

## MATHEMATICS

## **SET- A**

1. The projection of  $(\hat{i} - \hat{j})$  on  $(\hat{i} + \hat{j})$  is  
 (A) 0 (B) 1  
 (C) -1 (D) 2

2. The ratio in which the join of the point A(2, -1, 3) and B(4, 3, 1) is divided by the point C $\left(\frac{20}{7}, \frac{5}{7}, \frac{15}{7}\right)$  is  
 (A) 4 : 3 (B) 3 : 4  
 (C) 1 : 2 (D) 3 : 5

3. The integral  $\int_0^{\pi/2} \frac{\sqrt{\tan x} dx}{\sqrt{\tan x + \sqrt{\cot x}}}$  has the value  
 (A)  $\frac{\pi}{8}$  (B)  $\frac{\pi}{4}$   
 (C)  $\frac{\pi}{3}$  (D) 0

4. Solution of the differential equation  $\frac{dx}{x} + \frac{dy}{y} = 0$  is  
 (A)  $xy = C$  (B)  $\log x \log y = C$   
 (C)  $x + y = C$  (D)  $\frac{1}{x} + \frac{1}{y} = C$

5. If  $P(C \cap D) = \frac{1}{2}$ ,  $P(C' \cap D') = \frac{1}{3}$ ,  $P(C) = p$  and  $P(D) = 2p$ , then the value of  $p$  is  
 (A)  $\frac{7}{18}$  (B)  $\frac{1}{3}$   
 (C)  $\frac{4}{7}$  (D)  $\frac{1}{9}$

6. The function of  $2x^3 - 3x^2 - 12x + 4$  has
- (A) Two maxima
  - (B) Two minima
  - (C) No maximum and no minimum
  - (D) One maximum and one minimum
7. The tangents to the curve  $y = x^3$  at  $x = -1$  and  $x = 1$  are
- |                            |                                 |
|----------------------------|---------------------------------|
| (A) Intersecting obliquely | (B) Perpendicular to each other |
| (C) Parallel               | (D) None of these               |
8. The value of the integral  $\int \frac{\sin 4x}{\cos 2x} dx$  is
- |                    |                    |
|--------------------|--------------------|
| (A) $\sin 4x + C$  | (B) $-\sin 2x + C$ |
| (C) $-\cos 2x + C$ | (D) $\cos 4x + C$  |
9. Equation of a vertical line on left hand side of the  $x$ -axis at a distance ' $a$ ' from it is
- |              |             |
|--------------|-------------|
| (A) $x = a$  | (B) $x = 0$ |
| (C) $x = -a$ | (D) $x = 1$ |
10. The principal value of  $\tan^{-1} \sqrt{3} - \cot^{-1}(-\sqrt{3})$  is
- |                      |                     |
|----------------------|---------------------|
| (A) $\frac{-\pi}{2}$ | (B) $\frac{\pi}{2}$ |
| (C) $\frac{2\pi}{3}$ | (D) $\frac{\pi}{6}$ |
11. The next term of the sequence  $\sqrt{3}, \sqrt{12}, \sqrt{27}, \sqrt{48}$  is
- |                 |                 |
|-----------------|-----------------|
| (A) $\sqrt{75}$ | (B) $\sqrt{70}$ |
| (C) $\sqrt{65}$ | (D) $\sqrt{60}$ |

12. If  $n$  and  $r$  are positive integers such that  $1 \leq r \leq n$  then  ${}^nC_r + {}^nC_{r-1}$  is equal to

(A)  ${}^nC_{r+1}$

(B)  ${}^{n-1}C_r$

(C)  ${}^{n+1}C_r$

(D)  ${}^{n+1}C_{r-1}$

13. The value of  $p$  for which  $p(\hat{i} + \hat{j} + \hat{k})$  is a unit vector is

(A)  $\pm 3$

(B) 2

(C) 1

(D)  $\pm \frac{1}{\sqrt{3}}$

14. The number of ways in which 5 boys and 3 girls can be seated in a row so that no two girls are together is

(A) 2000

(B) 14000

(C) 14300

(D) 14400

15. If  $\overset{\leftrightarrow}{a}$  and  $\overset{\leftrightarrow}{b}$  are unlike vectors, then  $\overset{\leftrightarrow}{a} \cdot \overset{\leftrightarrow}{b}$  is

(A)  $a b$

(B) 0

(C)  $-a b$

(D) 1

16. Direction cosines of vector  $2\hat{i} - 3\hat{j}$  are

(A)  $(2, -3, 0)$

(B)  $\left( \frac{2}{\sqrt{13}}, \frac{-3}{\sqrt{13}}, 0 \right)$

(C)  $\left( \frac{2}{13}, \frac{-3}{13}, 0 \right)$

(D)  $(-2, 3, 0)$

17. The integral  $\int_0^{\pi/2} \sin x \sin 2x \, dx$  has the value

(A)  $\frac{1}{2}$

(B)  $\frac{2}{3}$

(C)  $\frac{2}{5}$

(D)  $\frac{3}{4}$

18. If  $\frac{dy}{dx} = e^{-2y}$  and  $y=0$  when  $x=5$ , then the value of  $x$  when  $y=3$  is

(A)  $e^5$

(B)  $e^6 + 1$

(C)  $\frac{e^6 + 9}{2}$

(D)  $\log_e 6$

19.  $I_n$  is an identity matrix of order  $n$ , then  $(I_n)^{-1}$  is equal to

(A) 0

(B)  $n I_n$

(C)  $I_n$

(D) Does not exist

20.  $\begin{vmatrix} a-b & b-c & c-a \\ x-y & y-z & z-x \\ p-q & q-r & r-p \end{vmatrix}$  is equal to

(A) 1

(B) -1

(C) 0

(D) -2

21. Domain of  $\sqrt{a^2 - x^2}$  ( $a > 0$ ) is

(A)  $(-a, a)$

(B)  $[-a, a]$

(C)  $(0, a)$

(D)  $(-a, 0]$

22. If  $a, b, c$  are in Arithmetic progression, then

(A)  $a^2 + c^2 + 6abc = 8b^3$

(B)  $a^3 + c^3 + 6abc = 8b^2$

(C)  $a^3 + c^3 + 6abc = 8b^3$

(D)  $a + c + 6abc = 8b^3$

23. The value of  $\cos \phi + \sin(270^\circ + \phi) - \sin(270^\circ - \phi) + \cos(180^\circ + \phi)$  is

(A) 0

(B) 1

(C) -1

(D) 2

24.  $\frac{\cos^3 \phi - \cos 3\phi}{\cos \phi} + \frac{\sin^3 \phi + \sin 3\phi}{\sin \phi}$  is equal to

(A) 1

(B) 3

(C) 5

(D) 0

25. If  $\tan \theta = \frac{a}{b}$ , then  $b \cos 2\theta + a \sin 2\theta$  is equal to

(A)  $a$

(B)  $b$

(C)  $\frac{b}{a}$

(D)  $\frac{a}{b}$

26. The distance between the line  $3x - 4y + 9 = 0$  and  $6x - 8y - 17 = 0$  is

(A)  $\frac{7}{4}$  units

(B)  $\frac{7}{3}$  units

(C)  $\frac{7}{2}$  units

(D)  $\frac{7}{5}$  units

27. The value of the integral  $\int \frac{\cos 2x}{\sqrt{1+\cos 4x}} dx$  is

(A)  $\frac{-\sin 2x}{2} + C$

(B)  $\frac{x}{\sqrt{2}} + C$

(C)  $\frac{x^2}{\sqrt{2}} + C$

(D)  $\frac{\cos 2x}{2} + C$

28. A can hit a target 4 times in 5 shots, B can hit 3 times in 4 shots, and C can hit 2 times in 3 shots. Then, the probability that A, B and C hit the target is

(A)  $\frac{1}{5}$

(B)  $\frac{2}{5}$

(C)  $\frac{4}{6}$

(D)  $\frac{3}{6}$

29. If a random variable  $X$  follows a binomial distribution with mean 4 and variance 2, then its distribution function  $P(X = r)$  is

(A)  ${}^6C_r \left(\frac{1}{4}\right)^{6-r}$

(B)  ${}^8C_r \left(\frac{1}{4}\right)^{8-r}$

(C)  ${}^8C_r \left(\frac{1}{2}\right)^8$

(D)  ${}^6C_r \left(\frac{1}{2}\right)^{6-r}$

30. Unit vector normal to the plane  $3x - 6y + 2z = 7$  is

(A)  $\frac{1}{7}(3\hat{i} - 6\hat{j} + 2\hat{k})$

(B)  $\frac{1}{11}(3\hat{i} - 6\hat{j} + 2\hat{k})$

(C)  $\frac{1}{7}(\hat{i} - \hat{j} + \hat{k})$

(D)  $\frac{1}{3}(\hat{i} - \hat{j} + \hat{k})$

31. A couple has 2 children. If it is known that one of the children is a boy, then the probability that both are boys is

(A)  $\frac{1}{3}$

(B)  $\frac{2}{5}$

(C)  $\frac{3}{5}$

(D)  $\frac{2}{3}$

32. The value of  $k$  for which the lines  $\frac{x-1}{-3} = \frac{y-2}{2k} = \frac{z-3}{2}$  and  $\frac{x-1}{3k} = \frac{y-2}{1} = \frac{z-3}{5}$  are perpendicular to each other is

(A)  $\frac{10}{7}$

(B)  $\frac{5}{7}$

(C)  $\frac{4}{7}$

(D)  $\frac{3}{7}$

33. If  $e^x + e^y = e^{x+y}$ , then  $\frac{dy}{dx}$  is equal to

(A)  $-e^{y-x}$

(B)  $e^x$

(C)  $e^y$

(D)  $-e^{x-y}$

34. A binary operation  $*$  is defined by  $a * b = a + b + 1 \forall a, b \in Z$ . The identity element of  $*$  in  $Z$  is given by

(A) 0 (B) 1

(C) -1 (D) 2

35. The range of the function  $\sin(\sin^{-1}x + \cos^{-1}x)$ ,  $|x| \leq 1$  is

(A)  $[-1, 1]$  (B)  $(-1, 1)$

(C)  $\{-1, 1\}$  (D)  $\{1\}$

36. Two dice are thrown. The odds in favour of getting the sum 7 is

(A) 5 : 1 (B) 5 : 31

(C) 1 : 5 (D) 31 : 5

37. If  $y = \frac{3^x}{x^3}$ , then  $\frac{dy}{dx}$  is equal to

(A)  $\frac{3^x \log 3}{x^3}$

(B)  $\frac{3^x}{x^3} \left(1 - \frac{3}{x}\right)$

(C)  $\frac{3^x}{x^3} \left(\log 3 - \frac{3}{x}\right)$

(D)  $\frac{3^x}{x^3} \left(\frac{3}{x} - \log 3\right)$

38. If  $X + Y = \begin{bmatrix} 5 & 2 \\ 0 & 9 \end{bmatrix}$  and  $X - Y = \begin{bmatrix} 3 & 6 \\ 0 & -1 \end{bmatrix}$ , then  $Y$  is equal to

(A)  $\begin{bmatrix} -1 & 2 \\ 0 & -5 \end{bmatrix}$

(B)  $\begin{bmatrix} 8 & 8 \\ 0 & 8 \end{bmatrix}$

(C)  $\begin{bmatrix} 2 & -4 \\ 0 & 10 \end{bmatrix}$

(D)  $\begin{bmatrix} 1 & -2 \\ 0 & 5 \end{bmatrix}$

39. If  $\lim_{x \rightarrow 0} \frac{1 - \cos mx}{1 - \cos 5x} = 4$ , then the value of  $m$  is

(A) 5 (B) 10  
 (C) 8 (D) 4

40. For any sets A, B and C,  $(A \cap B')' \cup (B \cap C)$  is equal to

(A)  $A' \cup B \cup C$  (B)  $A' \cup B$   
 (C)  $A' \cup C'$  (D)  $A' \cap B$

41. The complex number  $\frac{-16}{1+i\sqrt{3}}$  lies in quadrant

(A) I (B) II  
 (C) III (D) IV

42. The integral  $\int \sqrt{1 - \sin 2x} dx$  has the value

(A)  $\cos 2x + C$  (B)  $\sin x \cos x + C$   
 (C)  $\sin x + \cos x + C$  (D)  $\sin x - \cos x + C$

43. If  $2, x, y, z, \frac{32}{81}$  are in G.P, then the value of  $x, y$  and  $z$  are respectively

(A)  $\frac{4}{3}, \frac{8}{9}, \frac{16}{27}$  (B)  $\frac{1}{3}, \frac{8}{9}, \frac{16}{27}$   
 (C)  $\frac{4}{3}, \frac{7}{9}, \frac{8}{27}$  (D)  $\frac{4}{3}, \frac{8}{9}, \frac{13}{27}$

44. The length of the perpendicular from the point  $(a, b)$  to the line  $\frac{x}{a} + \frac{y}{b} = 1$  is

(A)  $\frac{|ab|}{\sqrt{a^2 - b^2}}$  (B)  $\frac{|ab|}{\sqrt{a^2 + b^2}}$   
 (C)  $\frac{|(ab)^2|}{\sqrt{a^2 - b^2}}$  (D)  $\frac{|(ab)^3|}{\sqrt{a^2 + b^2}}$

45. The total number of 9 digit numbers which have all different digits is

(A)  $10!$

(B)  $9!$

(C)  $9 \times 9!$

(D)  $10 \times 10!$

46. The value of the integral  $\int \cos \left\{ 2 \tan^{-1} \sqrt{\frac{1-x}{1+x}} \right\} dx$  is

(A)  $\sin^{-1}(\log x) + C$

(B)  $\log \frac{1-x}{1+x} + C$

(C)  $\cot^{-1} x + C$

(D)  $\frac{1}{2}x^2 + C$

47. If  $\overset{\leftrightarrow}{a}$  is a unit vector such that  $(\overset{\leftrightarrow}{x-a}) \cdot (\overset{\leftrightarrow}{x+a}) = 3$ , then the value of  $|\overset{\leftrightarrow}{x}|$  is

(A) 2

(B) 1

(C) 0

(D) 3

48. The value of  $p$  for which  $\overset{\leftrightarrow}{a} = 3\hat{i} + \hat{j} - 2\hat{k}$  and  $\overset{\leftrightarrow}{b} = \hat{i} + p\hat{j} - 3\hat{k}$  are perpendicular to each other is

(A) -7

(B) 1

(C) -9

(D) 2

49. A die is rolled. If the outcome is an even number, then the probability that it is a number greater than 2 is

(A)  $\frac{2}{3}$

(B)  $\frac{1}{4}$

(C)  $\frac{1}{3}$

(D)  $\frac{2}{5}$

50. A die is rolled 30 times. Getting a number greater than 4 is a success. Then, mean of the number of successes is

(A) 12

(B) 14

(C) 10

(D) 15





65. For any vector  $\hat{a}$ , the expression  $(\hat{a} \cdot \hat{i})\hat{i} + (\hat{a} \cdot \hat{j})\hat{j} + (\hat{a} \cdot \hat{k})\hat{k}$  is equal to

(A)  $\hat{a}$  (B)  $\hat{i}$   
 (C)  $\hat{j}$  (D)  $\hat{k}$

66. Two skew lines  $\vec{r} = \vec{r}_1 + \lambda \vec{u}$  and  $\vec{r} = \vec{r}_2 + \mu \vec{v}$  intersect if  $\frac{(\vec{r}_2 - \vec{r}_1) \cdot (\vec{u} \times \vec{v})}{|\vec{u} \times \vec{v}|}$  is equal to

(A) 0 (B) 1  
 (C) -1 (D) 2

67. If  $|\vec{a}| = \sqrt{26}$ ,  $|\vec{b}| = 7$  and  $|\vec{a} \times \vec{b}| = 35$ , then  $\vec{a} \cdot \vec{b}$  is equal to

(A) -7 (B) 7  
 (C) 5 (D) 9

68.  $\lim_{x \rightarrow 0} \left[ \frac{\sin 3x + 4x}{7x + \tan 2x} \right]$  is equal to

(A)  $\frac{4}{7}$  (B)  $\frac{7}{4}$   
 (C)  $\frac{7}{9}$  (D)  $\frac{9}{7}$

69. The integral  $\int_{\pi/8}^{3\pi/8} \frac{\cos x}{\cos x + \sin x} dx$  has the value

(A)  $\frac{\pi}{8}$  (B)  $\frac{\pi}{4}$   
 (C)  $\frac{\pi}{3}$  (D)  $\frac{\pi}{6}$

70. Let A and B be two square matrices such that  $AB = A$ ,  $BA = B$ , then  $B^2$  is equal to

(A) A (B) I  
 (C) 0 (D) B

71. If  $\sin \phi + \operatorname{cosec} \phi = 2$ , then  $\sin^2 \phi + \operatorname{cosec}^2 \phi$  is equal to

(A) 1 (B) 2  
 (C) 4 (D) 0

72. Sum of the cubes of first n odd natural numbers is

(A)  $\{n(2n-1)\}^2$  (B)  $n^2(2n-1)$   
 (C)  $n^2(2n^2+1)$  (D)  $n^2(2n^2-1)$

73. The value of  $(-\sqrt{-1})$  is  
 (A) 0      (B) 1  
 (C)  $i$       (D)  $-i$

74. The value of the integral  $\int \frac{x}{1+x^4} dx$  is  
 (A)  $\frac{1}{2} \tan^{-1} x^2 + C$       (B)  $\log(1+x^2) + C$   
 (C)  $\sin^{-1} 2x + C$       (D)  $\cot^{-1} x + C$

75. If  $A$  and  $B$  are events such that  $P(A) = 0.4$ ,  $P(B) = 0.8$  and  $P(B/A) = 0.6$ , then  $P(A \cap B)$  is  
 (A) 0.75      (B) 0.45  
 (C) 0.30      (D) 0.24

76. The value of  $m$  for which the line  $\underline{r} = (\hat{i} + 2\hat{j} - \hat{k}) + \lambda(2\hat{i} + \hat{j} + 2\hat{k})$  is parallel to the plane  $\underline{r} \cdot (3\hat{i} - 2\hat{j} + m\hat{k}) = 12$  is  
 (A) 2      (B) 1  
 (C) -1      (D) -2

77. A and B are two square matrices and their inverses exist, then  $(AB)^{-1}$  is equal to  
 (A)  $A^{-1}B^{-1}$       (B)  $A^{-1}B$   
 (C)  $B^{-1}A^{-1}$       (D)  $BA^{-1}$

78.  $\int_1^3 \frac{\cos(\log x)}{x} dx$  has the value  
 (A)  $\sin(\log 3)$       (B)  $\sin(\log 2) - 3$   
 (C)  $\log 3$       (D)  $2\log 2$

79. If  $y = \tan^{-1} \frac{ax-b}{bx+a}$ , then  $\frac{dy}{dx}$  is equal to  
 (A)  $\frac{a}{1+x^2}$       (B)  $\frac{b}{1+x^2}$   
 (C)  $\frac{1}{1+x^2}$       (D)  $\frac{-1}{1+x^2}$



88. The volume of a ball is increasing at the rate of  $4\pi$  c.c/sec. The rate of increase of radius when the volume is  $288\pi$  c.c is
- (A)  $\frac{1}{6}$  cm/sec      (B)  $\frac{1}{36}$  cm/sec  
 (C)  $\frac{1}{9}$  cm/sec      (D)  $\frac{1}{24}$  cm/sec
89. If  $x = t^2$ ,  $y = t^3$ , then  $\frac{d^2y}{dx^2}$  is equal to
- (A)  $\frac{3}{2}$       (B)  $\frac{3}{2t}$   
 (C)  $\frac{3}{4t^2}$       (D)  $\frac{3}{4}$
90.  $\lim_{x \rightarrow 0} \frac{3^{2+x} - 9}{x}$  is equal to
- (A)  $9 \log_e 3$       (B)  $3 \log_e 9$   
 (C) 1      (D)  $\log_e 3^2$
91. The number of diagonals that can be formed by a polygon of 100 sides is
- (A) 4,850      (B) 4,950  
 (C) 5,000      (D) 10,000
92. If  $\cos x + \cos y = \frac{1}{3}$  and  $\sin x + \sin y = \frac{1}{4}$ , then  $\tan\left(\frac{x+y}{2}\right)$  is equal to
- (A)  $\frac{4}{3}$       (B)  $\frac{3}{4}$   
 (C)  $\frac{1}{4}$       (D)  $\frac{1}{3}$
93. If  $f(x) = \frac{x}{x-1}$ , then  $\frac{f(a)}{f(a+1)}$  is equal to
- (A)  $f(-a)$       (B)  $f\left(\frac{1}{a}\right)$   
 (C)  $f(a^2)$       (D)  $f\left(-\frac{a}{a-1}\right)$

94. If  $\sin A = \frac{1}{\sqrt{5}}$  and  $\cos B = \frac{3}{\sqrt{10}}$ , then the value of  $A + B$  is
- (A)  $0^\circ$  (B)  $30^\circ$   
 (C)  $45^\circ$  (D)  $60^\circ$
95. The point  $(3, -2, -5)$  lies in octant
- (A) I (B) III  
 (C) VI (D) VIII
96. The solution set of the equation  $x^2 + \frac{x}{\sqrt{2}} + 1 = 0$  are
- (A)  $\left( \frac{1+\sqrt{7}i}{2\sqrt{2}}, \frac{1-\sqrt{7}i}{2\sqrt{2}} \right)$  (B)  $\left( \frac{-1+\sqrt{7}i}{2\sqrt{2}}, \frac{-1-\sqrt{7}i}{2\sqrt{2}} \right)$   
 (C)  $\left( \frac{1+\sqrt{7}i}{\sqrt{2}}, \frac{1-\sqrt{7}i}{\sqrt{2}} \right)$  (D)  $\left( \frac{-1+\sqrt{7}i}{2}, \frac{-1-\sqrt{7}i}{2} \right)$
97. The equation  $\frac{x^2}{10-a} + \frac{y^2}{4-a} = 1$  represents an ellipse if
- (A)  $a < 4$  (B)  $a > 4$   
 (C)  $4 < a < 10$  (D)  $a > 10$
98. If  $|a| = 2$ ,  $|b| = 7$  and  $a \times b = 3\hat{i} + 2\hat{j} + 6\hat{k}$ , the angle between  $a$  and  $b$  is
- (A)  $\frac{\pi}{6}$  (B)  $\frac{\pi}{4}$   
 (C)  $\frac{\pi}{3}$  (D)  $\frac{\pi}{2}$
99. Angle made by the vector  $r = \hat{i} + \hat{j} - \hat{k}$  with the X-axis is
- (A)  $\cos^{-1} \frac{1}{2}$  (B)  $\cos^{-1} \frac{1}{3}$   
 (C)  $\cos^{-1} \frac{1}{\sqrt{3}}$  (D)  $\cos^{-1} \sqrt{3}$
100. Direction ratios of the line  $\frac{4-x}{2} = \frac{y}{6} = \frac{1-z}{3}$  are
- (A)  $-2, 6, -3$  (B)  $2, 6, 3$   
 (C)  $\frac{1}{2}, 6, 3$  (D)  $\frac{1}{2}, \frac{6}{4}, \frac{3}{4}$