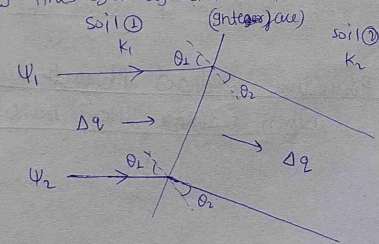


Lecture
22/11/19

Note : Flow through non-homogeneous medium.

- 1) When medium pass from one medium to another medium then flow lines get deflected and at interface such that



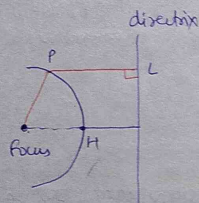
$$\frac{K_1}{K_2} = \frac{\tan \theta_1}{\tan \theta_2} \quad **$$

$K_2 > K_1 \Rightarrow (\theta_2 > \theta_1)$
(away)

$K_2 < K_1 \Rightarrow (\theta_2 < \theta_1)$
toward

θ_1 and θ_2 (angle made by flow lines with the normal to interface before and after getting deflected)

Phreatic line

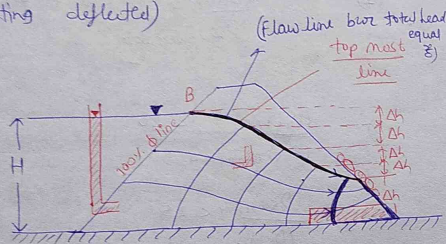


$$PF = PL$$

(Properties of Parabola)

- ① Phreatic line is the top most flow line below which seepage takes place (boundary cond)
- ② Pressure below the phreatic line is hydrostatic and pressure on and above phreatic line is atmospheric
- ③ Phreatic line follows the path of base parabola for which any point lying on it is equidistant from focus and directrix.
- ④ The flow takes place through downstream phase of dam, hence it always remains wet. To prevent its damage either stone pitching is carried out ^{on it} or drainage filter is provided

Procedure to draw Phreatic line
When drainage filter is provided



Step ① Focus (F) is the intersection of permeable and impermeable medium.

Step ② Let BD ($L = nH$) is the Horizontal projection of Upstream face AB of Dam on water surface level. Phreatic line start from point C, distance ($0.3L$) from Point B.

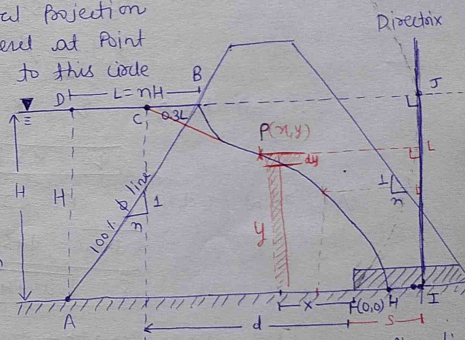
Step ③ Draw a circle with Point 'C' as center and CF as radius to meet the Horizontal projection of water surface level at Point J. Vertical tangent to this circle at Point J represent the directrix of Parabola.

Step ④ The vertex H of Parabola lies in between focus and directrix such that $(FH = HI = \frac{S}{2})$

Where $S \rightarrow$ focal length

Step ⑤ To locate the intermediate Point P (x, y) on Phreatic line Draw a circle with focus F as center and Radius of $(x + S)$ which meet the vertical line drawn at a distance of x from focus (F) which represent the required Point (P) such that $PF = PL = (x + S)$.

Step ⑥ Join all the intermediate Points P (x, y) to obtain the Phreatic line. As Phreatic line is the top most flow line it must start from Point (B) and should be $\perp$ to equipotential line (A-B) Hence an anticrossion is made to obtain phreatic line.



Determination of discharge through drainage

Let in distance due head loss is $dy \therefore i = \frac{dy}{dx}$
As per Darcy's law $q = KiA = K \frac{dy}{dx} (y \times 1)$

At Point P (a, y) $PF = PL$

$$\sqrt{x^2 + y^2} = x + s$$

$$x^2 + y^2 = x^2 + 52 + 2 \times 5$$

$$y^2 = s^2 + 2xs$$

$$\cancel{y} \cdot \frac{dy}{dn} = \cancel{y} \cdot s \quad \left(\frac{dy}{dn} \right) = \frac{s}{y}$$

$$\therefore \text{Discharge } Q = K \cdot \left(\frac{dy}{dx} \right) \cdot (y \cdot 1) = K \cdot \frac{5}{y} \cdot y^3 \cdot 1$$

$q = K \cdot S$ $\star\star$ $m^3/s / m \text{ length}$

At point C (d, h) $(F_z \leq J)$

$$\sqrt{d^2 + H^2} = d + S$$

$$S = \sqrt{d^2 + h^2} = d$$

$$d = \text{Base length} - \text{filter length} - 0.7L$$

If Non-isotopic medium

$q \propto K'S$ $K' = \sqrt{K_x K_y}$

$$[S = \sqrt{d_1^2 + h^2} - dr] \quad d_T = d \sqrt{\frac{\kappa_y}{\kappa_x}}$$

(H change नहीं होता
transform में क्योंकि
change होता)

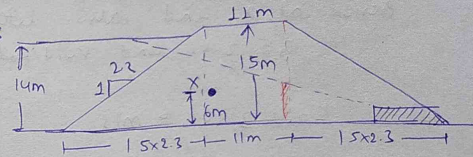
vertical change नहीं होता Horizontal $\therefore X = X_T \sqrt{\frac{K_y}{K_x}}$

Page No. (29) Question (40)

$$k_n = 8 \times 10^{-7} \text{ cm/s}$$

$$k_2 = 3.6 \times 10^{-7} \text{ cm/s}$$

Nd₂ 18



(a) seepage

$$p_s = (H - n \Delta h) \gamma_w$$

$$\Delta_h = \frac{H}{N_d} = \frac{14}{18}$$

$$q = K.H. \frac{N_f}{N_d}$$

$$\Delta h = 0.77$$
$$n = ?$$

$$[K'] = \sqrt{K_x K_y} = \sqrt{8 \times 10^{-7} \times 3.6 \times 10^{-7}} = 10^{-7} \times 536$$

$$q = K'S = 5.36 \times 10^{-7} \times S$$

$$S = \sqrt{d_T^2 + H^2} - d_T$$

$d = \text{Base width} - \text{filter medium} - 0.7L$

$$= (15 \times 2.3 + 11 + 15 \times 2.3) = 80 \text{ m}$$

$$L = 2.3 \times 14$$

$$d = 80 - 12 - 0.7 \times 2.3 \times 14 = 45.46 \text{ m}$$

$$d_T = d \sqrt{\frac{K_B}{K_D}} = 45.46 \sqrt{\frac{3 \times 10^{-7}}{6 \times 10^{-7}}} = 30.45 \text{ m}$$

$$s = \sqrt{d_r^2 + H^2} - d_r = \sqrt{30.45^2 + 172^2} - 30.45 = 170 \text{ cm}$$

$$Q_2 \text{ k/s} = 5.26 \times 10^{-7} \frac{\text{km} \cdot 10^{-2} \text{ m}}{\text{sec}} \times 3.06$$

$$\begin{matrix} \text{double} \\ \uparrow \end{matrix} = 3.164 \times 10^{-8} \text{ m}^3/\text{s/m}^2$$

$$p_{H_2} = (p_{H_2})_{DH} = (1 - \eta) \Delta h - DH = 1 - 1.2 = -0.2$$

$$= (1 - 3 \times \frac{14}{16}) - 6 = 5.67 \text{ m}$$

$$V_2(P.H)_{20} = 5.62 \times 9.81 = 55.59$$

Ques- (25) Also Determine seepage Pressure per water pressure at X and also determine P.O.S if $h = 2.65$ and void Ratio = 7

I) $K = 3.8 \times 10^{-6} \text{ m/s}$

$$q = KH \cdot \frac{Nf}{Nd} = 3.8 \times 10^{-6} \times 6.3 \times \frac{3}{10}$$

$$q = 7.182 \times 10^{-6} \frac{\text{m}^3}{\text{s}} = 7.182 \times 10^{-6} \times 10^4 \text{ cm}^3/\text{s}$$

$$q = 7.182 \text{ cm}^3/\text{s} \quad \text{Ans}$$

II) (T.H) / seepage Head (h) = $H - \Delta h$ ^{drawn} $\approx 6.3 - 5 \times \left(\frac{6.3}{10}\right)$

$$p_s = \gamma_w \cdot h = 9.81 \times 3.15 = 30.9 \text{ kN/m}^2 = 3.15 \text{ m}$$

III) $PH = TH - DH = 3.15 - (-9.4) = 12.5 \text{ m}$

$$\left[\begin{array}{l} \Delta h = \frac{H}{Nd} = \frac{6.3}{10} \\ H = \end{array} \right.$$

$$U = (PH) \gamma_w = 12.5 \times 9.81 = 123.11 \text{ kN/m}^2$$

IV) $P.O.S = \frac{jc}{\gamma_{sat}} = \frac{\left(\frac{9-1}{1+e}\right)}{\left(\frac{\Delta h}{1}\right)} = \frac{\left(\frac{9.65-1}{1+0.7}\right)}{\frac{6.3}{10}} = 4.62$

Page No. (31)

Solution (3)

$$d_o = 8 \text{ m}$$

$$\text{thickness} = 1 \text{ m}$$

$$q = 200 \text{ kN/m}^2$$

$$\sigma_z = \frac{q \cdot D^2}{(D + 2nz)^2}$$

$$\sigma_z = \frac{200 \times (8)^2}{(8 + 2 \times (1) \times 4)^2}$$

$$\sigma_z)_{\text{ring}} = \sigma_z)_{\text{outer rim}} - (\sigma_z)_{\text{inner}}$$

$$(1 - \cos 3\alpha_o) q - (1 - \cos 3\alpha_i) q$$

$$= \left\{ 1 - \left(\frac{4}{\sqrt{4^2 + 4^2}} \right)^3 \right\} 200$$

$$- \left\{ 1 - \left(\frac{4}{\sqrt{4^2 + 3^2}} \right)^3 \right\} 200$$

$$= 31.7 \text{ kN/m}^2 \quad \checkmark$$

