = \frac{2\pi}{2} = \pi \text{ rad}$$

$$f_o = 2f_s$$

$$T_o = \text{Time period pulse in rad} = \frac{2\pi}{m} (\text{rad})$$

(3) 3 pulse con^r →

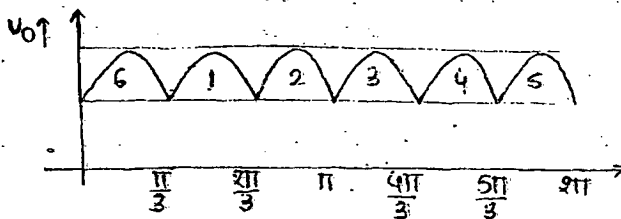
3- ϕ half wave rectifier



$$T_o = \frac{2\pi}{3} = 120^\circ$$

$$f_o = 3f_s$$

(4) 6 pulse con^r →



$$T_o = \frac{2\pi}{6} = \frac{\pi}{3} \text{ rad}$$

$$f_o = 6f_s$$

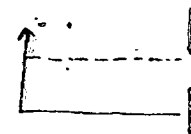
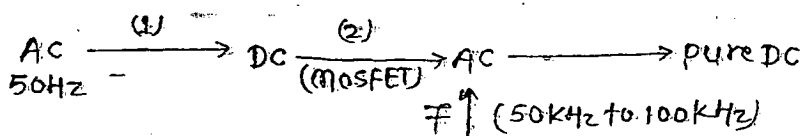
$$f_o = m f_s$$

where f_o = o/p ripple freq.

f_s = supply freq.

$m \uparrow, T_o \downarrow, f_o \uparrow, \text{ripple vol.} \downarrow \therefore \text{Harmonics} \downarrow$

Bricks →



* Effect of harmonics on the performance of dc motor →

* Harmonics overheat the m/c wdg, & Hence we can't use (utilise) the m/c to its full capacity.

Therefore we must derate the m/c when fed to con^r.

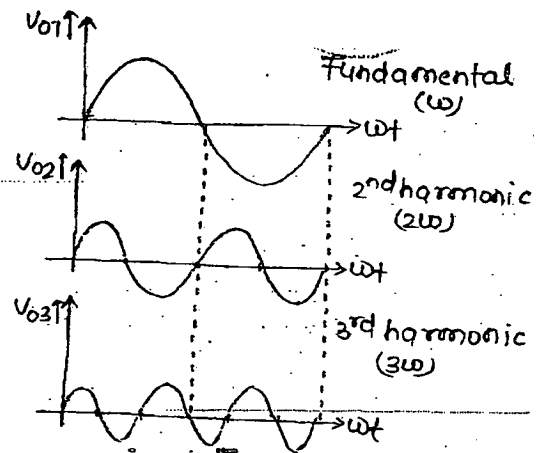
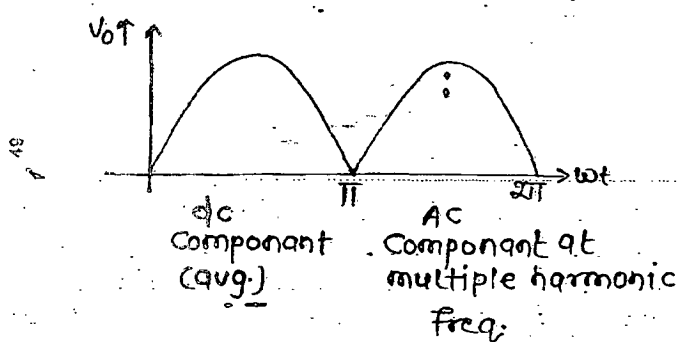
* Harmonics produce pulsating torque in rotor & hence smooth rotation may not be possible if it is used for power motors.

* The rotor inertia will damp for

* This pulsating torque produced by harmonics & hence smooth rotation is possible for bigger m/c.

Harmonics Analysis on the dc side of the converter →

Let us consider a 2 pulse converter



* Mathematical Formula for Fourier analysis →

$$V_o = a_0 + \sum_{n=1}^{\infty} (a_n \cos n\omega t + b_n \sin n\omega t)$$

(avg.)

$$V_o = a_0 + \sum_{n=1}^{\infty} C_n \sin(n\omega t + \phi_n)$$

$$\text{where } C_n = \sqrt{a_n^2 + b_n^2}$$

O/p rms voltage

$\phi_n = n^{\text{th}}$ harmonic displacement angle.

$$V_{or} = \sqrt{V_0^2 + V_{o1}^2 + V_{o2}^2 + V_{o3}^2 + \dots}$$

For all the dc loads avg. value is responsible to deliver the useful power.

$$V_{or}^2 = V_0^2 + V_{o1}^2 + V_{o2}^2 + \dots$$

$$V_{or}^2 - V_0^2 = V_{o1}^2 + V_{o2}^2 + \dots$$

$$\sqrt{V_{or}^2 - V_0^2} = \sqrt{V_{o1}^2 + V_{o2}^2 + \dots} = V_{or}$$

Voltage Ripple Factor (VRF) → It is a measure of harmonics on the dc side of converter.

$$VRF = \frac{\sqrt{V_{or}^2 - V_0^2}}{V_0}$$

$$VRF = \sqrt{\left(\frac{V_{or}}{V_0}\right)^2 - 1}$$

Form factor →

$$FF = \frac{V_{or}}{V_0}$$

$$VRF = \sqrt{FF^2 - 1}$$

Perfect dc →

(1.) No ripple

(2.) $V_{or} = V_0$

(3.) $FF = 1$

(4.) $VRF = 0$ (No harmonics)

Significance of FF:-

(1.) Without harmonics $FF = 1$

(2.) With harmonics $FF > 1$

(3.) As the FF decreases & reaches to unity then smoothness of waveform is improved towards dc.

(4.) FF gives the information on shape of waveform on dc side of converter.

Harmonics analysis of the AC side of Converter →

Let us consider an inverter

- * The o/p vol. waveform of the inverter may not be pure sinusoidal, it may contain harmonics.
- * For all the ac loads fundamental component is responsible to deliver 'useful power'.

$$V_{or} = \sqrt{V_0^2 + V_{01}^2 + V_{02}^2 + \dots}$$

$$\sqrt{V_{or}^2 - V_{01}^2} = \sqrt{V_0^2 + V_{02}^2 + \dots}$$

Total harmonic distortion (THD) → It is measure of harmonics on AC side of the conv.

$$THD = \frac{\sqrt{V_{or}^2 - V_{01}^2}}{V_{01}}$$

$$THD = \sqrt{\left(\frac{V_{or}}{V_{01}}\right)^2 - 1}$$

Distortion Factor 'g' → It gives the information of waveform on AC sides.

$$g = \frac{V_{01}}{V_{or}}$$

$$THD = \sqrt{\frac{1}{g^2} - 1}$$

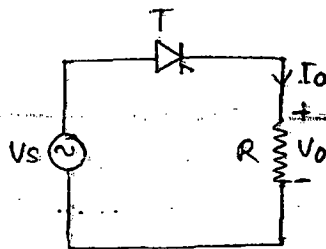
Perfect AC →

- (1.) $V_{or} = V_{01}$
- (2.) $g = 1$
- (3.) $THD = 0$ (No harmonics)

Significance of distortion factor →

- (1.) Without harmonics $g = 1$
- (2.) With harmonics $g < 1$
- (3.) As g value is increased & approaches unity then smoothness of waveform is improved towards sinusoidal.

(1) 1- ϕ Half wave Rectifier (One pulse converter) $\rightarrow$



$$\omega t_c = \pi \text{ rad}$$

$$t_c = \frac{\pi}{\omega} \text{ sec}$$

$$V_0 = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t d(\omega t)$$

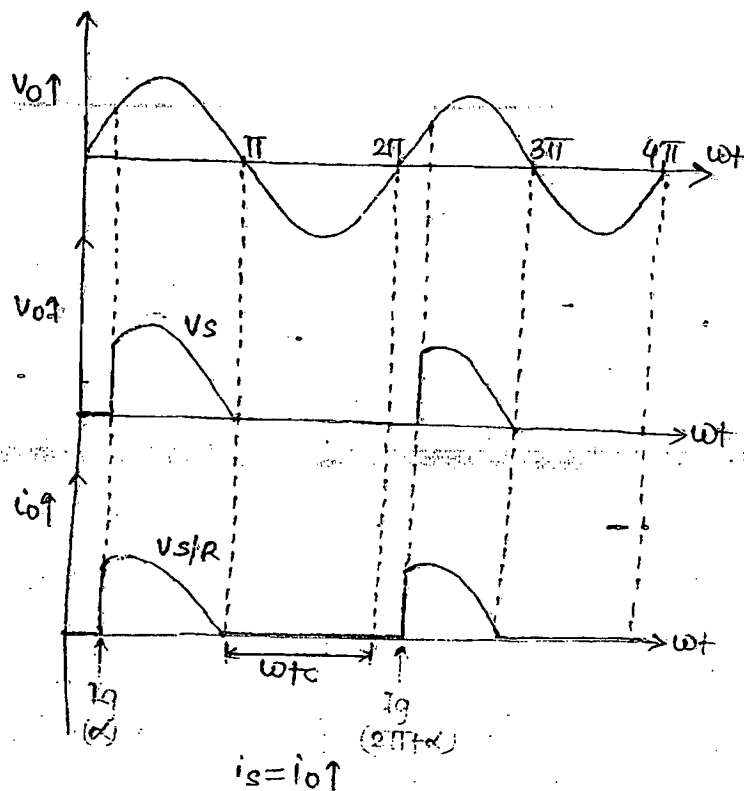
$$= \frac{V_m}{2\pi} (-\cos \omega t)_{\alpha}^{\pi}$$

$$V_0 = \frac{V_m}{2\pi} [-\cos \pi + \cos \alpha]$$

$$V_0 = \frac{V_m}{2\pi} (1 + \cos \alpha)$$

$$I_0 = \frac{V_0}{R} = \frac{V_m}{2\pi R} (1 + \cos \alpha)$$

$$I_0 = \frac{V_m}{2\pi R} (1 + \cos \alpha) = (I_s)_{avg.}$$



Drawback $\rightarrow$ The source current contains dc components & saturates the supply T/F core.

Therefore HWR is generally not preferred for applications.

$$V_{or} = \left[\frac{1}{2\pi} \int_{\alpha}^{\pi} V_m^2 \sin^2 \omega t d(\omega t) \right]^{1/2}$$

$$V_{or} = \left[\frac{V_m^2}{2\pi} \left\{ (\omega t)_{\alpha}^{\pi} - \frac{1}{2} (\sin 2\omega t)_{\alpha}^{\pi} \right\} \right]^{1/2}$$

$$V_{or} = \left[\frac{V_m^2}{2\pi} \left\{ (\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right\} \right]^{1/2} = \frac{V_m}{2\sqrt{2}\pi} \left[(\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right]^{1/2}$$

$$V_{or} = \frac{V_m}{\sqrt{2}T_0} \left[(1-\alpha) + \frac{1}{2}(\sin 2\alpha - \sin 2\omega t) \right]^{1/2}$$

$$P_{in} = V_{sr} \cdot I_{sr} \cdot PF \text{ ----- (i)}$$

$$V_s = V_m \sin \omega t ; V_{sr} = \frac{V_m}{\sqrt{2}}$$

$$I_{sr} = I_{or} = \frac{V_{or}}{R}$$

$$P_{in} = V_{sr} I_{sr} \cos \phi_1 \text{ ----- (ii)}$$

$$P_o = V_o I_o \times$$

i.e. For resistive load take Rms values. i.e.

$$P_o = V_{or} \cdot I_{or}$$

Assuming no losses in the thy.

$$V_{sr} \cdot I_{sr} \cdot PF = V_{or} \cdot I_{or}$$

$$PF = \frac{V_{or}}{V_{sr}} \text{ for R load}$$

$$PF = \frac{1}{\sqrt{2\pi}} \left[(\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right]^{1/2}$$

(1) The supply current contains harmonics on Ac side of the converter.
In general (other than resistive load) Fundamental source current is responsible to deliver useful power on Ac side of the conv.

Fundamental displacement factor (FDF) = $\cos \phi_1$

$$V_{sr} \cdot I_{sr} \cdot PF = V_{sr} \cdot I_{s1} \cos \phi_1$$

$$PF = \frac{I_{s1}}{I_{sr}} \cos \phi_1$$

$$PF = g \cdot \cos \phi_1$$

$$PF = g \cdot FDF$$

Mode(1) $\rightarrow (\alpha \text{ to } \pi)$

$$V_o = V_s$$

* Power Flows from Source to the load

So power is +ve i.e. (P+)

Apply KVL;

$$V_s = V_m \sin \omega t = R i_o + L \frac{di_o}{dt}$$

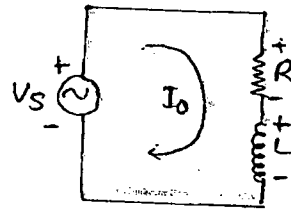
$$i_o = I_{\text{steady}} + I_{\text{transient}} \\ \text{(PI)} \quad \text{(CE)}$$

$$i_o = \frac{V_m}{|Z|} \sin(\omega t - \phi) + K e^{-t/T}$$

$$\text{at } \omega t = \alpha, i_o = 0$$

$$K = \frac{V_m}{|Z|} (e^{t/T})_x \sin(\alpha - \phi)$$

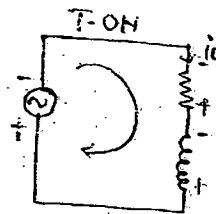
$$K = -\frac{V_m}{|Z|} \sin(\alpha - \phi) e^{\frac{-R\alpha}{\omega L}}$$



Mode(2) $\rightarrow (\pi \text{ to } \beta)$

$$\frac{1}{2} L i^2 \longrightarrow \text{Source } \& I^2 R$$

L is releasing energy



* Here the inductance energy makes the thy. to conduct even in the -ve cycle until it releases its complete energy at $\omega t = \beta$

$$\downarrow PF = \frac{P_o}{V_{sr} I_{sr}}$$

$$\omega t_c = 2\pi - \beta$$

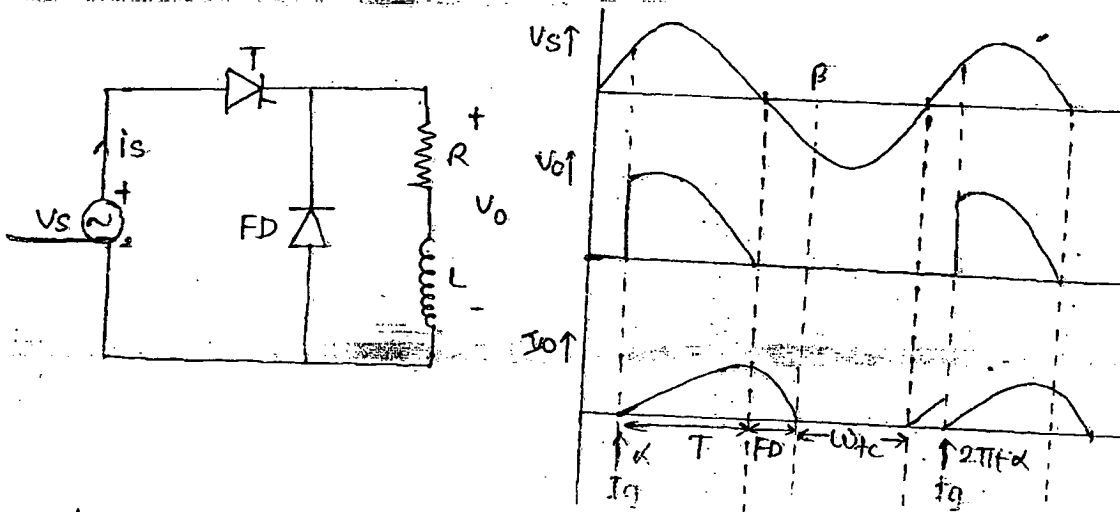
$$t_c = \frac{2\pi - \beta}{\omega} \text{ sec}$$

$$V_o = \frac{1}{2\pi} \int_{\alpha}^{\beta} V_m \sin \omega t (d\omega t)$$

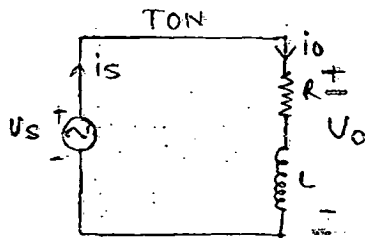
$$V_o = \frac{V_m}{2\pi} (\cos \alpha - \cos \beta)$$

$$V_{or} = \frac{V_m}{2\sqrt{\pi}} \left[(\beta - \alpha) + \frac{1}{2} (\sin 2\alpha - \sin 2\beta) \right]^{1/2}$$

3) 1- ϕ HWR RL load with FD $\rightarrow$

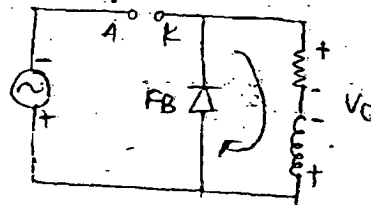


mode (1) $\rightarrow$



source (P) $\rightarrow$ load

mode (2) $\rightarrow$



$$\frac{1}{2} L i^2 \rightarrow I^2 R$$

PF improved, $PF = \frac{P_o}{V_{or} I_{sr}}$

$$V_o = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t (d\omega t)$$

$$V_o = \frac{V_m}{2\pi} (1 + \cos \alpha)$$

$$V_{or} = \frac{V_m}{2\sqrt{\pi}} \left[(\pi - \alpha) + \frac{1}{2} (\sin 2\alpha) \right]^{1/2}$$

$$\omega t_c = \pi \text{ rad}$$

$$t_c = \frac{\pi}{\omega}$$

* -ve power is removed i.e. avg. P_o is increased; so PF is increased.

$$\uparrow PF = \frac{P_o \uparrow}{V_s I_s \uparrow}$$

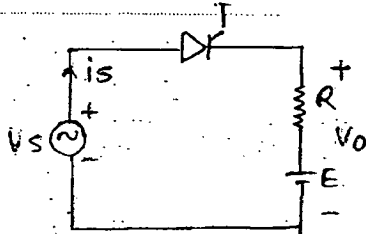
Advantage of FD →

- (1) The PF is improved on Ac side of the conv^r.
 - (2) -ve Voltage spikes in the o/p voltage waveform is removed; thus increased o/p voltage, active power & PF.
 - (3) The shape of the o/p current waveform is improved.
- Hence the performance of the converter is improved with a FD.
- * The PF of the semiconv^r is better than full conv^r due to its freewheeling action.

Therefore the performance of the semiconv^r is superior to full conv^r.

Application →

1- ϕ HWR charging a battery (RE load) →



+ $V_s > E$, T(F)

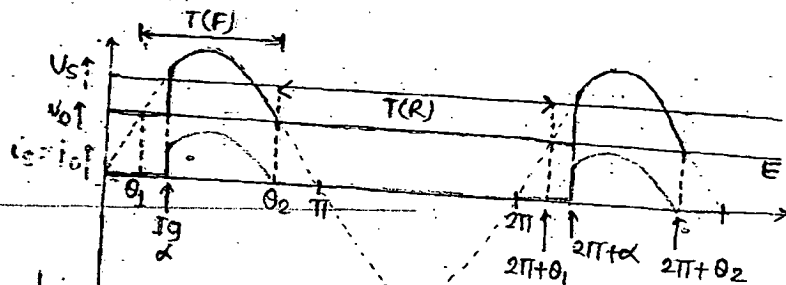
At $\omega t = \theta_1$, $V_s = E$

$$V_m \sin \theta_1 = E$$

$$\theta_1 = \sin^{-1} \left(\frac{E}{V_m} \right)$$

$$\theta_2 = \pi - \theta_1$$

$$\theta_1 \leq \alpha \leq \theta_2$$



T(ON)

$$V_o = V_s$$

$$V_s = R i_o + E$$

$$i_o = \frac{V_s - E}{R}$$

$$i_o = \frac{V_m \sin \omega t - E}{R}$$

T → (OFF)

$$i_o = 0, V_o = E$$

$$\omega t = 2\pi + \theta_1 - \theta_2$$

$$= 2\pi + \theta_1 - \pi + \theta_1$$

$$\omega t_c = \pi + 2\theta_1 \text{ rad.}$$

$$t_c = \frac{\pi + 2\theta_1}{\omega} \text{ sec}$$

* PIV of thyristor = $V_m + E$

$$V_o(\text{avg}) = \frac{1}{2\pi} \left[\int_{\alpha}^{\theta_2} V_m \sin \omega t \, d(\omega t) + \int_{\theta_2}^{2\pi + \alpha} E \, d(\omega t) \right]$$

$$V_o(\text{avg}) = \frac{1}{2\pi} \left[V_m (\cos \alpha - \cos \theta_2) + E (2\pi + \alpha - \theta_2) \right] \text{ Rad.}$$

Charging current of Battery

$$I_o = \frac{1}{2\pi} \int_{\alpha}^{\theta_2} \left(\frac{V_m \sin \omega t - E}{R} \right) d(\omega t)$$

$$I_o = \frac{1}{2\pi R} \left[V_m (\cos \alpha - \cos \theta_2) - E (\theta_2 - \alpha) \right] \text{ Rad.}$$

* When the diode rectifier is charging a battery substitute $\alpha = 0$,
in the above eqⁿ to Find the V_o & I_o

$$P_{in} = V_{sr} I_{sr} \text{PF}$$

$$P_o = I_{or}^2 R + E I_o$$

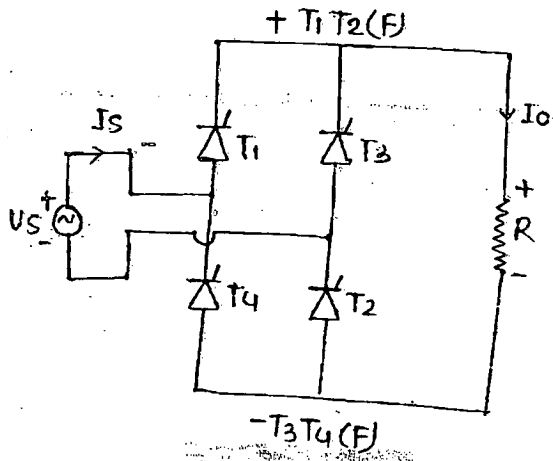
Assuming no losses in thy. i.e. we get:

$$\boxed{\text{PF} = \frac{I_{or}^2 R + E I_o}{V_{sr} I_{sr}}}$$

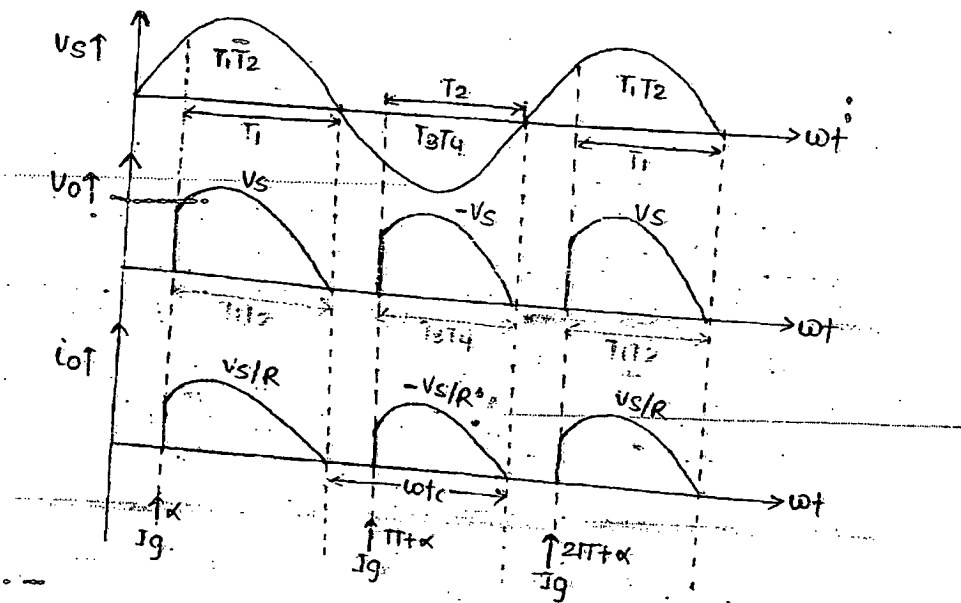
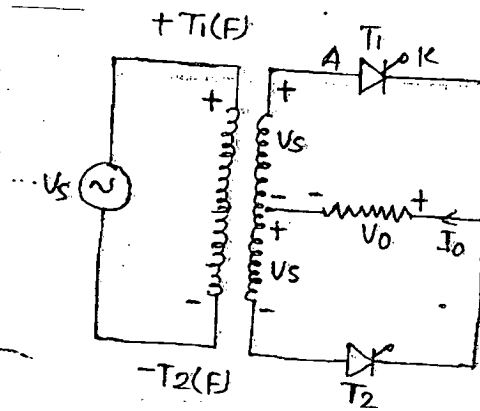
$$I_{or} = \left[\frac{1}{2\pi} \int_{\alpha}^{\theta_2} \left(\frac{V_m \sin \omega t - E}{R} \right)^2 d(\omega t) \right]^{1/2}$$

1- ϕ Full Wave Rectifier $\rightarrow$ (2-pulse converter)

* Bridge Rectifier



* Mid point rectifier



$T_1 T_2 \rightarrow \text{ON}$

i.e. $V_o = V_s$

$$I_o = \frac{V_s}{R}$$

$T_3 T_4 \rightarrow \text{ON}$

i.e. $V_o = -V_s$

$$I_o = \frac{-V_s}{R}$$

$T_1 \rightarrow \text{ON}$

i.e. $V_o = V_s$

$$I_o = \frac{V_s}{R}$$

$T_2 \rightarrow \text{ON}$

$V_o = -V_s$

$$I_o = \frac{-V_s}{R}$$

$$\omega t_c = \pi$$

$$t_c = \frac{\pi}{\omega}$$

$$V_o = \frac{1}{\pi} \int_{\alpha}^{\pi} V_m \sin \omega t d(\omega t)$$

$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$V_{or} = \frac{V_m}{\sqrt{2\pi}} \left[(\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right]^{1/2}$$

For Resistive load; $PF = \frac{V_{or}}{V_{sr}}$

$$= \frac{1}{\sqrt{\pi}} \left[(\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right]^{1/2}$$

* For mid point rectifier $PIV = 2V_m$

; * For bridge rectifier $PIV = V_m$.

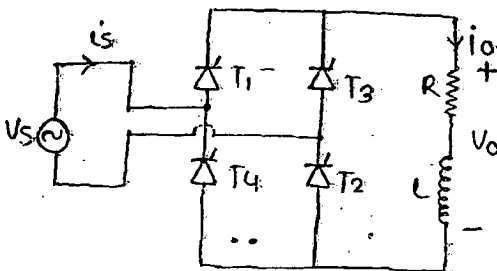
* In mid point rectifier V_m is the peak value of upper 2° voltage.

Advantage of bridge rectifier →

* The PIV of the thy. in bridge rectifier half of that when compared to mid point rectifier.

* If same thy. are used in both the conv^r then the avg. o/p vol. & power handled by bridge rectifier is double that of mid point rectifier.

Bridge Rectifier with RL load → (1 ϕ Fully Controlled rectifier)



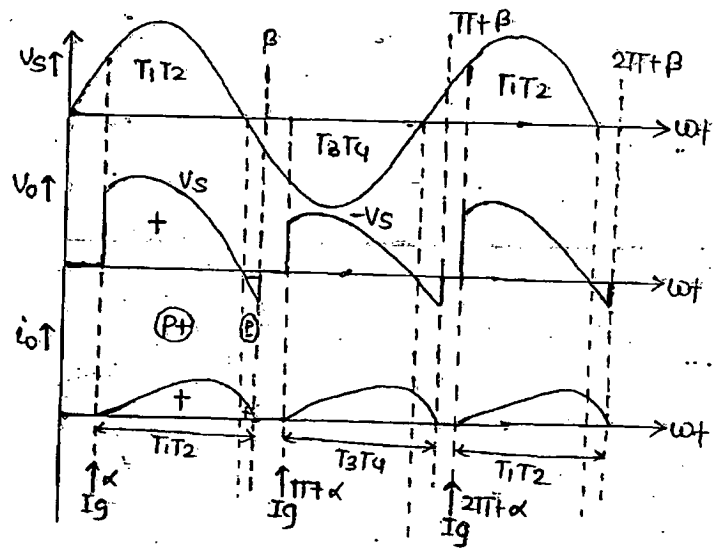
$$\omega t_c = 2\pi - \beta$$

$$t_c = \frac{2\pi - \beta}{\omega}$$

$$V_o = \frac{1}{\pi} \int_{\alpha}^{\beta} V_m \sin \omega t d(\omega t)$$

$$V_o = \frac{V_m}{\pi} (\cos \alpha - \cos \beta)$$

$$V_o = \frac{V_m}{\pi} (\cos \alpha - \cos \beta)$$



$$V_{or} = \frac{V_m}{\sqrt{2\pi}} \left[(\beta - \alpha) + \frac{1}{2} (\sin 2\alpha - \sin 2\beta) \right]^{1/2}$$

We get discontinuous condⁿ $\beta < (\pi + \alpha)$

Reasons $\rightarrow$ (1.) $L \downarrow$ $T \downarrow$ i.e. $\beta \downarrow$

$$\because T = \frac{L}{R}$$

(2.) $\alpha \uparrow$ $\beta \downarrow$

(3.) If avg o/p current is less the β is also less ($I_o \downarrow$ $\beta \downarrow$)

RL Load with Continuous conduction $\rightarrow$

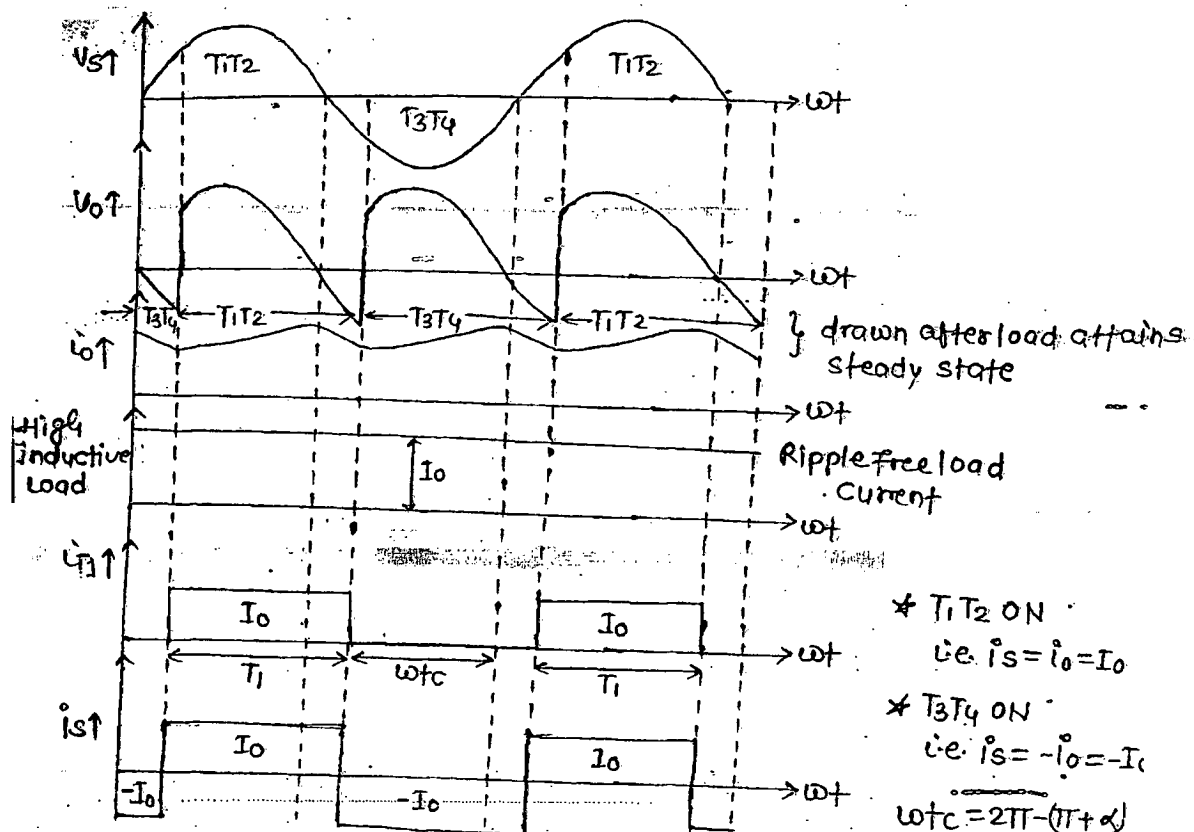
We get continuous condⁿ when $\beta \geq (\pi + \alpha)$

Reasons $\rightarrow$ (1.) $L \uparrow$ $T \uparrow$ i.e. $\beta \uparrow$

$$T = \frac{L}{R}$$

(2.) $\alpha \downarrow$ $\beta \uparrow$

(3.) $I_o \uparrow$ $\beta \uparrow$



$$V_o = \frac{1}{\pi} \int_{\alpha}^{\pi+\alpha} v_m \sin \omega t d\omega t$$

$$V_o = \frac{2V_m}{\pi} \cos \alpha$$

$$V_{or} = \frac{V_m}{\sqrt{2\pi}} \left[\pi + \frac{1}{2} (\sin 2\alpha - \sin 2\alpha) \right]^{1/2}$$

$$V_{or} = \frac{V_m}{\sqrt{2}} = V_{sr}$$

$$I_{sr} = I_o$$

Assume high inductive load $\rightarrow$

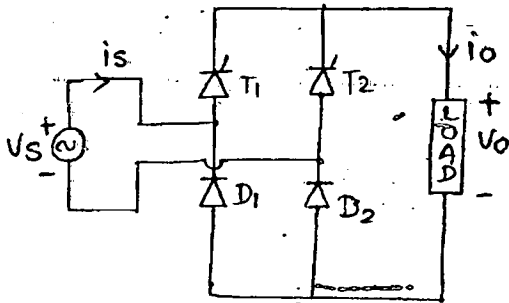
(1) Conduction angle of each thy. = π rad for every cycle. $\{(\pi + \alpha) - \alpha\}$

(2) Avg. thy. current $(I_T)_{avg} = \frac{I_o \pi}{2\pi} = \frac{I_o}{2}$

$$(I_T)_{rms} = I_o \left(\frac{\pi}{2\pi} \right)^{1/2} = \frac{I_o}{\sqrt{2}}$$

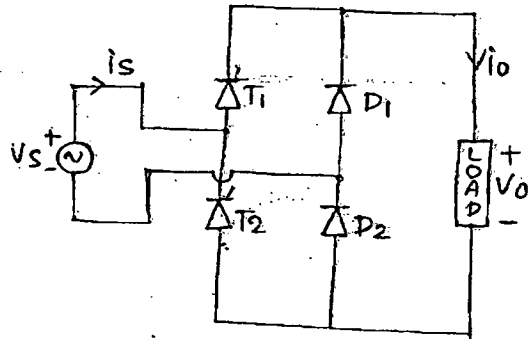
1- ϕ Half Controlled Rectifier $\rightarrow$

Symmetrical Connection



$+T_1 D_2 (F)$
 $-T_2 D_1 (F)$

Asymmetrical Connection

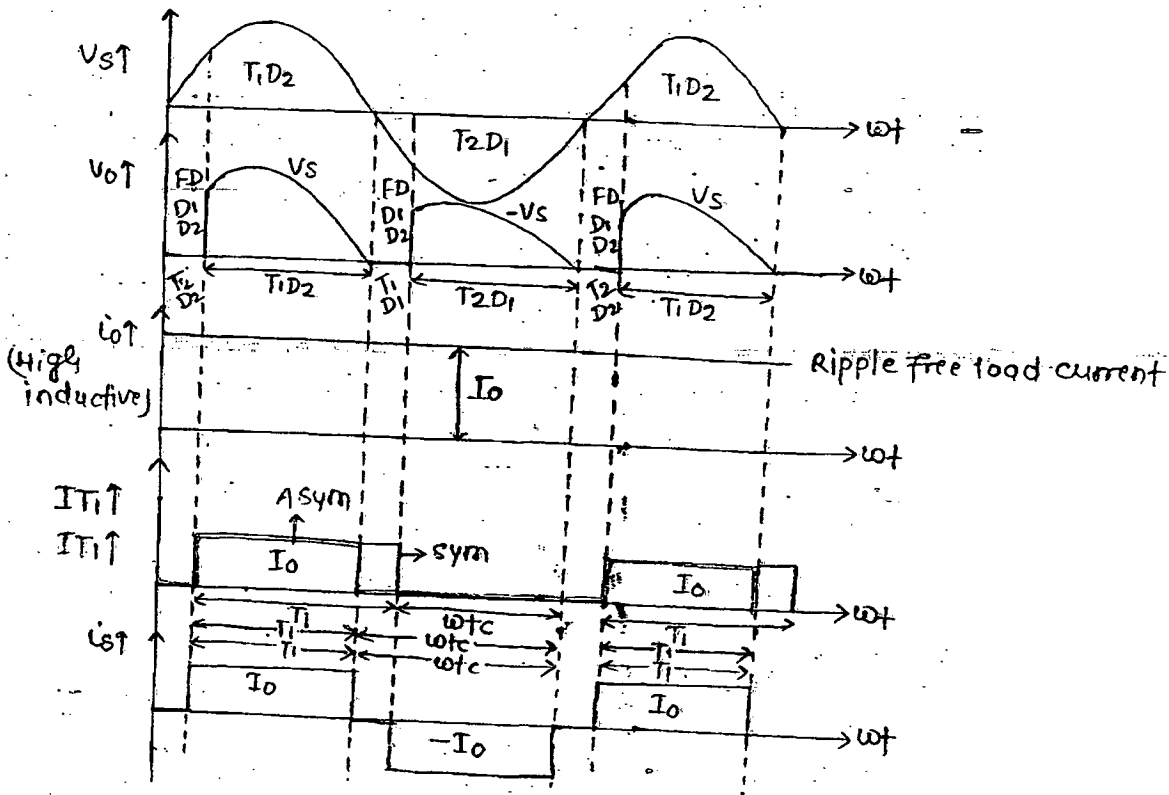


$+T_1 D_2 (F)$
 $-T_2 D_1 (F)$

* During FD period the -ve spikes are removed & the source current also becomes zero.

* For resistive load waveforms are same in full con^r & semicon^r.

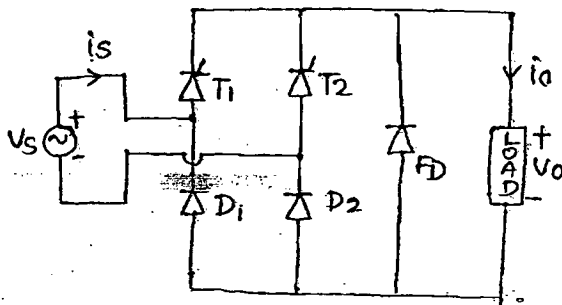
** Let us assume high inductive load.



Que → What is the problem with sym. connection?

Ans → * At $\alpha, \pi + \alpha, 2\pi + \alpha$ ----- There is a possibility of short circuit across the supply when incoming thy starts conducting before the o/p (outgoing) thy stops conducting.

* To rectify this problem we must connect a separate FD across the load as shown in the fig. given below:-



$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$V_{or} = \frac{V_m}{\sqrt{2\pi}} \left[(\pi - \alpha) + \frac{1}{2} \sin 2\alpha \right]^{1/2}$$

* In the semiconverter :-

(1) Condⁿ angle of each thy. = $\pi - \alpha$ (for every 2π rad)

(2) Avg. thy. current $(I_T)_{avg} = I_o \left(\frac{\pi - \alpha}{2\pi} \right)$

$$(I_T)_{rms} = I_o \left(\frac{\pi - \alpha}{2\pi} \right)^{1/2}$$

(3) Condⁿ angle of FD is α rad. (for every π rad)

(4) Avg. FD current $(I_{FD})_{avg} = I_o \left(\frac{\alpha}{\pi} \right)$

$$(I_{FD})_{rms} = I_o \left(\frac{\alpha}{\pi} \right)^{1/2}$$

$$I_{sr} = I_o \left(\frac{\pi - \alpha}{\pi} \right)^{1/2} \quad \left\{ \begin{array}{l} \text{If you have any symm. -ve wave} \\ \text{form we cal. for } \pi \text{ rads} \end{array} \right.$$

Ratings of Thyristor →

(1) Thyristor RMS Rating $(I_T)_{RMS} \rightarrow$

- * It gives the RMS value Rating of ON state current of thy.
- * $(I_T)_{RMS}$ value in con^r should be less than thy. RMS Rating.

(2) Average thy. Rating $(I_T)_{avg} \rightarrow$

- * It gives the avg. rating of ON state current of a thy.

$$(I_T)_{avg} = \frac{(I_T)_{RMS \text{ Rating}}}{FF}$$

FF → It is a FF of thy. current waveform in a con^r.

Avg. Rating of thy. depends on :-

- (1) Condⁿ angle of thy. $\uparrow$ FF $\downarrow \Rightarrow (I_T)_{avg} \uparrow$
 - (2) Avg. Rating depends on type of the load.
- eg. $\rightarrow L \uparrow \frac{di}{dt} \downarrow$ smoothness $\uparrow \therefore$ FF $\downarrow \Rightarrow (I_T)_{avg} \uparrow$

(3) I_t^2 Rating → This Rating is provided for the thy. to select a proper fuse for over current protection.

* I_t^2 rating of thy. should always greater than fuse.

(4) Surge Current Rating → Surge Current Rating is specified for short duration of time.

n cycle surge current Rating (I_{sn}) → It is the surge current that the SCR can withstand for n cycle.

$$I_{sn}^2 \left(\frac{nT}{2} \right) = I_t^2 \text{ Rating of thy.}$$

From above we can find I_{sn}

One cycle surge current Rating (I_{s1}) → It is the surge current that the SCR can withstand for 1 cycle

$$I_{S1}^2 \left(\frac{T}{2} \right) = I_{Sn}^2 \cdot n \cdot \frac{T}{2}$$

$$I_{S1} = \sqrt{n} I_{Sn}$$

Sub cycle Current Rating ($I_{S/n}$) → It is the surge current that the SCR can with stand for

$\frac{1}{n}$ th period of a cycle.

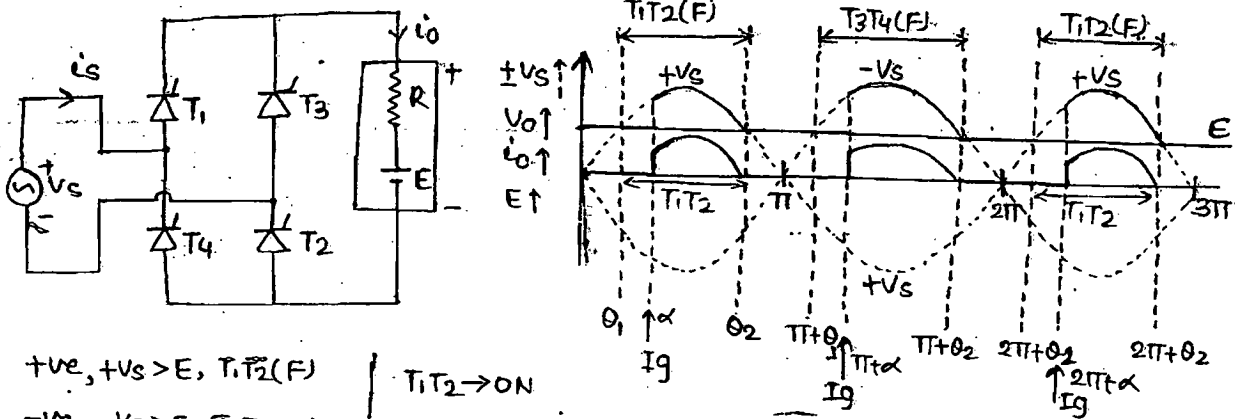
$$(I_{S/n})^2 \cdot \left(\frac{1}{n} \right) \frac{T}{2} = (I_{S1})^2 \frac{T}{2}$$

$$(I_{S/n}) = \sqrt{n} I_{S1}$$

Half cycle surge current Rating

$$(I_{S/2}) = \sqrt{2} I_{S1}$$

1) 1 ϕ Full Converter - Charging Battery $\rightarrow$



$$+V_s, +V_s > E, T_1T_2(F)$$

$$-V_s, -V_s > E, T_3T_4(F)$$

$$\theta_1 = \sin^{-1}\left(\frac{E}{V_m}\right), \theta_2 = \pi - \theta_1$$

$$\theta_1 \leq \alpha \leq \theta_2$$

$$T_1T_2 \rightarrow ON$$

$$V_o = V_s$$

$$I_o = \frac{V_s - E}{R}$$

$$I_o = \frac{V_m \sin \omega t - E}{R}$$

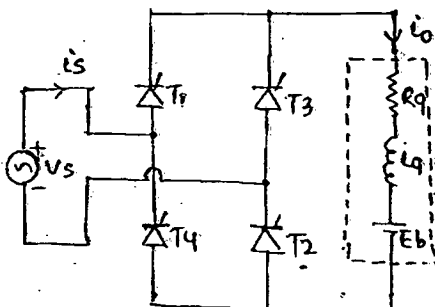
$$V_o = \frac{1}{\pi} \left[\int_{\alpha}^{\theta_2} V_m \sin \omega t d(\omega t) + \int_{\theta_2}^{\pi + \alpha} E d(\omega t) \right]$$

$$V_o = \frac{1}{\pi} \left[V_m (\cos \alpha - \cos \theta_2) + E (\pi + \alpha - \theta_2) \right]$$

$$I_o = \frac{1}{\pi} \left[\int_{\alpha}^{\theta_2} \frac{V_m \sin \omega t - E}{R} d(\omega t) \right]$$

$$I_o = \frac{1}{\pi R} \left[V_m (\cos \alpha - \cos \theta_2) - E (\theta_2 - \alpha) \right]$$

1 ϕ Full Converter - DC Motor (RLE load) $\rightarrow$



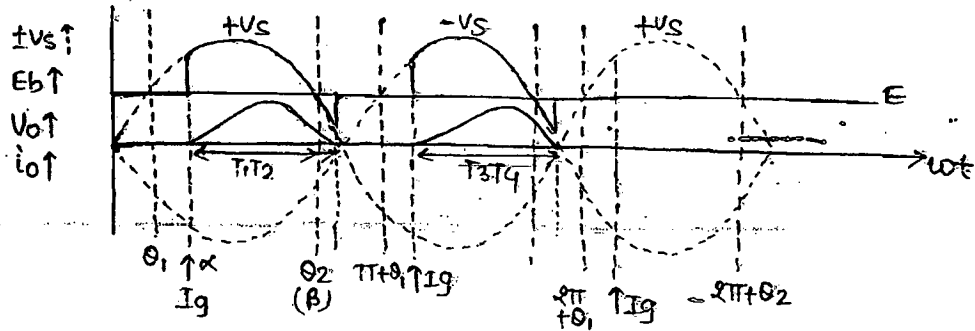
(1) Discontinuous Conduction

$$\theta_2 < \beta < (\pi + \alpha)$$

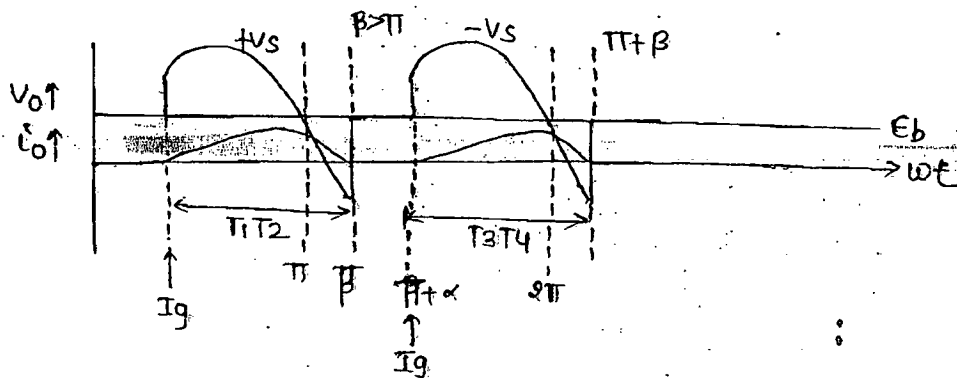
$$(a) \beta < \pi$$

$$(b) \beta \geq \pi$$

(i) $\beta < \pi$



(ii) $\beta > \pi$



$$t_c = \frac{2\pi + \theta_1 - \beta}{\omega}$$

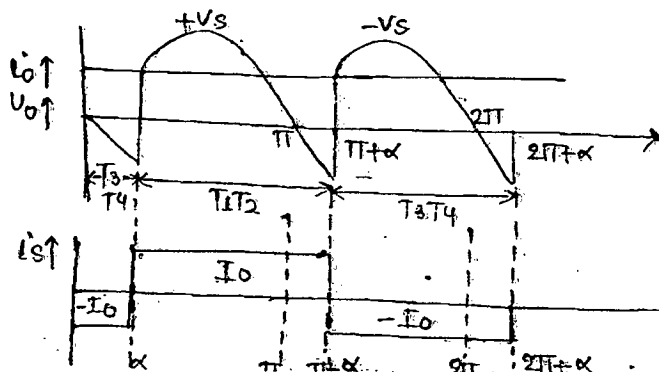
$$V_o = \frac{1}{\pi} \left[\int_{\alpha}^{\beta} V_m \sin \omega t d(\omega t) + \int_{\beta}^{\pi + \alpha} E_b d(\omega t) \right]$$

$$V_o = \frac{1}{\pi} \left[V_m (\cos \alpha - \cos \beta) + E_b (\pi + \alpha - \beta) \right]$$

(2) Continuous Conduction $\rightarrow$

$$\beta > (\pi + \alpha)$$

* For continuous condⁿ there is no effect of back emf in the o/p vol waveform therefore the o/p vol. waveform will remain same for RL & RLE load.



$$\boxed{U_0 = \frac{2V_m}{\pi} \cos \alpha \rightarrow RL, RLE}$$

$$I_{sr} = I_0$$

$$I_{sr} = I_0 \left(\frac{\pi + \alpha - \alpha}{\pi} \right)^{1/2}$$

$$I_{sr} = I_0$$

Harmonic analysis on AC side of converter $\rightarrow$

The Fourier series for supply waveform is

$$i_s = \sum_{n=1,3,5}^{\infty} \frac{4I_0}{n\pi} \sin(n\omega t + \phi_n)$$

where $\phi_n = -n\alpha$, $\phi_1 = -\alpha$

$$i_{sn} = \frac{4I_0}{n\pi} \sin(n\omega t + \phi_n)$$

$$\boxed{\begin{array}{l} i = \text{instantaneous} \\ I = \text{RMS} \end{array}}$$

$$I_{sn} = \frac{2\sqrt{2}}{n\pi} I_0$$

$$\boxed{I_{s1} = \frac{2\sqrt{2}}{\pi} I_0} \text{----- (i)}$$

$$FDF = \cos \phi_1$$

$$\boxed{FDF = \cos \alpha} \text{----- (ii)}$$

$$g = \frac{I_{s1}}{I_{sr}}$$

$$= \frac{\frac{2\sqrt{2}}{\pi} I_0}{I_0}$$

$$\boxed{g = \frac{2\sqrt{2}}{\pi}} \text{----- (iii)}$$

$$PF = g \cdot FDF$$

$$\boxed{PF = \frac{2\sqrt{2}}{\pi} \cos \alpha} \text{----- (iv)}$$

$$THD = \left(\frac{1}{g^2} - 1 \right)^{1/2}$$

$$= \left(\frac{\pi^2}{8} - 1 \right)^{1/2}$$

$$= 0.4834$$

$$\boxed{THD = 48.34\%} \text{----- (v)}$$

Active power $P = V_{sr} I_{s1} \cos \alpha$
(Useful power)

$$P = \frac{V_m}{\sqrt{2}} \frac{2\sqrt{2}}{\pi} I_0 \cos \alpha$$

$$P = \frac{2V_m}{\pi} I_0 \cos \alpha$$

$$\boxed{P = V_0 I_0} \quad \text{--- (vi) where; } V_0 = \frac{2V_m}{\pi} \cos \alpha$$

Reactive power

$$Q = V_{sr} I_{s1} \sin \alpha \quad (\text{lag}) \rightarrow [\sin(-\alpha) = -\sin \alpha]$$

$$= V_{sr} I_{s1} \cos \alpha \frac{\sin \alpha}{\cos \alpha}$$

$$Q = P \tan \alpha$$

$$\boxed{Q = P \tan \alpha = V_0 I_0 \tan \alpha} \quad \text{--- (vii)}$$

Harmonics analysis on dc side of converter $\rightarrow$

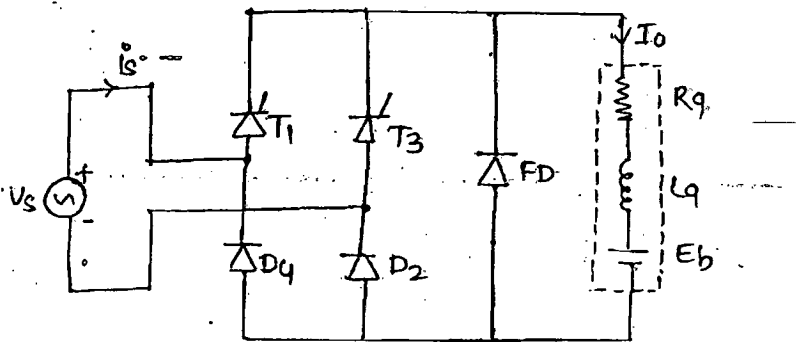
$$FF = \frac{V_{or}}{V_0} = \frac{V_m/\sqrt{2}}{\frac{2V_m}{\pi} \cos \alpha}$$

$$\boxed{FF = \frac{\pi}{2\sqrt{2} \cos \alpha}}$$

$$URF = \sqrt{FF^2 - 1}$$

$$\boxed{URF = \sqrt{\frac{\pi^2}{8 \cos^2 \alpha} - 1}}$$

1 ϕ Semi Converter $\rightarrow$



(i) Discontinuous conduction:-

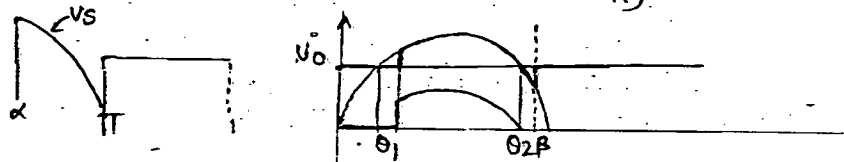
$$\theta_2 < \beta < (\pi + \alpha)$$

(a) $\beta < \pi$

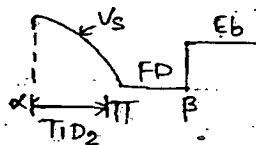
(b) $\beta > \pi$

(a) $\beta < \pi \rightarrow$ * In this condition FD will not conduct (Because FD conduct after π rad. i.e. due to inductor the -ve spikes come after π)

$$V_o = \frac{1}{\pi} \left[V_m (\cos \alpha - \cos \beta) + E_b (\pi + \alpha - \beta) \right]$$



(b) $\beta > \pi \rightarrow$ * In this condⁿ FD will conduct from π to β

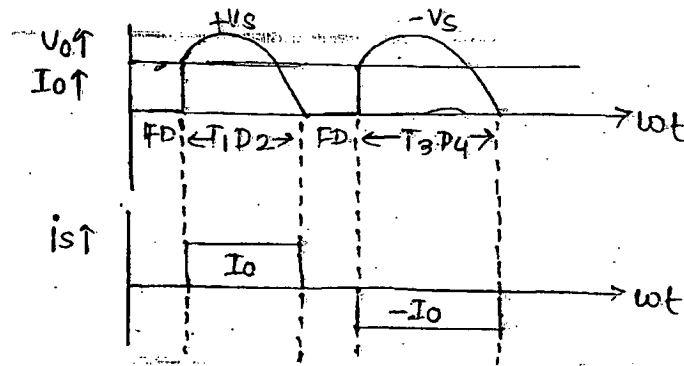


$$V_o = \frac{1}{\pi} \left[\int_{\alpha}^{\pi} V_m \sin \omega t d(\omega t) + \underbrace{\int_{\pi}^{\beta} 0 d\omega t}_{FWR} + \int_{\beta}^{\pi + \alpha} E_b d(\omega t) \right]$$

discontinuous

$$V_o = \frac{1}{\pi} \left[V_m (1 + \cos \alpha) + E_b (\pi + \alpha - \beta) \right]$$

Continuous Conduction $\rightarrow$ For this condⁿ there is no effect of back emf for o/p vol. waveform. Therefore the o/p vol. waveform will remain same for RL & RLE load.



$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$I_{sr} = I_o \left(\frac{\pi - \alpha}{\pi} \right)^{1/2}$$

Harmonic Analysis on AC side of Con^r

The Fourier series for the supply current

$$i_s = \sum_{n=1,3,5,\dots}^{\infty} \frac{4I_o}{n\pi} \cos \frac{n\alpha}{2} \sin(n\omega t + \phi_n)$$

where $\phi_n = -\frac{n\alpha}{2}$, $\phi_1 = -\frac{\alpha}{2}$

$$i_{sn} = \frac{4I_o}{n\pi} \cos \frac{n\alpha}{2} \sin(n\omega t + \phi_n)$$

$$I_{sn} = \frac{2\sqrt{2}}{n\pi} I_o \cos \frac{n\alpha}{2}$$

$$I_{s1} = \frac{2\sqrt{2}}{\pi} I_o \cos \frac{\alpha}{2} \quad \text{--- (i)}$$

$$FDF = \cos \frac{\alpha}{2} \quad \text{--- (ii)}$$

$$g = \frac{I_{s1}}{I_{sr}} = \frac{\frac{2\sqrt{2}}{\pi} I_o \cos \frac{\alpha}{2}}{I_o \left(\frac{\pi - \alpha}{\pi} \right)^{1/2}}$$

$$g = \frac{2\sqrt{2} \cos \alpha/2}{\sqrt{\pi(\pi - \alpha)}} \quad \text{--- (ii)}$$

$$PF = g \cdot PDF$$

$$= \frac{2\sqrt{2} \cos \alpha/2}{\sqrt{\pi(\pi - \alpha)}} \cos \alpha/2$$

$$= \frac{2\sqrt{2} \cos^2 \alpha/2}{\sqrt{\pi(\pi - \alpha)}}$$

$$PF = \frac{2\sqrt{2}(1 + \cos \alpha)}{\sqrt{\pi(\pi - \alpha)}} \quad \text{--- (iv)}$$

$$THD = \left(\frac{1}{g^2} - 1 \right)^{1/2}$$

$$THD = \left[\frac{\pi(\pi - \alpha)}{8 \cos^2 \alpha/2} - 1 \right]^{1/2} \quad \text{--- (v)}$$

Active Power

$$P = V_{sr} \cdot I_{s1} \cos \alpha/2$$

$$= \frac{V_m}{\sqrt{2}} \cdot \frac{2\sqrt{2}}{\pi} I_0 \cos \frac{\alpha}{2} \cdot \cos \frac{\alpha}{2}$$

$$= \frac{V_m}{\pi} (1 + \cos \alpha) \cdot I_0$$

$$= V_0 I_0$$

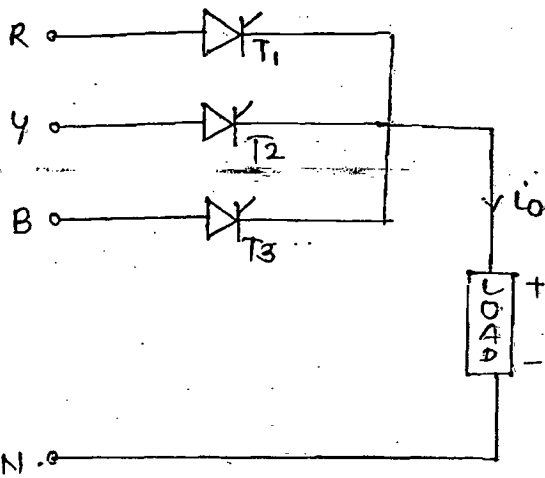
$$P = V_{sr} \cdot I_{s1} \cos \alpha/2 = V_0 I_0 \quad \text{--- (vi)}$$

Reactive Power

$$Q = V_{sr} \cdot I_{s1} \sin \alpha/2$$

$$Q = P \tan \alpha/2 \quad \text{--- (vii)}$$

3 Phase Converter

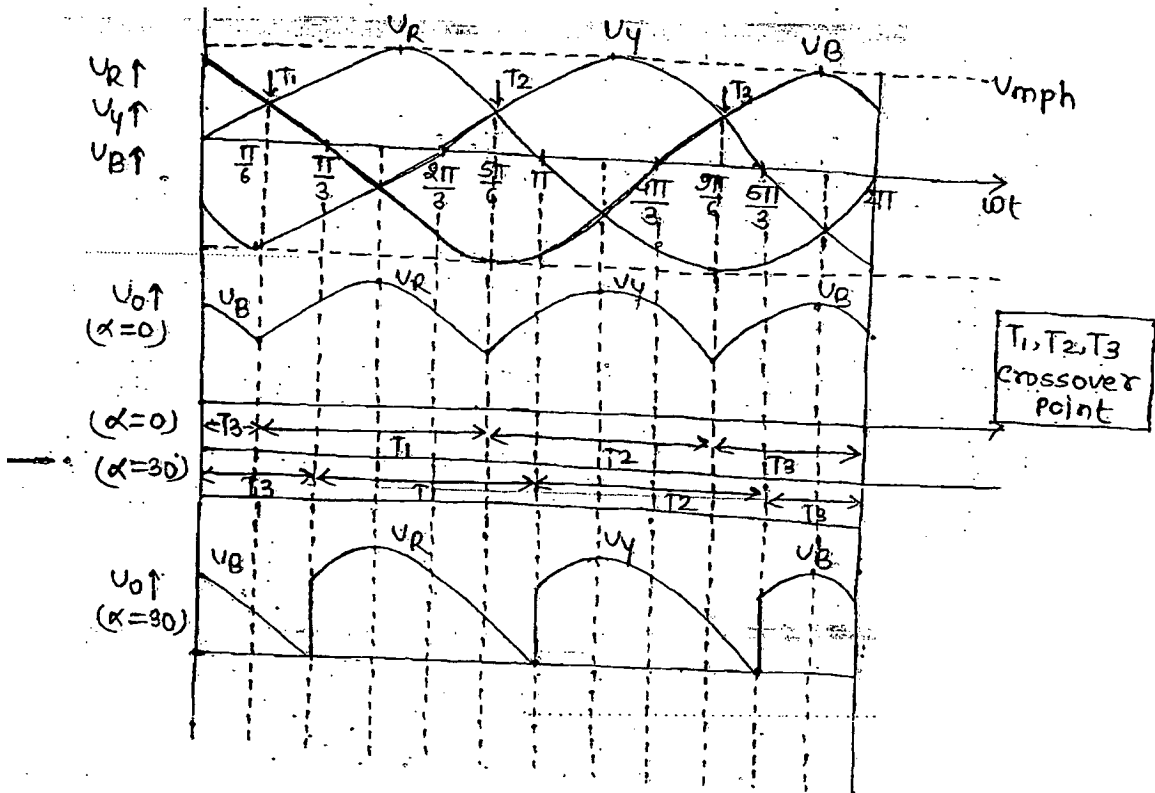


Phase Seq. $\rightarrow$ RYB

$$V_B = V_{mph} \sin(\omega t - 240^\circ)$$

$$V_R = V_{mph} \sin \omega t$$

$$V_Y = V_{mph} \sin(\omega t - 120^\circ)$$



(1.) $\alpha \leq 30^\circ$ Continuous Condⁿ for R load $\rightarrow$

$$V_o = \frac{1}{2\pi/3} \int_{\pi/6 + \alpha}^{\pi/6 + \alpha + 2\pi/3} V_{mph} \sin \omega t d(\omega t)$$

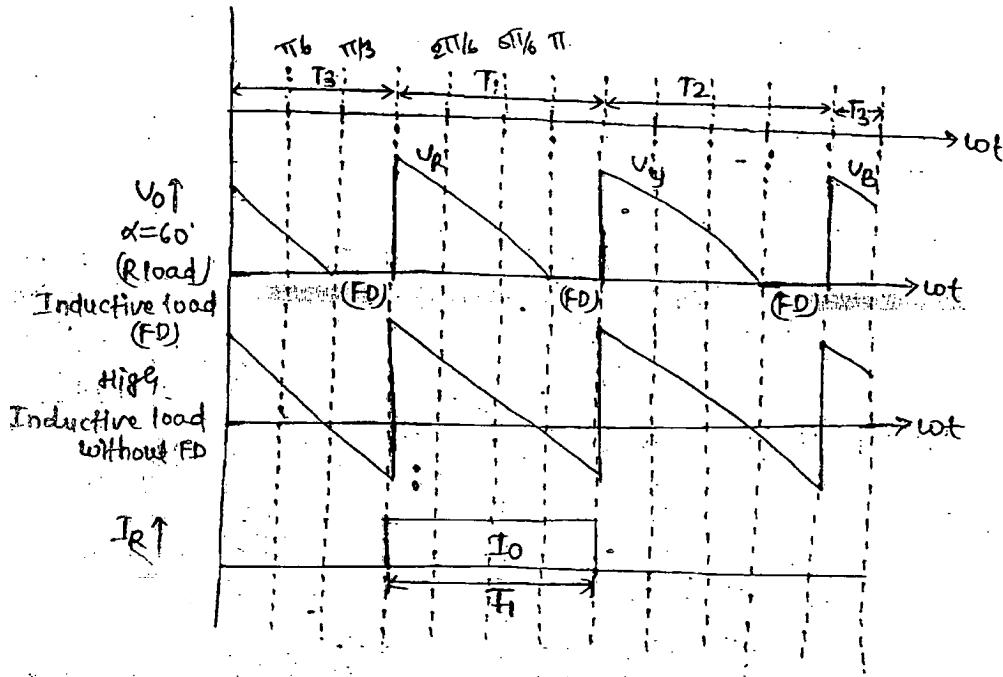
$$V_o = \frac{3\sqrt{3}}{2\pi} V_{mph} \cos \alpha$$

$$V_o = \frac{3V_{ml}}{2\pi} \cos \alpha$$

$R(\alpha \leq 30^\circ)$ $R, RLE(\alpha > 30^\circ)$
(Continuous)

$$V_{or} = \left[\frac{1}{(2\pi/3)} \int_{\pi/6+\alpha}^{\pi/6+\pi} V_{mph}^2 \sin^2 \omega t d(\omega t) \right]^{1/2}$$

$$V_{or} = \frac{V_{mL}}{\sqrt{3}} \left[\frac{1}{6} + \frac{\sqrt{3}}{8\pi} \cos 2\alpha \right]^{1/2}$$



(2.) $\alpha > 30^\circ$: discontinuous conduction for R load:-

$$V_o = \frac{1}{(2\pi/3)} \int_{\pi/6+\alpha}^{\pi/6+\pi} V_{mph} \sin \omega t d(\omega t)$$

$$V_o = \frac{3V_{mph}}{2\pi} \left[1 + \cos\left(\frac{\pi}{6} + \alpha\right) \right] \quad \begin{matrix} R (\alpha > 30^\circ) \\ R, RLE (with FD \alpha > 30^\circ) \end{matrix}$$

$$V_{or} = \left[\frac{1}{(2\pi/3)} \int_{\pi/6+\alpha}^{\pi/6+\pi} V_{mph}^2 \sin^2 \omega t d(\omega t) \right]^{1/2}$$

$$V_{or} = \frac{V_{mL}}{\sqrt{3}} \left[\left(\frac{5\pi}{6} - \alpha \right) + \frac{1}{2} \sin\left(\frac{\pi}{3} + 2\alpha\right) \right]^{1/2}$$

Assume high inductive load with FD:-

(1) $\alpha \leq 30^\circ$:- FD will not conduct

Conduction angle of each thy. is $\frac{2\pi}{3}$ rad [For every $\frac{2\pi}{3}$ rad]

$$(I_T = I_{ph} = I_L)_{avg} = I_0 \left[\frac{\frac{2\pi/3}{2\pi}} \right]$$

$$= \frac{I_0}{3}$$

$$(I_T = I_{ph} = I_L)_{rms} = \frac{I_0}{\sqrt{3}}$$

(2) $\alpha > 30^\circ \rightarrow$ Conduction angle of FD = $(\alpha - \frac{\pi}{6})$ [For every $\frac{2\pi}{3}$ rad]

Conduction angle of each thy. is $(\frac{5\pi}{6} - \alpha)$ [For every $\frac{2\pi}{3}$ rad]

$$(I_T = I_{ph} = I_L)_{avg} = \frac{I_0 \left[\frac{\frac{5\pi}{6} - \alpha}{2\pi} \right]}{\frac{2\pi/3}{2\pi}}$$

$$(I_T = I_{ph} = I_L)_{rms} = I_0 \left[\frac{\frac{5\pi}{6} - \alpha}{\frac{2\pi}{3}} \right]^{1/2}$$

$(I_{FD})_{avg} = I_0 \left(\frac{\alpha - \pi/6}{2\pi/3} \right)$	$(I_{FD})_{rms} = I_0 \left(\frac{\alpha - \pi/6}{2\pi/3} \right)^{1/2}$
---	---

Assume high inductive load without FD:-

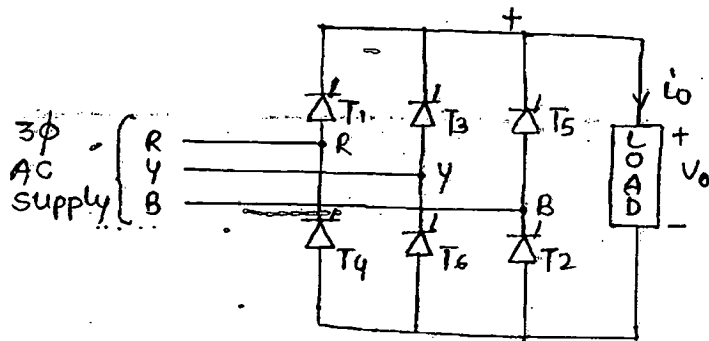
For any value of α

Conduction angle of each thy = $\frac{2\pi}{3}$ rad [For every $\frac{2\pi}{3}$ rad]

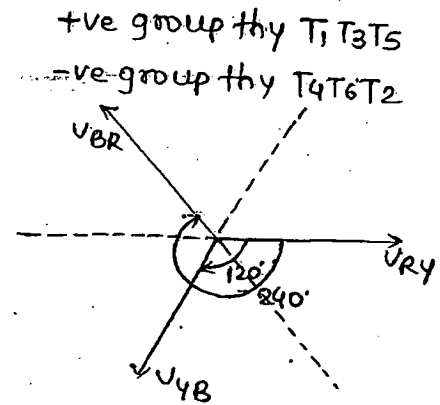
$$(I_T = I_{ph} = I_L)_{avg} = I_0 \left(\frac{2\pi/3}{2\pi} \right) = \frac{I_0}{3}$$

Drawback $\rightarrow$ The source current contains dc component & saturates the supply Xmer core.

3-Phase Fully Controlled Rectifier :- (6 pulse Converter) →



For 6 pulse → Line vol.
3 pulse → Phase vol.



(1) $\alpha \leq 60^\circ$:- Continuous Conduction for R load →

$$V_o = \frac{1}{\pi/3} \int_{\pi/3 + \alpha}^{2\pi/3 + \alpha} V_{mL} \sin \omega t d(\omega t)$$

$$V_o = \frac{3V_{mL} \cos \alpha}{\pi} \rightarrow R (\alpha \leq 60^\circ)$$

→ RL, RLE (Any α) (Continuous)

$$V_{or} = \left[\frac{1}{\pi/3} \int_{\pi/3 + \alpha}^{2\pi/3 + \alpha} V_{mL}^2 \sin^2 \omega t d(\omega t) \right]^{1/2}$$

$$V_{or} = \frac{V_{mL}}{\sqrt{3}} \left[\frac{\pi}{3} + \frac{1}{2} \left\{ \sin \left(\frac{2\pi}{3} + 2\alpha \right) - \sin \left(\frac{4\pi}{3} + 2\alpha \right) \right\} \right]^{1/2}$$

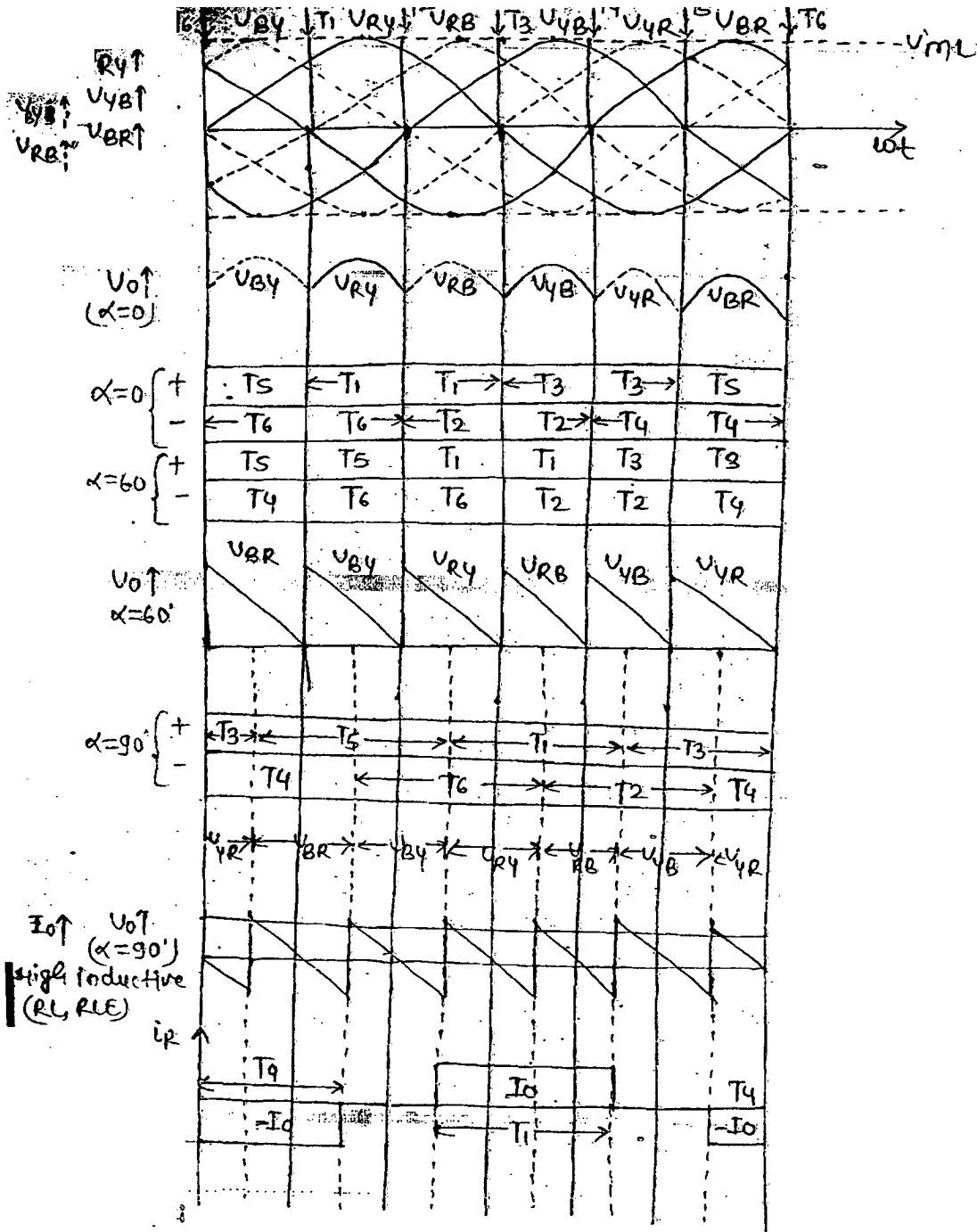
(2) $\alpha > 60^\circ$:- Discontinuous Conduction for R load →

$$V_o = \frac{1}{\pi/3} \int_{\pi/3 + \alpha}^{\pi} V_{mL} \sin \omega t d(\omega t)$$

$$V_o = \frac{3V_{mL}}{\pi} \left[1 + \cos \left(\frac{\pi}{3} + \alpha \right) \right] R (\alpha > 60^\circ)$$

$$V_{or} = \left[\frac{1}{\pi/3} \int_{\pi/3 + \alpha}^{\pi} V_{mL}^2 \sin^2 \omega t d(\omega t) \right]^{1/2}$$

$$V_{or} = \sqrt{\frac{3}{2\pi}} V_{mL} \left[\left(\frac{2\pi}{3} - \alpha \right) + \frac{1}{2} \sin \left(\frac{2\pi}{3} + 2\alpha \right) \right]^{1/2}$$



Assume High inductive load $\rightarrow$

Conduction of angle of each thy. = $\frac{2\pi}{3}$ rad. (for every 2π rad)

$$(I_T)_{avg} = I_o \left(\frac{2\pi/3}{2\pi} \right) = \frac{I_o}{3}$$

$$(I_T)_{rms} = \frac{I_o}{\sqrt{3}}$$

$$I_{sr} = I_o \left(\frac{2\pi/3}{\pi} \right)^{1/2} = \sqrt{\frac{2}{3}} I_o$$

Harmonic analysis on AC side of Converter →

$$i_s = \sum_{n=1,3,5,\dots}^{\infty} \frac{4I_0}{n\pi} \sin \frac{n\pi}{3} \cdot \sin(n\omega t + \phi_n)$$

$$n = 6k \pm 1$$

$$n = 1, 5, 7, 11, 13, \dots$$

$$\phi_n = -n\alpha, \phi_1 = -\alpha$$

Note:- Even & tripple harmonics are not present in the waveform

$$i_{sn} = \frac{4I_0}{n\pi} \sin \frac{n\pi}{3} \cdot \sin(n\omega t + \phi_n)$$

$$I_{sn} = \frac{4I_0}{n\pi\sqrt{2}} \sin \frac{n\pi}{3} = \frac{2\sqrt{2}}{n\pi} I_0 \sin \frac{n\pi}{3}$$

$$I_{s1} = \frac{2\sqrt{2}}{\pi} I_0 \sin \frac{\pi}{3}$$

$$I_{s1} = \frac{\sqrt{6}}{\pi} I_0 \quad \text{----- (i)}$$

$$FDF = \cos \alpha \quad \text{----- (ii)}$$

$$I_{sr} = \sqrt{\frac{2}{3}} I_0$$

$$g = \frac{I_{s1}}{I_{sr}} = \frac{\frac{\sqrt{6}}{\pi} I_0}{\sqrt{\frac{2}{3}} I_0}$$

$$g = \frac{3}{\pi} \quad \text{----- (iii)}$$

$$PF = g \cdot FDF$$

$$= \frac{3}{\pi} \cos \alpha$$

$$PF = \frac{3}{\pi} \cos \alpha \quad \text{----- (iv)}$$

$$THD = \left(\frac{1}{g^2} - 1 \right)^{1/2} = \left(\frac{\pi^2}{9} - 1 \right)^{1/2}$$

$$THD = 0.31$$

$$THD = 31\% \quad \text{----- (v)}$$

$$\begin{array}{l} m \uparrow, \theta \uparrow, THD \downarrow \\ m \uparrow, g \uparrow, PF \downarrow \end{array}$$

Active power $\rightarrow$

$$P = \sqrt{3} V_{sr} I_{s1} \cos \alpha$$

$$= \sqrt{3} \times \frac{V_{m1}}{\sqrt{2}} \times \frac{\sqrt{6} I_0}{\pi} \cos \alpha$$

$$= \sqrt{3} \times \frac{V_{m1}}{\sqrt{2}} \times \frac{\sqrt{2} \sqrt{3}}{\pi} I_0 \cos \alpha$$

$$= \frac{3 V_{m1} \cos \alpha \cdot I_0}{\pi}$$

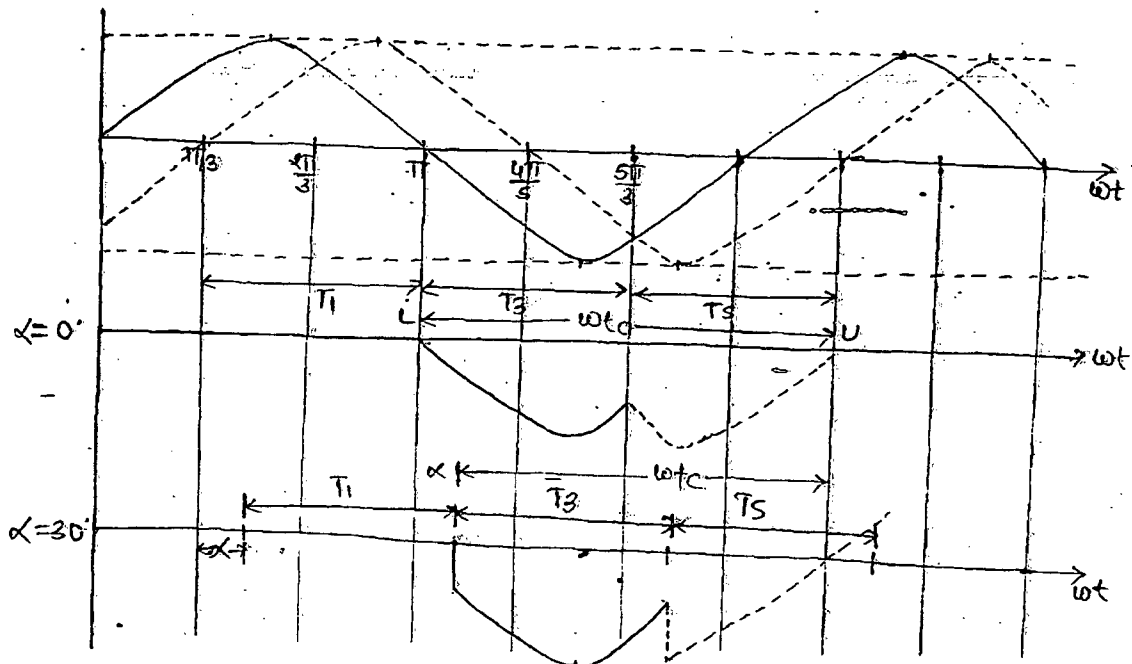
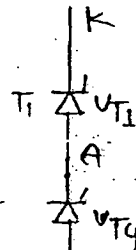
$$P = \frac{3 V_{m1}}{\pi} \cos \alpha \cdot I_0 = V_0 I_0 \quad \text{--- (vi)}$$

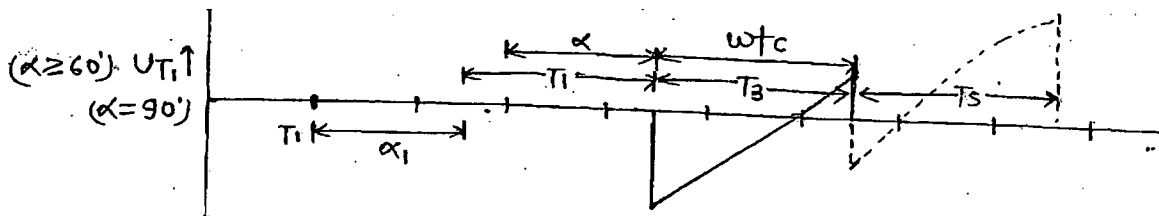
Reactive power $\rightarrow$

$$Q = \sqrt{3} V_{sr} I_{s1} \sin \alpha$$

$$Q = P \tan \alpha \quad \text{--- (vii)}$$

$$\begin{aligned} V_{AK} &\rightarrow (V_{T1}) \\ T_1 &\rightarrow \text{ON}, V_{T1} = 0 \\ T_3 &\rightarrow \text{ON}, V_{T1} = V_{RY} \\ T_5 &\rightarrow \text{ON}, V_{T1} = V_{RB} \end{aligned}$$





$$\alpha = 0^\circ \dots$$

$$\omega t_c = \frac{4\pi}{3}$$

$$t_c = \frac{4\pi}{3\omega} \text{ sec}$$

$$\boxed{\text{PIV} = V_{m2}}$$

$$\alpha < 60^\circ$$

$$\alpha + \omega t_c = \frac{4\pi}{3}$$

$$\omega t_c = \frac{4\pi}{3} - \alpha$$

$$\boxed{t_c = \frac{4\pi - \alpha}{3\omega}}$$

$$\alpha > 60^\circ$$

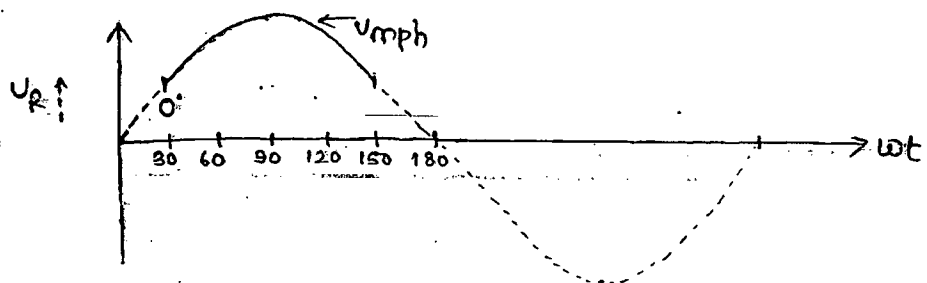
$$\alpha + \omega t_c = 3 \cdot \frac{\pi}{3}$$

$$\alpha + \omega t_c = \pi$$

$$\omega t_c = \pi - \alpha$$

$$\boxed{t_c = \frac{\pi - \alpha}{\omega}}$$

magination method For 3 pulse Converter $\rightarrow$



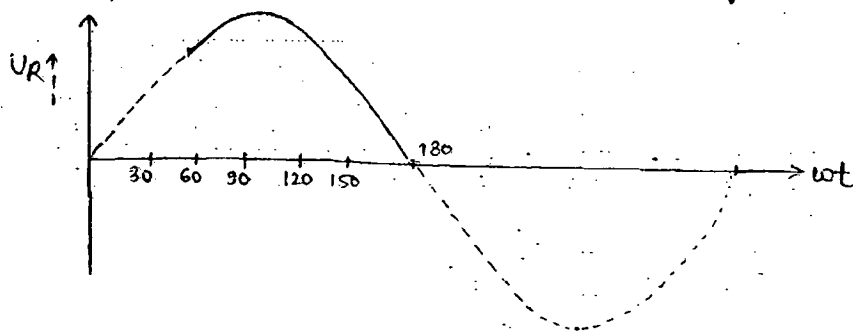
$$\alpha = \omega t - 30^\circ$$

$$\text{Pulse length} = \frac{2\pi}{3} \text{ rad} = 120^\circ$$

$$0 \leq \alpha \leq 150^\circ \rightarrow R \text{ Load}$$

$$0 \leq \alpha \leq 180^\circ \rightarrow \text{Inductive load.}$$

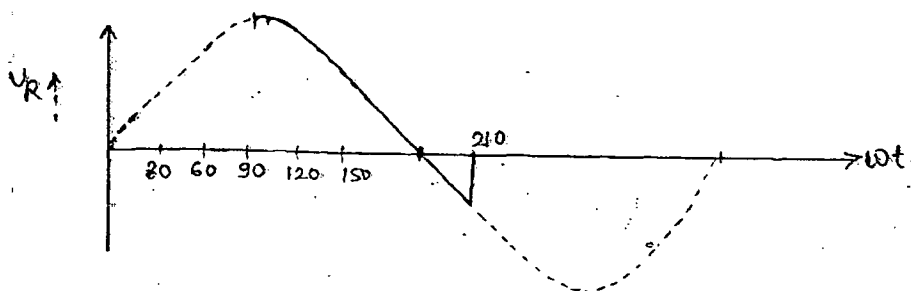
For $\alpha = 0^\circ$, $\omega t = 30^\circ$ (Fig (i))



$$\alpha = \omega t - 30^\circ$$

$$\text{Pulse length} = 120^\circ$$

$$\text{For } \alpha = 30^\circ, \omega t = 60^\circ \text{ \& } 60 + 120 = 180^\circ$$



$$\alpha = 60^\circ, \omega t = 90^\circ, \text{ end } 90 + 120 = 210^\circ$$

6. Pulse converter →

$$\alpha = \omega t - 60^\circ$$

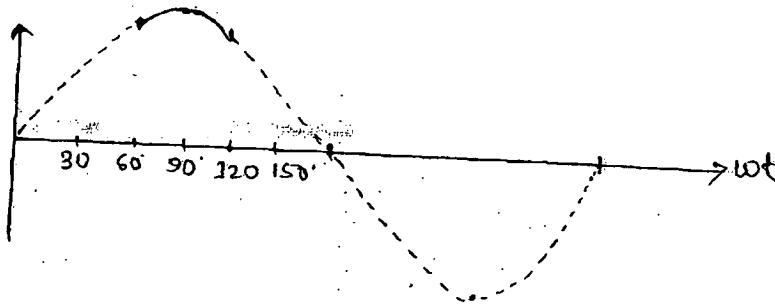
$$\text{pulse length} = \frac{2\pi}{6} \text{ rad} = \frac{\pi}{3} \text{ rad}$$

$$= 60^\circ$$

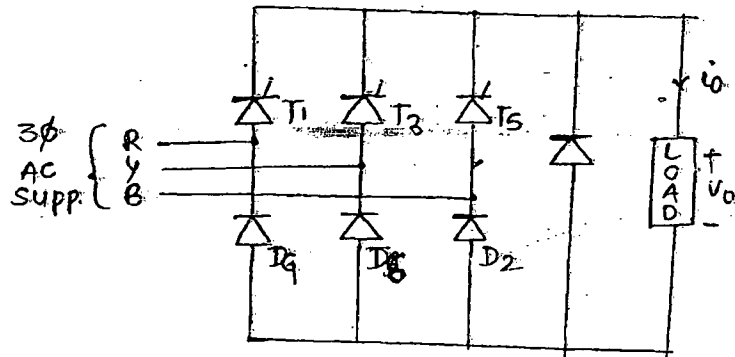
$$0 \leq \alpha \leq 120^\circ \text{ R load}$$

$$0 \leq \alpha \leq 180^\circ \text{ L load}$$

$$\alpha = 0, \omega t = 60^\circ \text{ \& } 60 + 60 = 120^\circ$$



* 3 ϕ Semi Conv^r / 3 ϕ Half Controlled Rectifier $\rightarrow$



Assume High inductive load $\rightarrow$

(1) $\alpha \leq 60^\circ \rightarrow$ * FD will not conduct.

* Conduction angle of each thy. = $\frac{2\pi}{3}$ rad { For every 2π rad }

$$(I_T)_{avg.} = I_o \left(\frac{2\pi/3}{2\pi} \right) = \frac{I_o}{3}$$

$$(I_T)_{rms} = \frac{I_o}{\sqrt{3}}$$

$$I_{sr} = I_o \left(\frac{2\pi/3}{\pi} \right)^{1/2} = \sqrt{\frac{2}{3}} I_o$$

(2) $\alpha > 60^\circ \rightarrow$ * Conduction angle of FD = $(\alpha - \frac{\pi}{3})$ { For every $\frac{2\pi}{3}$ rad }

* Conduction angle of each thy. = $(\pi - \alpha)$ { For every $2\pi/3$ rad }

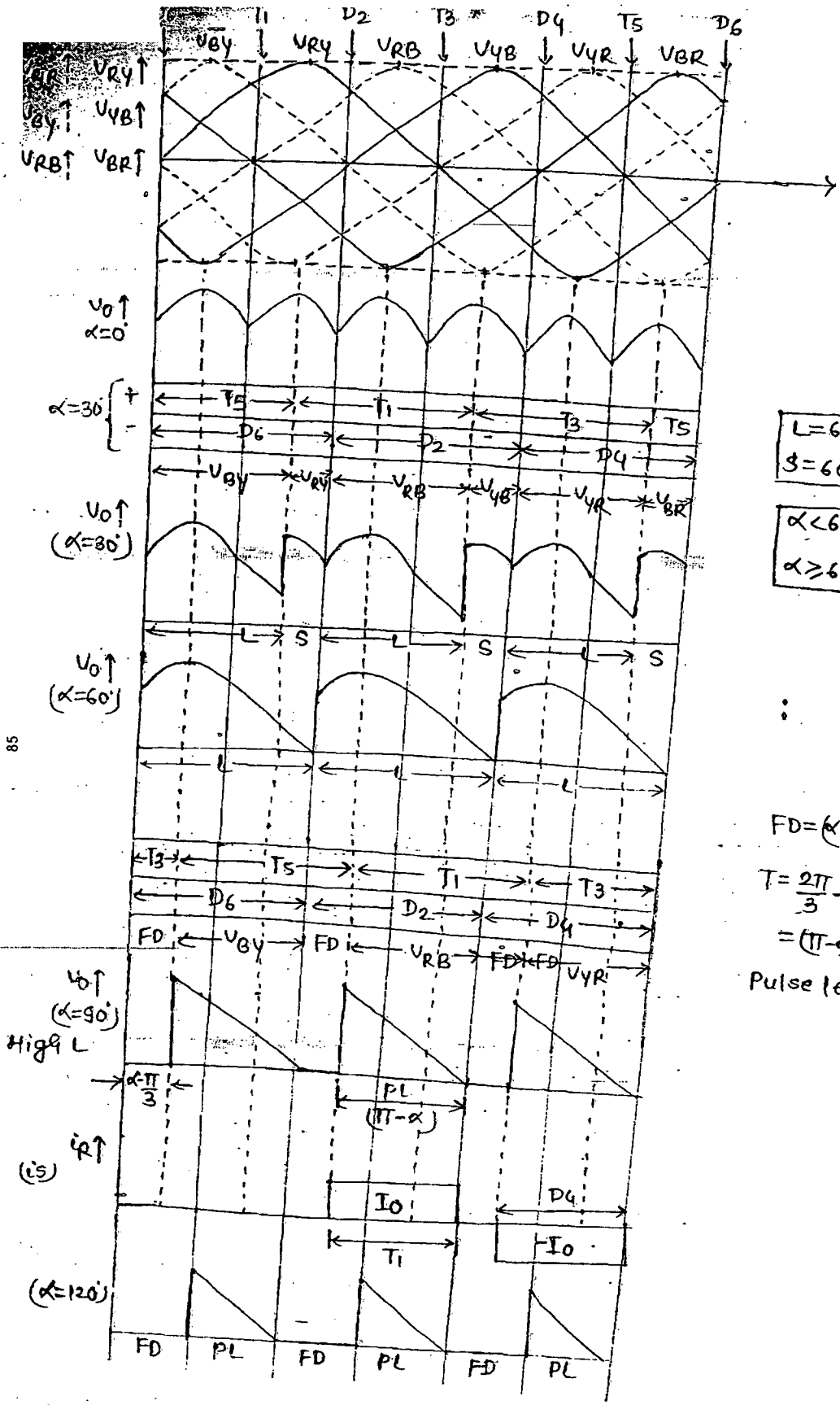
$$(I_T)_{avg.} = I_o \left(\frac{\pi - \alpha}{2\pi} \right) \quad (I_T)_{rms} = I_o \left(\frac{\pi - \alpha}{2\pi} \right)^{1/2}$$

$$I_{sr} = I_o \left(\frac{\pi - \alpha}{\pi} \right)^{1/2}$$

$$(I_{FD})_{avg.} = I_o \left(\frac{\alpha - \pi/3}{2\pi/3} \right)$$

$$(I_{FD})_{rms} = I_o \left[\frac{\alpha - \pi/3}{2\pi/3} \right]^{1/2}$$

$$V_o = \frac{3V_{mL}}{\pi} (1 + \cos \alpha)$$



$$L = 60 + \alpha$$

$$\beta = 60 - \alpha$$

$\alpha < 60 \Rightarrow 6 \text{ pulse}$
 $\alpha > 60 \Rightarrow 3 \text{ pulse}$

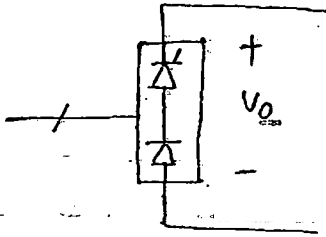
$$FD = (\alpha - \pi/3)$$

$$T = \frac{2\pi}{3} - (\alpha - \frac{\pi}{3})$$

$$= (\pi - \alpha)$$

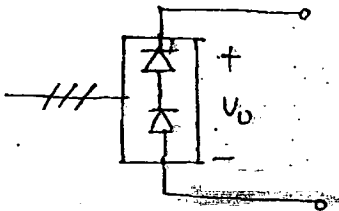
Pulse length = T

1 ϕ semi converter $\rightarrow$



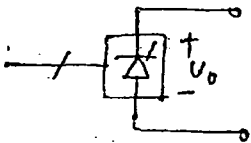
$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

3 ϕ semi converter $\rightarrow$



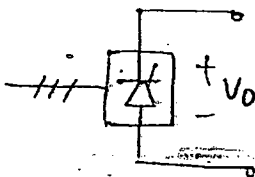
$$V_o = \frac{V_{mL}}{2\pi/3} (1 + \cos \alpha)$$

1 ϕ Full Cond^r $\rightarrow$



$$V_o = \frac{2V_m}{\pi} \cos \alpha$$

3 ϕ Full Conv^r $\rightarrow$



$$V_o = \frac{3V_{mL}}{\pi} \cos \alpha$$

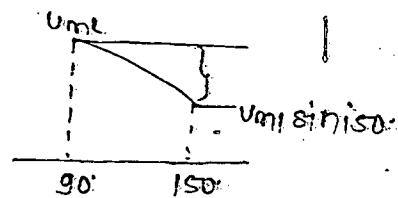
(1/44)

$$\alpha = 30^\circ$$

Peak to peak ripple voltage

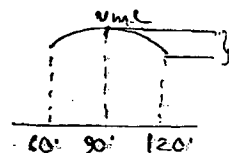
Peak o/p dc voltage

$$\frac{V_{mL} - V_{mL} \sin 150^\circ}{V_{mL}} = 0.5$$



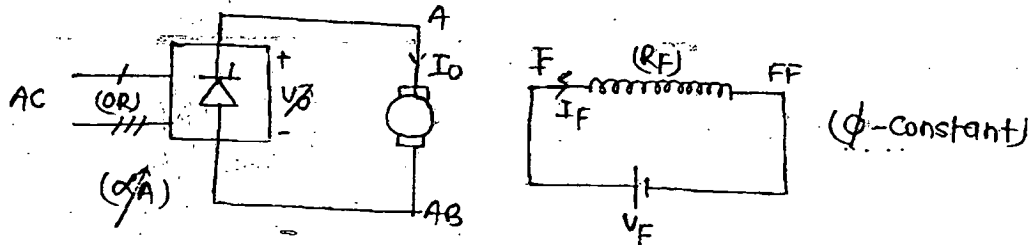
$$\alpha = 0^\circ$$

$$\frac{V_{mL} - V_{mL} \sin 120^\circ}{V_{mL}} = 1 - \frac{\sqrt{3}}{2}$$



Drives

(b) Armature Voltage Control method $\rightarrow (\omega < \omega_r)$



$$\begin{aligned} 1\phi, V_d &= \frac{2V_m}{\pi} \cos \alpha \\ 3\phi, V_d &= \frac{3V_{mL}}{\pi} \cos \alpha \end{aligned}$$

We know that:

$$E_b \propto \phi N$$

$$E_b \propto N \quad (\because \phi \rightarrow \text{const})$$

$$E_b = k \cdot N$$

$$\frac{\text{EMF Const.}}{\text{Motor Const.}} = \frac{V}{\text{rpm}}$$

$$E_b = \omega$$

$$\frac{\text{EMF Const.}}{\text{Motor Const.}} = \left(\frac{\text{V} \cdot \text{sec}}{\text{rad}} \right)$$

$$\text{SI} \rightarrow \omega \text{ rad/sec}$$

$$\omega = \frac{2\pi N}{60}$$

We know that:

$$T_q \propto \phi I_a$$

$$T_q \propto I_a$$

$$T_q = k \cdot I_a$$

$$\frac{\text{Motor Const.}}{\text{Torque const.}} = \left(\frac{\text{Nm}}{\text{A}} \right)$$

$$\frac{\text{Nm}}{\text{A}} = \frac{\text{V} \cdot \text{sec}}{\text{rad}}$$

$$I_o = \frac{T_a}{K}; \quad \text{For motoring mode}$$

$$V_o = E_b + I_o R_a$$

$$V_o = K\omega + I_o R_a$$

~~$$\omega = \frac{V_o - I_o R_a}{K}$$~~

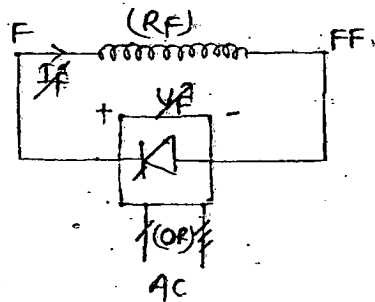
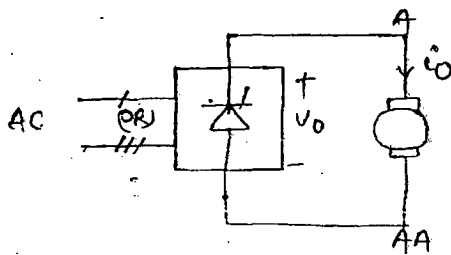
$$\omega = \frac{V_o}{K} - \frac{I_o R_a}{K}$$

$$\omega = \frac{V_o}{K} - \frac{R_a}{K^2} T_a$$

Speed-torque eqⁿ

$$\alpha \uparrow, V_o \downarrow \therefore \omega \downarrow (\omega < \omega_r)$$

(2) Field Control method →



$$V_F = \frac{2V_m}{\pi} \cos \alpha_F \rightarrow 1\phi$$

$$V_F = \frac{3V_{mL}}{\pi} \cos \alpha_F \rightarrow 3\phi$$

$$I_F = \frac{V_F}{R_F}$$

$$\phi \propto I_F$$

$$\phi = K_F I_F$$

($K_F \rightarrow$ Field constant)

$$E_b \propto \phi N$$

$$E_b = K_1 \phi N$$

$$E_b = K_1 K_F N I_F$$

$$E_b = K I_F N$$

EMF const (OR) motor const $\left(\frac{V}{\omega \phi N A} \right)$

$$E_b = k I_f \omega \rightarrow \text{Emf Const (or) motor const. } \frac{\text{V sec}}{\text{rad A}}$$

$$T_q \propto \phi I_a$$

$$T_q = k_1 \phi I_a$$

$$T_q = k_1 (k_f I_f) I_o$$

$$T_q = k I_f I_o$$

$$\rightarrow \text{Torque const. (or) motor const. } \frac{\text{Nm}}{\text{A}^2} = \frac{\text{V sec}}{\text{rad A}}$$

$$I_o = \frac{T_q}{k I_f} ; \text{ For motoring mode;}$$

$$V_o = E_b + I_o R_a$$

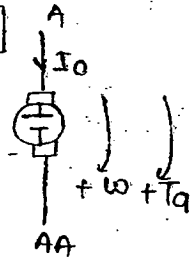
$$V_o = k I_f \omega + I_o R_a$$

$$\omega = \frac{V_o - I_o R_a}{k I_f}$$

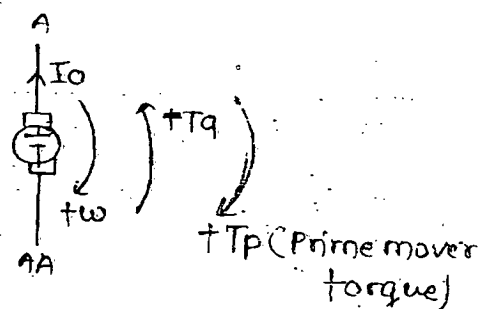
$$\omega = \frac{V_o}{k I_f} - \frac{R_a}{(k I_f)^2} T_q$$

$$\propto F \uparrow, V_f \downarrow, I_f \downarrow \therefore \omega \uparrow (\omega > \omega_r)$$

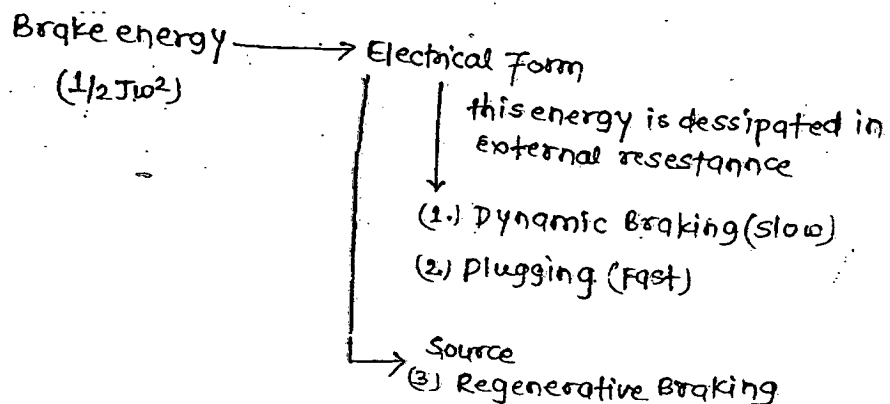
motoring action



Generating action



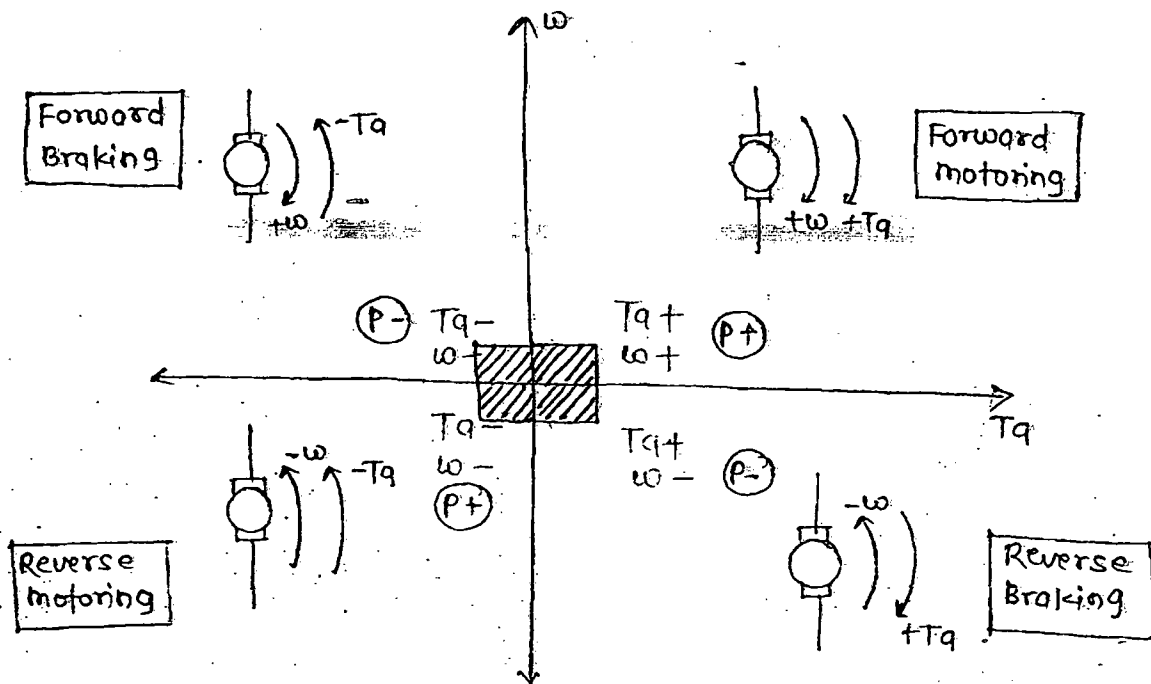
Electrical Braking →



During braking the m/c behaves as generator & the brake energy available in the rotor inertia is converted into ele. form.

* If this energy is given back to the supply then it is known as regenerative braking.

* We can utilize a dc m/c in 4 modes:-



Quadrant operation of Full Converter → (Two quadrant)

1 ϕ Full conv^r

$$V_o = \frac{2V_m \cos \alpha}{\pi}$$

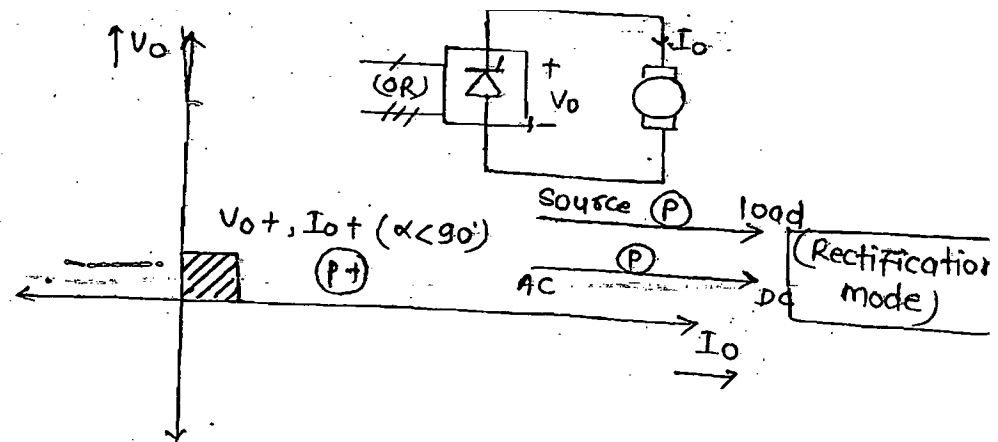
$$\alpha \leq 90^\circ, V_o +$$

$$\alpha > 90^\circ, V_o -$$

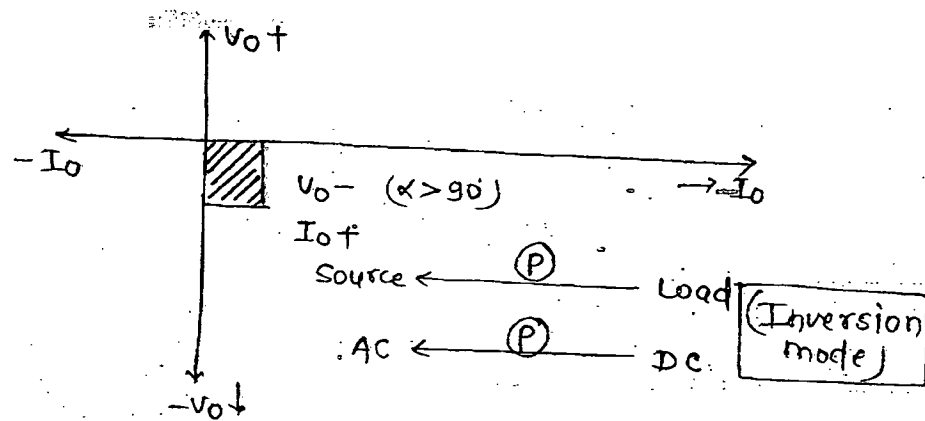
3 ϕ Full conv^r

$$V_o = \frac{3V_{mL} \cos \alpha}{\pi}$$

$$I_o \text{ (always) } +$$



* Rectification mode can be used for motoring mode of a dc m/c & charging battery.

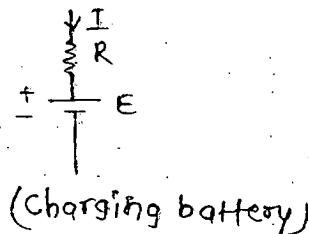
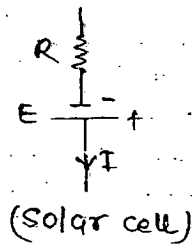
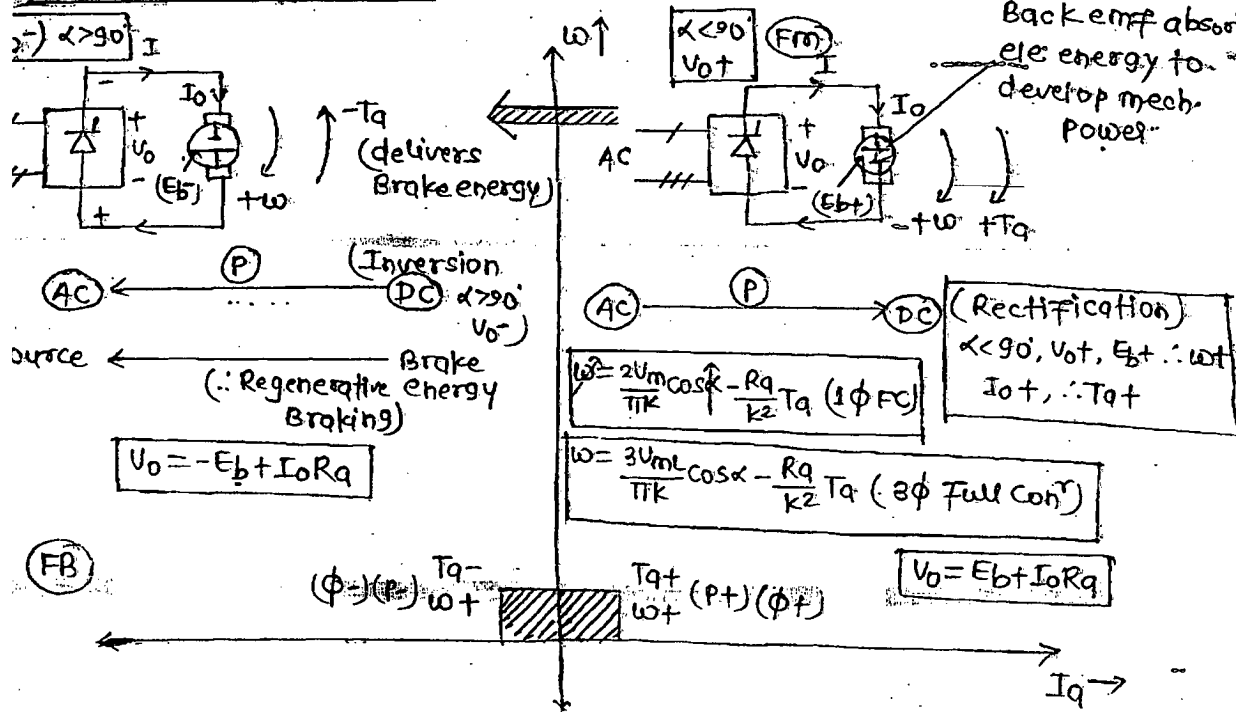


* Inversion mode can be used for regenerative braking of a dc m/c.

* Inversion mode is also used for solar sell.

(The solar energy stored in the form of dc is given to the AC side of conr when conr is supporting the inversion mode)

Full Conv^r fed DC m/c →



Quadrant Operation of semi converter →

1φ semi conv^r

$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

3φ semi conv^r

$$V_o = \frac{3V_m L}{\pi} (1 + \cos \alpha)$$

V_o always → +ve

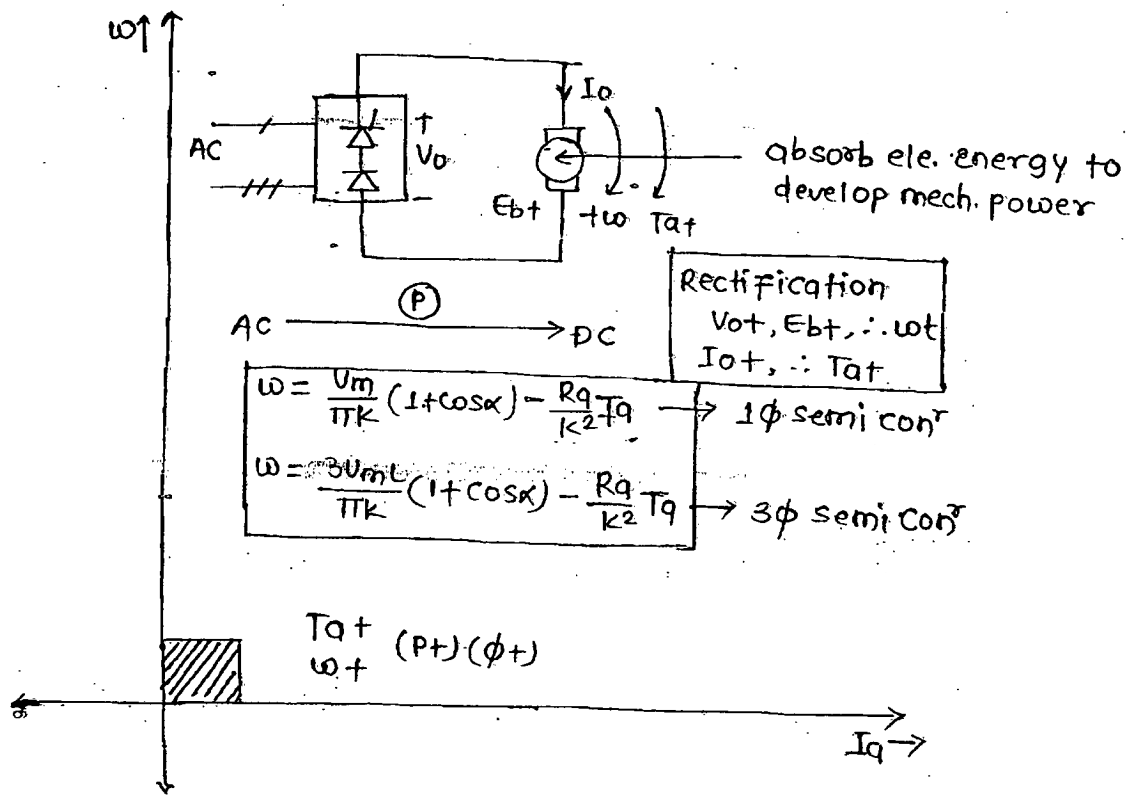
I_o always → +ve

* Semi converter gives only one quadrant operation.

* Inversion of semi converter is not accepted i.e. only charging battery

application is possible with semiconv.

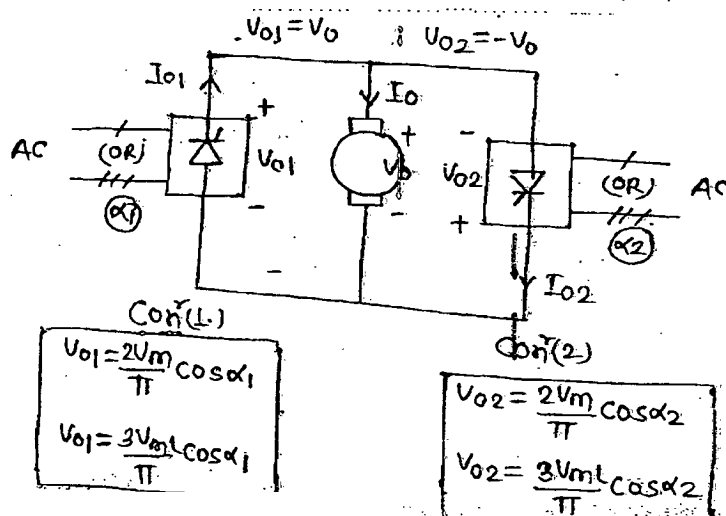
* solar cell application is not possible with semiconverter.

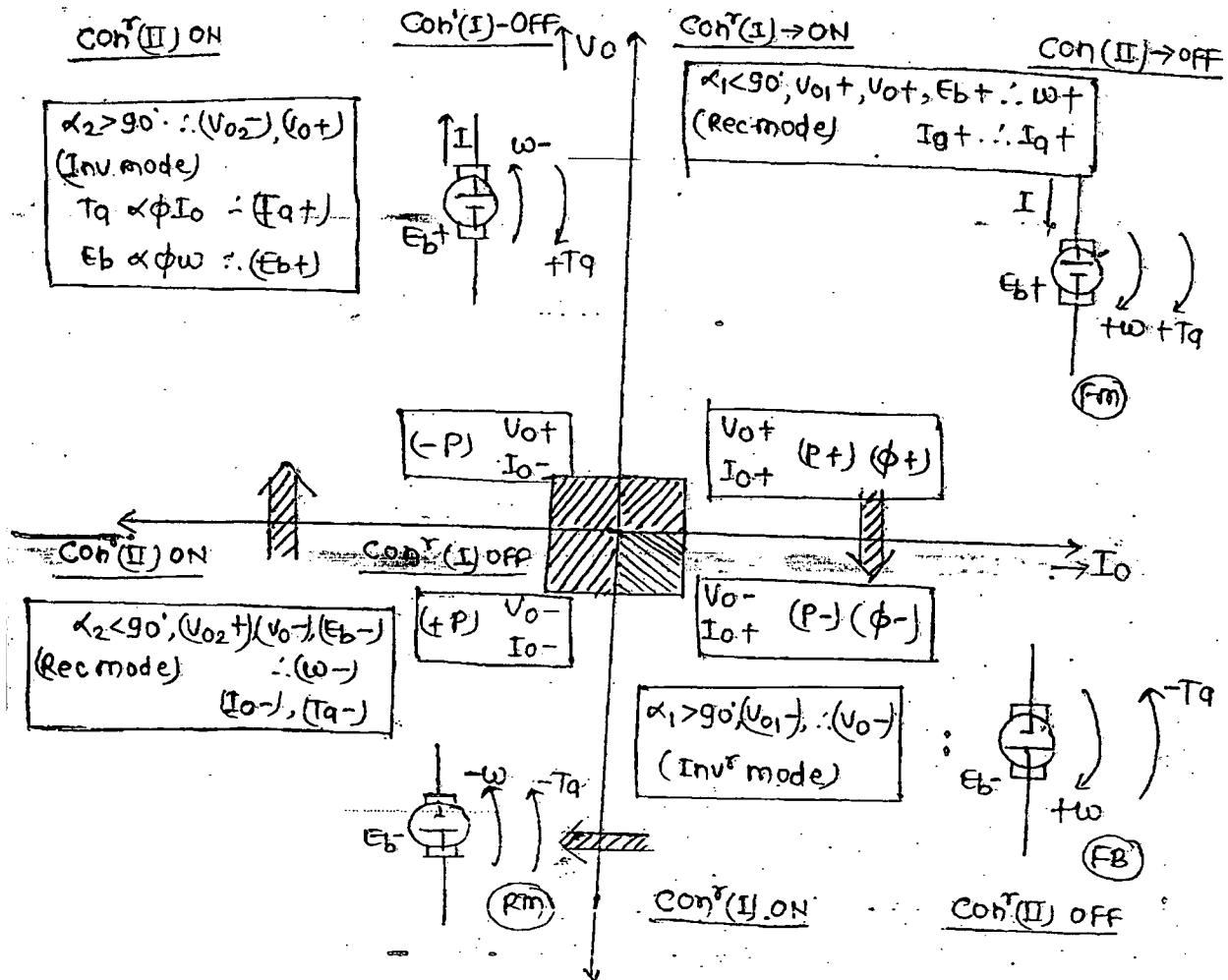


* Dual Conv $\rightarrow$ * It gives 4 quadrant operation.

(1) Non-circulating current type :- * In this dual conv if one conv is in the ON state then other conv remains in the off state.

Advantage:- There is no circulating current b/w 2 conv.





* Disadvantage:- It gives slow speed response & the reversal of arm current is not smooth during switching operation of the con^r.

* Reason of slow speed response:- Here we must provide comm. delay time for outgoing con^r before the incoming con^r is switched on. to avoid high circulating current

* This comm. delay time is responsible for slow speed response.

(2) Circulating current type $\rightarrow$ * In this dual con^r both the con^r are simultaneously in the on state.

Disadvantage:- There will be circulating current b/w 2 con^r & hence

power loss is responsible.

* we can reduce the circulating current if $V_{o1} = -V_{o2}$

$$V_{o1} = -V_{o2}$$

$$\therefore \frac{2V_m}{\pi} \cos \alpha_1 = -\frac{2V_m}{\pi} \cos \alpha_2$$

$$\cos \alpha_1 + \cos \alpha_2 = 0$$

$$\cos \alpha_1 + \cos (180 - \alpha_1) = 0$$

$$(\alpha_2 = 180 - \alpha_1)$$

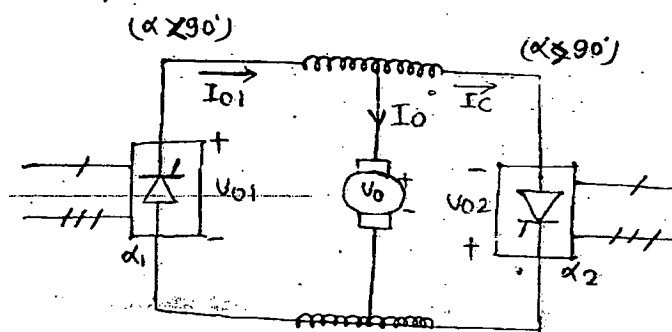
$$0 = 0$$

$$\text{Hence } \alpha_2 = 180 - \alpha_1$$

$$\boxed{\alpha_1 + \alpha_2 = 180^\circ}$$

* even after satisfying the condⁿ $\alpha_1 + \alpha_2 = 180^\circ$ still there is some circulating current due to the instantaneous vol. diff. between the 2 con^s.

* To reduce this circulating current we must connect a reactor b/w the 2 con^s as shown in fig. given below.

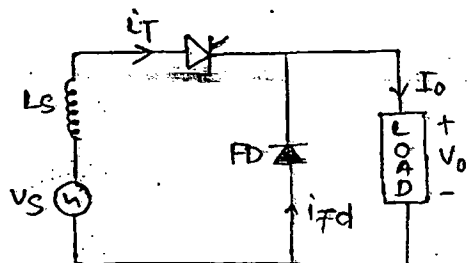


$$I_{o1} = I_o + I_{o2}$$

Advantage → It gives high speed response & reversal of arm. current is smooth during switching operation at con^s.

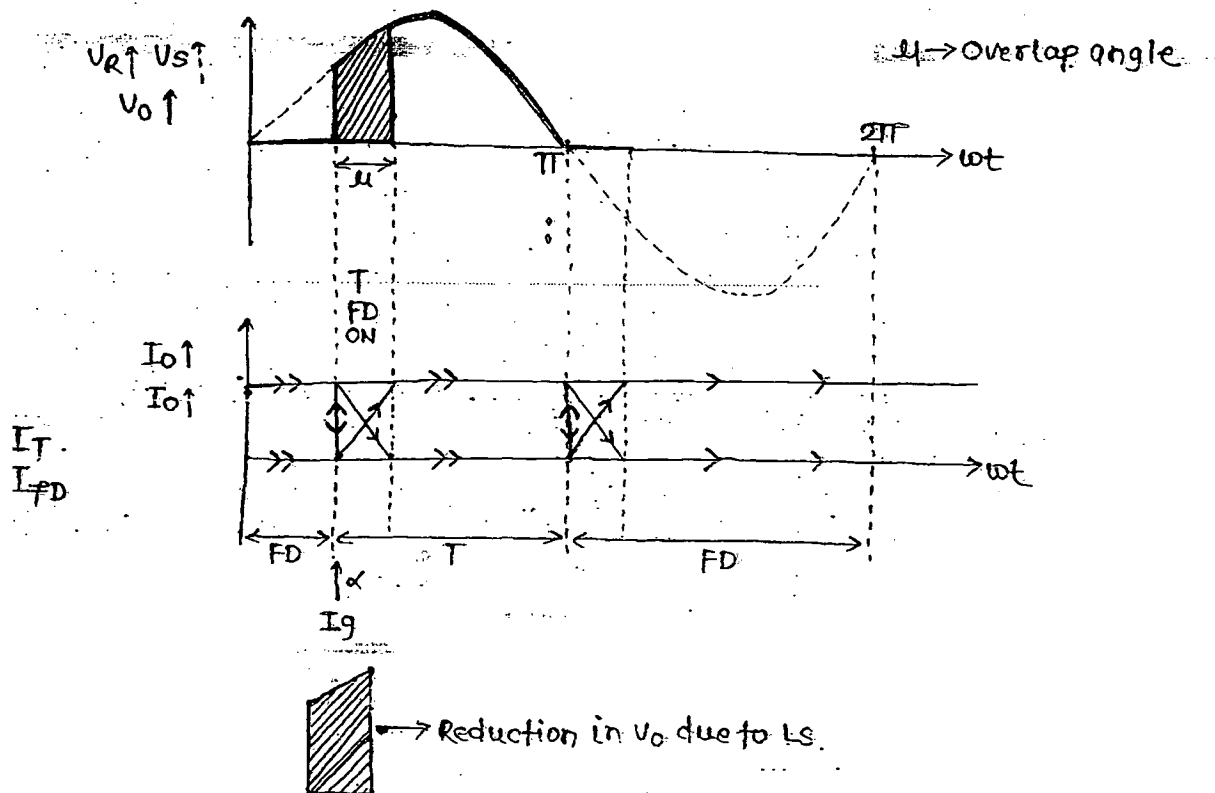
Effect of Source Inductance → Let L_s be the source inductance

One pulse converter →



Let us assume high inductive Load.

Without L_s (ideal source) →
With L_s (Non-ideal source) →



With L_s →

During μ , T & FD → ON state $\therefore V_o = 0$

$i_T + i_{FD} = I_o$ (during μ)

The value of load current constant & value of thy. current suddenly increases. Hence $I_{FD} \downarrow$.

$$V_s = L_s \frac{di}{dt}$$

$$V_m \sin \omega t \, dt = L_s di_s$$

Multiplying w by the both sides of eqⁿ

$$V_m \sin \omega t \, d(\omega t) = L_s \omega di_s$$

$$V_m \sin \omega t \, d(\omega t) = L_s \omega di_s$$

Integrating both sides

$$\int_{\alpha}^{\alpha+\mu} V_m \sin \omega t \, d(\omega t) = \omega L_s \int_0^{I_o} di_s$$

$$V_m [\cos \alpha - \cos(\mu + \alpha)] = \omega L_s I_o$$

Deviding both side by 2π ; then we will get average reduction in area

$$\frac{V_m}{2\pi} [\cos \alpha - \cos(\mu + \alpha)] = \frac{\omega L_s I_o}{2\pi}$$

$$\frac{V_m}{2\pi} [\cos \alpha - \cos(\mu + \alpha)] = f L_s I_o$$

$$\Delta V_{d0} = \frac{V_m}{2\pi} [\cos \alpha - \cos(\mu + \alpha)] = f L_s I_o \quad \text{----- (i)}$$

Where; ΔV_{d0} = average reduction in dc o/p voltage due to L_s

$$V_o = \frac{V_m}{2\pi} (1 + \cos \alpha) - \Delta V_{d0}$$

$$V_o = \frac{V_m}{2\pi} (1 + \cos \alpha) - f L_s I_o \quad \text{----- (ii)}$$

$$V_o = \frac{V_m}{2\pi} [1 + \cos(\alpha + \mu)] \quad \text{----- (iii)}$$

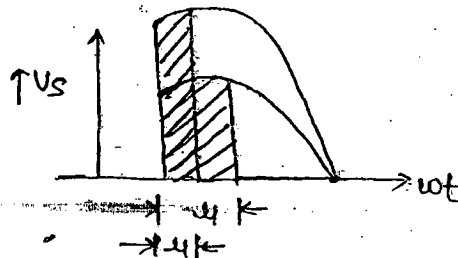
ΔV_{d0} does not depend on μ ; it depends on $f L_s I_o$ but μ depend on the ΔV_{d0} .

* ΔV_{d0} depends only on f, L_s, I_o

* μ depends on ΔV_{d0} & hence f, L_s, I_o, V_s, α

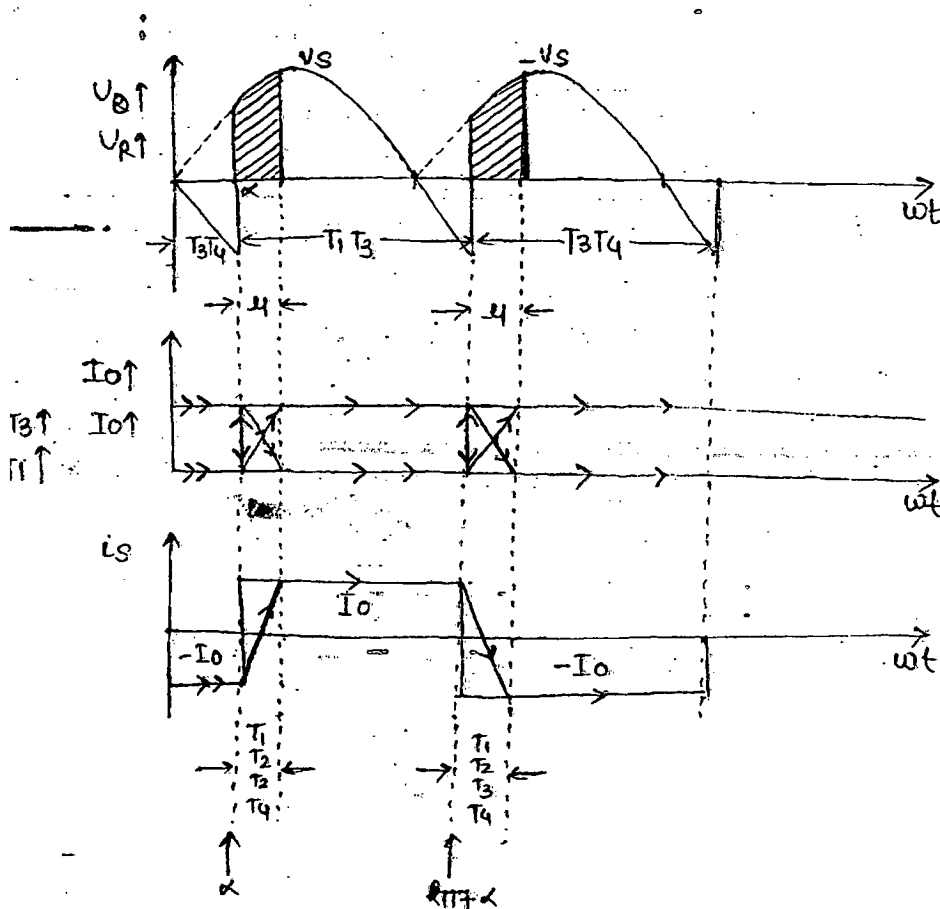
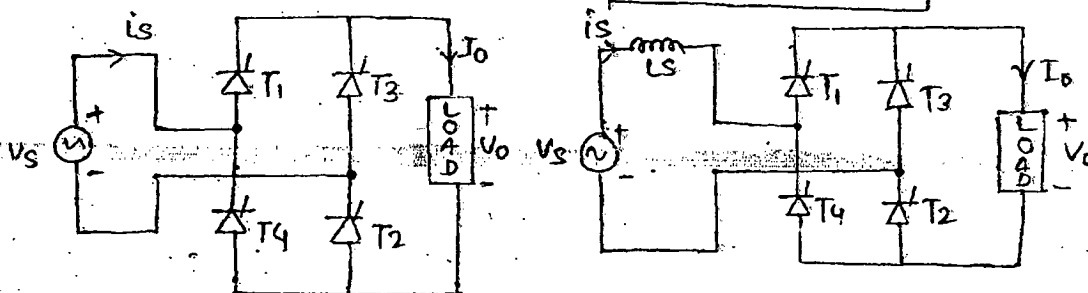
* If $f \uparrow$ (or) $L_s \uparrow$ (or) $I_o \uparrow$, without changing the overlap angle V_s & α then $\mu \uparrow$

* If $V_s \uparrow$, without changing T , L_s , I_o , α then $\mu \downarrow$ to remain the avg constant.



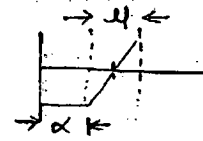
2: Two pulse converter $\rightarrow$

without L_s (Ideal)
with L_s (Non-ideal)



(iii) Fundamental displacement factor

$$FDF = \cos\left(\alpha + \frac{\mu}{2}\right)$$

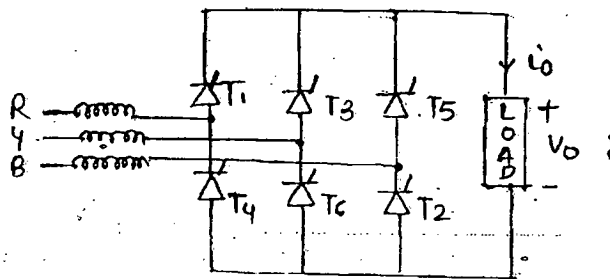


(iv) $g \uparrow$, $TMD \downarrow \therefore$ Harmonic on AC side $\downarrow$
(advantage)

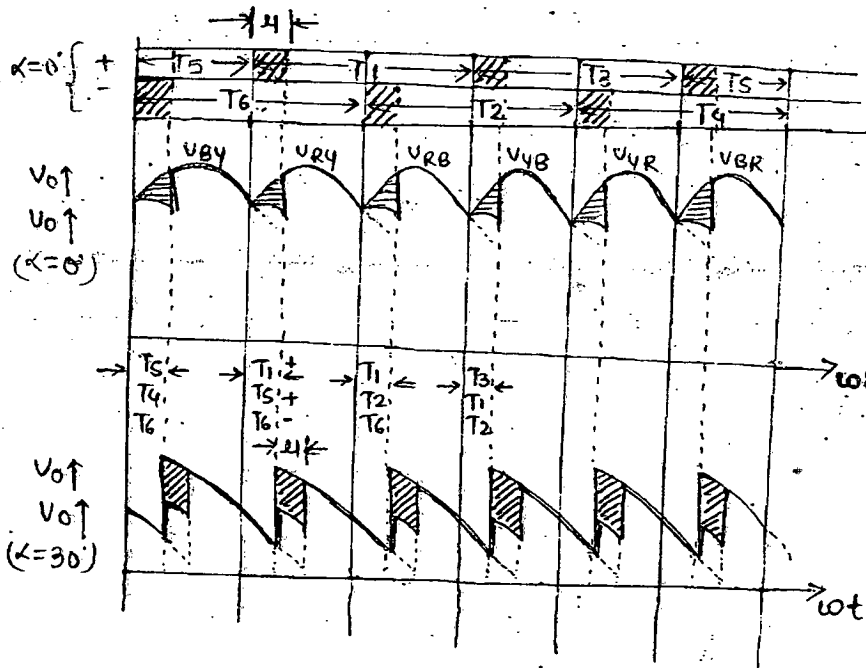
(v) $PF = g \uparrow FDF \downarrow$ (can't say)

Here the increase in g value is more than decrease in FDF
 $\therefore$ the PF is slightly increased.

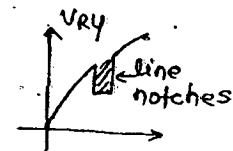
(3) 6 pulse converter $\rightarrow$



without L_s
with L_s



$$\frac{v_{BY} + v_{RY}}{2} \text{ (mean value)}$$



Ques → If α increases without changing other parameters then what happen to overlap angle?

Ans → Case (I) $0 \leq \alpha \leq 90^\circ$ ($\alpha \uparrow, u \downarrow$)

If $\alpha \uparrow$, without changing F, L_s, I_o & V_s , then $u \downarrow$
 $\text{Const } \Delta V_{do} \rightarrow \text{constant}$

$\alpha \uparrow$ ripple vol $\uparrow$, height of reduction $\uparrow \therefore u \downarrow$ to maintain same area of ΔV_{do} .

Overlap angle is max^m at $\alpha = 0^\circ$ & min^m at $\alpha = 90^\circ$

Case (2) $\alpha > 90^\circ$ ($\alpha \uparrow, u \uparrow$)

$\alpha \uparrow$, Ripple $\downarrow$, height $\downarrow, \therefore u \uparrow$

Conventional question →

Que. (3/48)

at $\alpha = 0^\circ, u_0 = 30^\circ$

then u_0 at $\alpha = 30^\circ, 60^\circ, 90^\circ, 120^\circ$

$$\frac{I_o}{I_p} = \cos \alpha - \cos(u + \alpha)$$

For $\alpha = 0^\circ$,
$$\frac{I_o}{I_p} = \cos 0^\circ - \cos(30 + 0)$$

$$\frac{I_o}{I_p} = 0.133$$

α	u	
0	30	→ max ^m
30	8.46 12.85	$\alpha \uparrow, u \downarrow$
60	7.61 8.46	
90	7.61	→ min ^m
120	9.21	$\alpha \uparrow, u \uparrow$

Let $V_{d0} \rightarrow (V_0)_{\max}$ $V_{d0} = \frac{2V_m}{\pi}$ (2 pulse)

$V_{d0} = \frac{3V_{mL}}{2\pi}$ (3 pulse)

$V_{d0} = \frac{3V_{mL}}{\pi}$ (6 pulse)

with $L_s \rightarrow$

During u , $T_1 T_2$ & $T_3 T_4 \rightarrow ON \therefore V_0 = 0$

$$V_m \sin \omega t = L_s \frac{di_s}{dt}$$

$$V_m \sin \omega t dt = L_s di_s$$

$$V_m \sin \omega t d(\omega t) = \omega L_s di_s$$

$$\int_{-I_0}^{I_0} V_m \sin \omega t d(\omega t) = \omega L_s \int_{-I_0}^{I_0} di_s \quad \left[\begin{array}{l} \text{Source current change} \\ \text{from } I_0 \text{ to } -I_0 \end{array} \right]$$

$$V_m [\cos \alpha - \cos(\alpha + u)] = 2\omega L_s I_0$$

$$\frac{V_m}{\pi} [\cos \alpha - \cos(\alpha + u)] = \frac{2\omega L_s I_0}{\pi}$$

$$\Delta V_{d0} = \frac{V_m}{\pi} [\cos \alpha - \cos(\alpha + u)] = \frac{2\omega L_s I_0}{\pi} \quad \text{--- (i)}$$

$$\Delta V_{d0} = \frac{V_{d0}}{2} [\cos \alpha - \cos(\alpha + u)] \quad m=2,3,6$$

m	ΔV_{d0}
1	$7L_s I_0$
2	$47L_s I_0$
3	$37L_s I_0$
6	$67L_s I_0$

$$V_0 = V_{d0} \cos \alpha - \Delta V_{d0} \quad \text{--- (ii)}$$

$$V_0 = \frac{V_{d0}}{2} [\cos \alpha + \cos(\alpha + u)] \quad \text{--- (iii)}$$

$$-\frac{V_m}{\pi} [\cos \alpha - \cos(\alpha + \mu)] = \frac{2\omega L_s I_o}{\pi}$$

$$I_o = \frac{V_m}{2\omega L_s} [\cos \alpha - \cos(\alpha + \mu)]$$

$$I_o = I_p [\cos \alpha - \cos(\alpha + \mu)]$$

$$\boxed{\frac{I_o}{I_p} = \cos \alpha - \cos(\alpha + \mu)} \quad \text{where } I_p = \frac{V_m}{2\omega L_s}$$

Que. → What is meant by inductive vol. regulation?

Ans. → It is a measure of reduction in o/p vol. due to source inductance.

It is taken as a ratio of $= \frac{\Delta V_{d0}}{V_{d0}}$

$$= \frac{\frac{V_{d0}}{2} [\cos \alpha - \cos(\mu + \alpha)]}{V_{d0}}$$

$$UR^{\%} = \frac{\cos \alpha - \cos(\alpha + \mu)}{2}$$

$$= \frac{1 - \cos \mu_0}{2}$$

$\mu_0 =$ Overlap angle at $\alpha = 0^\circ$

Que. → What is the effect of source inductance on the performance of Conⁿ?

Ans. → (i) It reduces the avg. o/p vol. of Conⁿ.

(ii) It limits the maxⁿ range of firing angle.

$$\boxed{\alpha_{max} = 180^\circ - [\omega t_q + \mu_0]}$$

Ideal Vol. source, Ideal thy. $\alpha_{max} = 180^\circ$

Ideal vol. source, Practical thy. $\alpha_{max} = 180^\circ - \omega t_q$

Practical vol. source, practical thy. $\alpha_{max} = 180^\circ - \omega t_q - \mu$