

Chapter 4

Transistor Biasing

LEARNING OBJECTIVES

After reading this chapter, you will be able to understand:

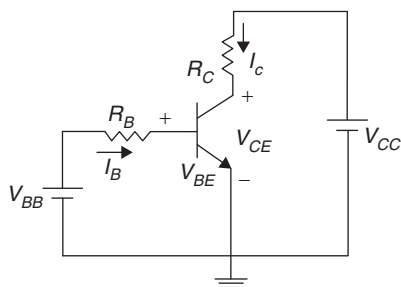
- The operating point
- Bias stability
- Stability factor
- 3 Biasing the BJT
- Bias compensation
- Compensation techniques
- Thermistor compensation
- Sensistor compensation
- Thermal run away
- Thermal resistance
- Biasing the FET
- Four resistor bias circuit

THE OPERATING POINT

A Transistor is a current controlled 3-terminal device having 2 junctions (i) Base-emitter junction and (ii) Base-collector junction.

Base-emitter Junction	Base-collector Junction	Application	Region of Operation
FB	FB	ON switch	Saturation
FB	RB	Amplifier	Active
RB	FB	–	Inverse active
RB	RB	OFF switch	Cut-off

Transistor Circuit Under DC Condition



Apply KVL at input side gives $V_{BB} - I_B R_B - V_{BE} = 0$
 $\Rightarrow V_{BE} = V_{BB} - I_B R_B$

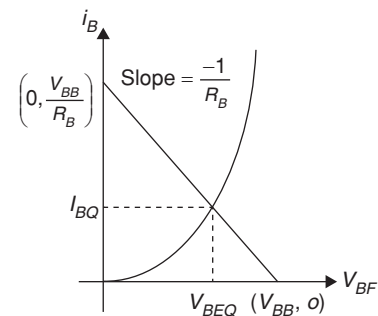
$$\text{When } V_{BE} = 0 \Rightarrow I_B = \frac{V_{BB}}{R_B}$$

$$I_B = 0 \Rightarrow V_{BE} = V_{BB}$$

DC load line is the line joining the two points

$$(V_{BB}, 0) \text{ and } \left(0, \frac{V_{BB}}{R_B}\right)$$

Input Characteristics of a CE Transistor



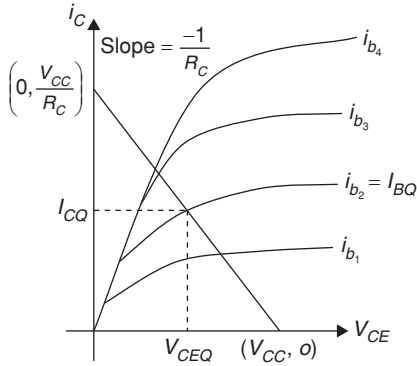
Intersection of the load line with the characteristics of the transistor gives the Q point (operating point). Apply KVL at the output:

$$V_{CC} - I_C R_C - V_{CE} = 0$$

$$V_{CE} = 0 \Rightarrow I_C = \frac{V_{CC}}{R_C}$$

$$I_C = 0 \Rightarrow V_{CE} = V_{CC}$$

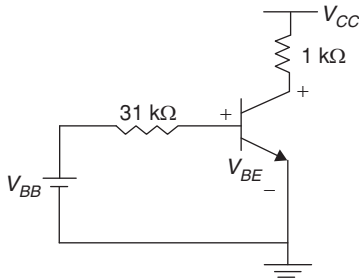
Output Characteristics of a CE Transistor



Intersection of the load line with the output characteristics for a particular value of I_B gives the Quiescent point/ Operating point.

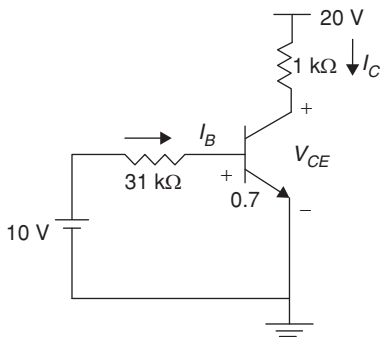
Hence 'Q' point is given by $Q(I_{CQ}, V_{CEQ})$

Example 1: Determine the 'Q' point for the following circuit if $\beta = 50$ and $V_{BB} = 10\text{ V}$, $V_{BE} = 0.7\text{ V}$, $V_{CC} = 20\text{ V}$.



- (A) (0.3 mA and 5 V) (B) (15 mA and 5 V)
(C) (0.6 mA and 4 V) (D) (15 mA and 4 V)

Solution: (B)



Writing KVL for the base emitter loop gives

$$10 - 31 I_B - 0.7 = 0$$

$$\Rightarrow I_B = 0.3\text{ mA}$$

$$I_{CQ} = \beta (0.3\text{ mA}) = 15\text{ mA}$$

Writing KVL for the collector loop gives

$$20\text{ V} - I_C (1\text{ k}\Omega) - V_{CE} = 0$$

$$\Rightarrow V_{CE} = 20 - (15\text{ mA}) (1\text{ k})$$

$$= 20 - 15$$

$$V_{CE} = 5\text{ V}$$

$$(I_C, V_{CEQ}) = (15\text{ mA}, 5\text{ V})$$

BIAS STABILITY

Operating point defines where the transistor will operate on its characteristics curve, under DC conditions. For linear (minimum distortion) amplification, the DC operating point should not be too close to the maximum power and voltage or current rating and should avoid the regions of saturation and cut off. To keep the operating point stable, we use external network to bias the transistor.

The stability of operating point depends on V_{BE} , β , I_{CO} . β is very sensitive to temperature, and V_{BE} decreases about 2.5 mV for each 1°C increase in temperature. The reverse saturation current typically doubles for every 10°C increase in temperature.

Stability Factor(S)

$$I_C = f(I_{CO}, V_{BE}, \beta)$$

$$S = \frac{\partial I_C}{\partial I_{CO}}, S^I = \frac{\partial I_C}{\partial V_{BE}}, S^{II} = \frac{\partial I_C}{\partial \beta}$$

$$I_C = \beta I_B + (1 + \beta) I_{CO}$$

Differentiating wrt I_C gives

$$1 = \beta \frac{\partial I_B}{\partial I_C} + (1 + \beta) \frac{\partial I_{CO}}{\partial I_C}$$

$$\Rightarrow 1 = \beta \frac{\partial I_B}{\partial I_C} + \frac{1 + \beta}{S} \Rightarrow S = \frac{1 + \beta}{1 - \beta \frac{\partial I_B}{\partial I_C}}$$

Where 'S' is the stability factor.

Smaller value of 'S' is desirable for a proper biasing of circuit to act as an amplifier.

The networks are the most stable and least sensitive to temperature changes have the smallest stability factors.

BIASING THE BJT

Base Bias or Fixed Bias

Input loop

$$V_{CC} = I_B R_B + V_{BE}$$

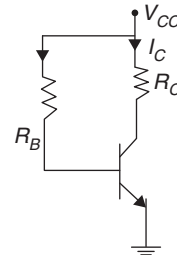
$$I_B = \frac{V_{CC} - V_{BE}}{R_B}$$

Output loop

$$V_{CC} - I_C R_C - V_{CE} = 0$$

$$V_{CE} = V_{CC} - I_C R_C$$

$$I_C = \beta I_B = \beta \left(\frac{V_{CC} - V_{BE}}{R_B} \right)$$



3.158 | Analog and Digital Electronics

Voltage drop across R_C can never be greater than V_{CC} .

$$I_C R_C < V_{CC} \Rightarrow I_C < \frac{V_{CC}}{R_C}$$

If I_C becomes greater than this value, the operating point will lie in saturation region.

$$\text{Stability factor} = S = 1 + \beta \left(\because \frac{\partial I_B}{\partial I_C} = 0 \right)$$

It's a simple circuit with few parts.

Operating point can be fixed anywhere in active region, by simply varying R_B .

I_C depends on β . β in turn unstable wrt temperature, this biasing in useful is switching and digital applications.

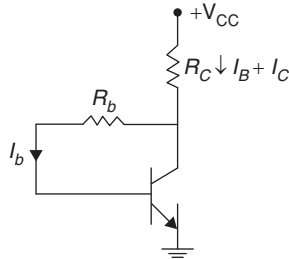
Collector to Base Bias Circuit

Input loop

$$V_{CC} - (I_B + I_C) R_C - R_B I_B - V_{BE} = 0$$

$$\Rightarrow \frac{\partial I_B}{\partial I_C} = \frac{-R_C}{R_C + R_B}$$

$$I_B = \frac{I_C}{\beta}$$



$$\Rightarrow I_B = \frac{V_{CC} - V_{BE}}{(\beta + 1)R_C + R_B}$$

$$\therefore I_C = \frac{\beta(V_{CC} - V_{BE})}{(\beta + 1)R_C + R_B}$$

If ' β ' is very large ($I_B = 0$) then the approximate value of

$$I_C = \frac{V_{CC} - V_{BE}}{R_C}$$

KVL at output side:

$$V_{CC} - (I_C + I_B) R_C - V_{CE} = 0$$

$$\Rightarrow V_{CE} = V_{CC} - (I_C + I_B) R_C$$

If $(\beta + 1)R_C \gg R_B$, then $I_C = \frac{V_{CC} - V_{BE}}{R_C}$ independent of ' β '.

The feedback resistor R_B provides negative feedback for AC input consequently reduces the AC gain of the circuit.

$$\text{Stability factor } S = \frac{1 + \beta}{1 + \beta \left(\frac{R_C}{R_C + R_B} \right)}$$

Collector to base bias is having lesser stability factor than fixed bias. Thus it provides better stability.

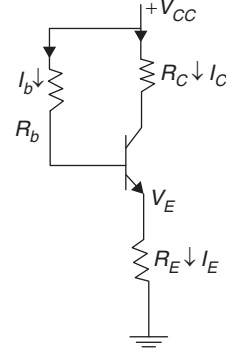
Emitter Feedback Bias

$$I_E = I_C + I_B$$

$$V_E = I_E R_E = (I_C + I_B) R_E$$

$$V_B = V_{BE} + (I_C + I_B) R_E$$

$$I_B = \frac{V_{CC} - V_B}{R_b}$$



Output loop

$$(I_C + I_B) R_E + R_C I_C - V_{CC} + V_{CE} = 0$$

$$\text{Stability factor } S = \frac{1 + \beta}{1 + \beta \left(\frac{R_E}{R_E + R_b} \right)}$$

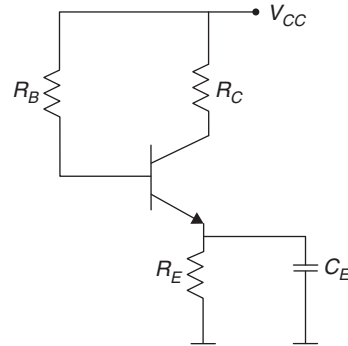
I_C can be made insensitive to β , if we choose $R_E \gg R_b$.

Advantages

1. Simplest biasing scheme
2. Better stability over fixed bias if $R_E \gg \frac{R_B}{(\beta + 1)}$

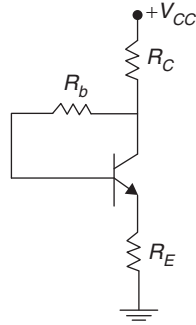
Disadvantages: The Resistor R_E provides a negative feed back for AC input consequently reduces the gain.

To increase the stability of the emitter feedback circuit, a bypass capacitor has been placed in parallel with R_E .



The purpose of bypass capacitor is to make $R_E = 0$ for AC input hence no gain reduction at the output of the circuit.

Collector-Emitter Feedback Bias



By applying KVL to the circuit.

Output loop

$$V_{CC} - (I_C + I_B) R_C - V_{CE} - R_E (I_C + I_B) = 0$$

Input loop

$$V_{CC} - (I_C + I_B) R_C - I_B R_B - V_{BE} - R_E (I_B + I_C) = 0$$

$$\text{Stability factor } S = \frac{1 + \beta}{1 + \beta(R_E + R_B) / (R_E + R_C + R_B)}$$

Self-bias, Emitter-bias, or Voltage-divide-bias

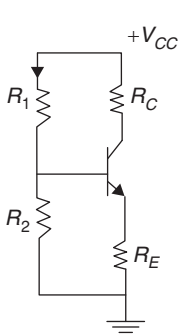


Figure 1 Self biasing circuit **Figure 2** Thevenine's equivalent circuit

$$V_{BB} = \frac{R_2 \cdot V_{CC}}{R_2 + R_1}, \quad R_B = \frac{R_2 R_1}{R_2 + R_1}$$

Input loop

$$V_{BB} = I_B R_B + V_{BE} + (I_B + I_C) R_E$$

Output loop

$$V_{CC} - R_C I_C + V_{CE} + (I_B + I_C) R_C$$

$$\text{Stability factor } S = \frac{1 + \beta}{1 + \beta \left(\frac{R_E}{R_E + R_B} \right)}$$

KVL at input side:

$$V_{BB} - I_B R_B - V_{BE} - (I_B + I_C) R_E = 0$$

$$I_C = \beta I_B$$

$$\Rightarrow I_B = \frac{V_{BB} - V_{BE}}{(\beta + 1) R_E + R_B} \Rightarrow I_C = \frac{\beta (V_{BB} - V_{BE})}{(\beta + 1) R_E + R_B}$$

KVL at out put side:

$$V_{CC} - I_C R_C - V_{CE} - (I_B + I_C) R_E = 0$$

$$\Rightarrow V_{CE} = V_{CC} - I_C R_C - (\beta + 1) I_B R_E$$

If ' β ' is very large, then approximate value of

$$I_C \approx \frac{V_{BE} - V_{BE}}{R_E}$$

$$\text{Where } V_{BB} = \frac{V_{CC} \cdot R_2}{R_1 + R_2}$$

$$R_B = R_1 \parallel R_2$$

If $(\beta + 1) R_E \gg R_B$, then I_C is Independent of ' β '

(i) Better stability over, all biasing schemes if

$$R_E \gg \frac{R_B}{(1 + \beta)}$$

(ii) Most of the amplifiers uses self-biasing scheme.

BIAS COMPENSATION

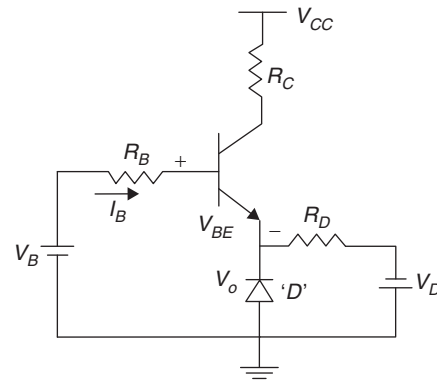
Compensation Techniques

$$I_C = f(I_{co}, V_{BE}, \beta)$$

I_{co} (reverse saturation current), V_{BE} and β are temperature dependent parameters. Hence to stabilize the circuit against the variation in temperature, i.e., (to make I_C independent of I_{co} , V_{BE} , β) compensation techniques are used.

1. Reverse saturation current doubles for every 10°C rise in temperature.
2. V_{BE} decreases for 7.5 mv for 1°C rise in temperature.

Compensation for V_{BE}

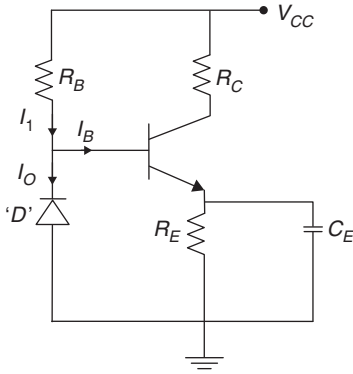


If the value of V_D and R_D are designed such that the voltage across the diode is V_{BE} from p-n side, I_B is $V_B - I_B R_B - V_{BE} + V_{BE} = 0$

$$I_B = \frac{V_B}{R_B} \text{ gives } I_C = \frac{\beta V_B}{R_B} \text{ independent of } V_{BE}$$

V_{BE} tracks V_0 with respect to temperature, so I_C will be insensitive to variations in V_{BE} .

Compensation for I_{co}



Let us assume that the transistor and the diode are made up of same material. Hence I_{co} is same for both

$$\therefore I_C = \beta I_B + (1 + \beta) I_{co}$$

$$I_C = \beta (I_1 - I_0) + (1 + \beta) I_{co} \quad (\because \text{from the figure})$$

If ' β ' is assumed to be so large and $I_0 = I_{co}$

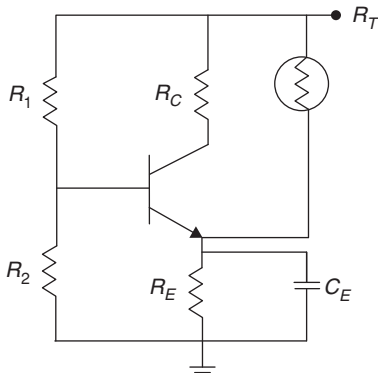
$$\Rightarrow \beta + 1 \approx \beta$$

$$I_C = \beta I_1 - \beta I_0 + \beta I_{co}$$

$I_C = \beta I_1$ which is independent of reverse saturation current.

If the diode and transistor are the same type of material, the reverse, saturation current of diode will increase with temperature at the same rate as the transistor collector saturation current I_{co} .

Thermistor compensation

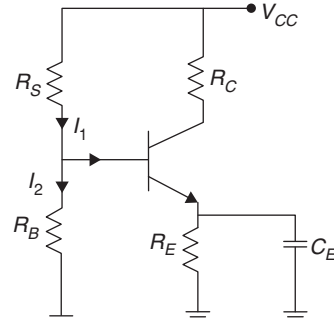


The thermistor has a negative temperature coefficient. Its resistance decreases exponentially with increase in temperature.

As T rises, R_T decreases, and the current fed through R_T into R_B increase. Since the voltage drop across R_E is in the

direction to reverse-bias the transistor. The temperature sensitivity of R_T acts so as to tend to compensate the increase in I_C due to temperature.

Sensistor compensation



R_s : sensistor

Sensistor is having a positive temperature coefficient of resistance whose resistance increases, as temperature increases, (as the collector current is increasing). Hence the current through sensistor decreases.

$$I_B = I_1 - I_2$$

I_1 decreases I_B also starts decreasing.

Since, $I_C = \beta I_B$ so the collector current is in control thus providing a better stability.

THERMAL RUN AWAY

Power dissipated at collector causes self heating, as a consequence junction temperature rises, and this in turn increase collector current, with a subsequent increase in power dissipation, if this phenomenon (referred to as thermal run away) continues, it may result in permanently damaging the transistor.

Thermal Resistance

It is found that steady state temperature rise at the collector junction is proportional to the power dissipated at the junction.

$$\Delta T = T_J - T_A = \theta P_D$$

T_J = Junction temperature

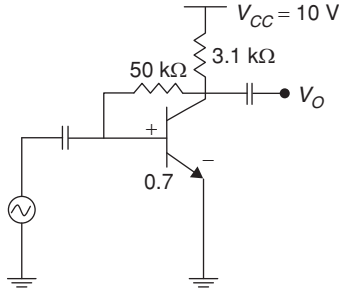
T_A = Ambient temperature

P_D = Power dissipated at collector junction

θ = Thermal resistance

The required condition for thermal stability is the rate at which heat is released must not exceed the rate at which the heat can be dissipated $\frac{\partial P_C}{\partial T_J} < \frac{\partial P_D}{\partial T_J} \Rightarrow \frac{\partial P_C}{\partial T_J} < \frac{1}{\theta}$ is the condition to avoid thermal runaway.

Example 2: Find the DC collector current if $V_{BE} = 0.7$ V and ' β ' is considered as very large



- (A) 2 mA (B) 4 mA
(C) 5 mA (D) 3 mA

Solution: (D)

$$I_C = \frac{\beta(V_{CC} - V_{BE})}{(\beta + 1)R_C + R_B}$$

As ' β ' is large

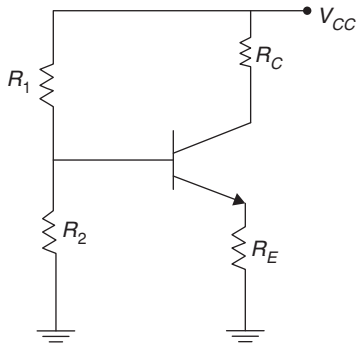
$$(\beta + 1)R_C \approx \beta R_C \gg R_B$$

$$I_C \approx \frac{V_{CC} - V_{BE}}{R_C}$$

$$= \frac{10 - 0.7}{3.1 \text{ k}\Omega}$$

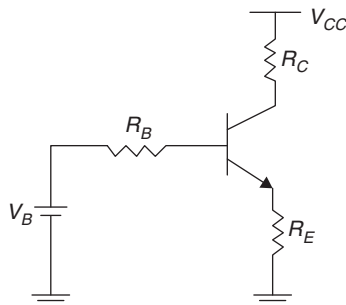
$$I_C = 3 \text{ mA.}$$

Example 3: A common emitter amplifier has a potential Divider bias using $V_{cc} = 20 \text{ V}$, $R_1 = R_2 = 6.2 \text{ k}\Omega$ and $V_{BE} = 0.7 \text{ V}$, β is assumed to be so large then, the operating point is (given R_C as $1 \text{ k}\Omega$ and R_E as $2 \text{ k}\Omega$)



- (A) (4.65 mA and 6.05 V) (B) (3 mA and 12 V)
(C) (9 mA and 6 V) (D) (9 ma and 14 V)

Solution: (A)



$$V_{BB} = \frac{V_{CC} \cdot R_2}{R_1 + R_2} = 10 \text{ V}$$

$$R_B = R_1 \parallel R_2 = 3.1 \text{ k}\Omega$$

$$I_C = \frac{\beta(V_{BB} - V_{BE})}{(\beta + 1)R_E + R_B}$$

As ' β ' is very large, i.e., $(\beta + 1)R_E \gg R_B$

$$\therefore I_C \approx \frac{V_{BB} - V_{BE}}{R_E}$$

$$I_C = \frac{10 - 0.7}{3.1 \text{ k}\Omega}$$

$$I_C = 4.65 \text{ mA}$$

Apply KVL at output side

$$V_{CEQ} = V_{cc} - I_{CQ}R_C - I_E R_E \text{ as } \beta \text{ is large } I_E \approx I_{CQ}$$

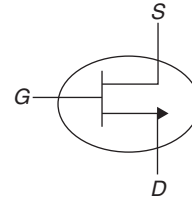
$$\therefore V_{CEQ} = V_{cc} - I_{CQ} [R_C + R_E]$$

$$= 20 - (4.65 \text{ mA}) (1 + 2 \text{ k}\Omega)$$

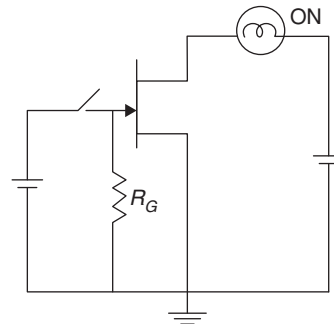
$$V_{CEQ} = 6.05 \text{ V.}$$

BIASING THE FET

Field effect transistor (FET) is a voltage controlled device having 3 terminals gate, source and drain.



FET is a symmetrical device (i.e., source and drain are interchangeable). FET acts as a better switch over BJT



For JFET and depletion mode MOSFET'S Shockley's equation is valid. R_G is called the bleeder resistor, FET is ON when input circuit is open

$$\therefore I_G = 0$$

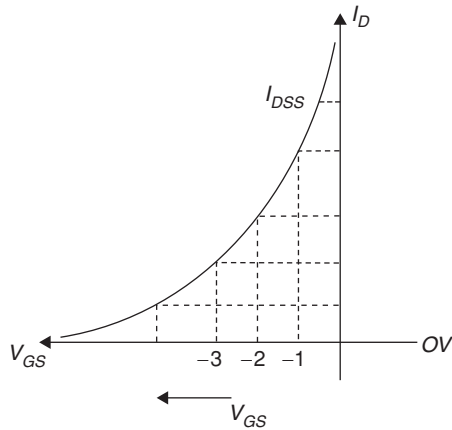


Figure 3 Transfer characteristics

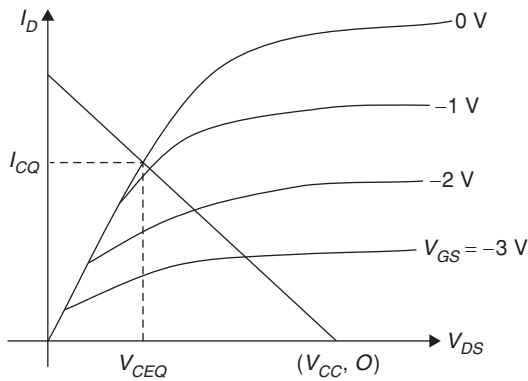


Figure 4 Output characteristics

Transfer characteristics are governed by the equation

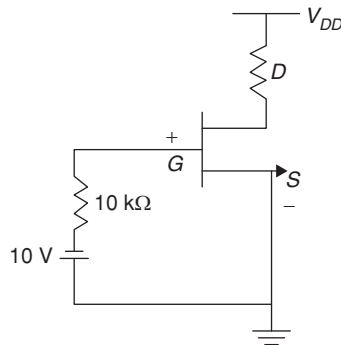
$$I_D = I_{DSS} \left[1 - \frac{V_{GS}}{V_P} \right]^2$$

When I_D = drain current

$I_D = I_{DSS}$ when $V_{GS} = 0$, i.e., drain saturation current

V_P = pinch off voltage

Example 4: Find I_D , V_{GS} for the given circuit assuming $V_{DD} = 30$ V, $V_P = -5$ V, $I_{DSS} = 30$ mA.



- (A) 0.27 A, 10 V
(B) 0.27 A, 20 V
(C) 0.135 A, 10 V
(D) 0.27 A, -10 V

Solution: (D)

$$I_G = 0 \text{ A}$$

Apply KVL at input side gives

$$-10 - V_{GS} - 0 (10 \text{ k}) = 0$$

$$V_{GS} = -10 \text{ V}$$

$$I_D = I_{DSS} \left[1 - \frac{V_{GS}}{V_P} \right]^2$$

$$= 30 \text{ mA} \left[1 + \frac{10}{5} \right]^2$$

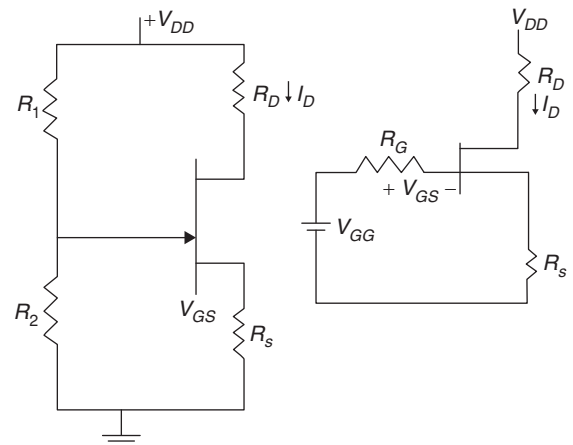
$$= 270 \text{ mA}$$

$$I_D = 0.27 \text{ A.}$$

In MOS circuits biasing schemes control deviations in the operating point caused by fabrication variations in the Threshold Voltage V_T and transconductance (processing) parameter k . Both IC and discrete-component JFET circuits are biased so that the effects of unit-to-unit variations in the pinch off voltage V_P and zero bias drain saturation current I_{DSS} are controlled.

BJT	FET
(i) Current-controlled device	(i) Voltage-controlled device
(ii) Apply KVL at Input gives I_B	(ii) $I_G = 0 \text{ A}$
(iii) $I_C = \beta I_B$	(iii) $I_D = I_{DSS} \left[1 - \frac{V_{GS}}{V_P} \right]^2$
(iv) Not symmetrical	(iv) Symmetrical device (source and drain are interchangeable)

Four Resistor Bias Circuit



$$V_{GG} = \frac{R_2}{R_1 + R_2} \cdot V_{DD}$$

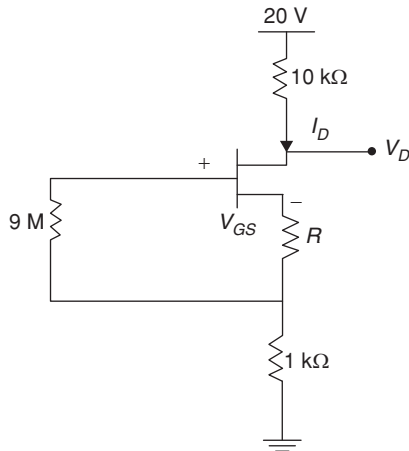
$$R_G = R_1 \parallel R_2 = \frac{R_1 R_2}{R_1 + R_2}, I_s = I_D$$

By KVL for the gate loop $-V_{GG} + V_{GS} + I_D R_S = 0$, by KVL for drain and source loop

$$-V_{DD} + R_D I_D + V_{DS} + R_S I_D = 0$$

In this analysis $I_G = 0$ was assumed, however the small reverse saturation current I_{GSS} exists in the gate loop. The resistance R_G is selected to be as large as it is Feasible while maintaining the voltage drop ($I_{GSS} R_G \ll V_{GG}$) at a negligible value.

Example 5: Find the value of resistor 'R' if the drain to ground voltage = 0 given $I_{DSS} = 50$ mA, $V_p = -6$ V.



- (A) 1.2 kΩ (B) 1.4 kΩ
(C) 1.3 kΩ (D) 1.5 kΩ

Solution: (B)

$$I_G = 0 \text{ A}$$

$$I_D = \frac{20 - V_D}{10 \text{ k}}$$

$$I_D = \frac{20 - 0}{10 \text{ k}} \approx 2 \text{ mA}$$

$$I_D = I_S = 2 \text{ mA}$$

$$I_D = I_{DSS} \left[1 - \frac{V_{GS}}{V_P} \right]^2$$

$$2 \text{ mA} = 50 \text{ mA} \left[1 + \frac{V_{GS}}{6} \right]^2$$

$$\Rightarrow 1 + \frac{V_{GS}}{6} = \frac{1}{5}$$

$$\Rightarrow V_{GS} = -4.8 \text{ V}$$

KVL at input gives

$$-V_{GS} - I_D [R + 1 \text{ k}\Omega] = 0$$

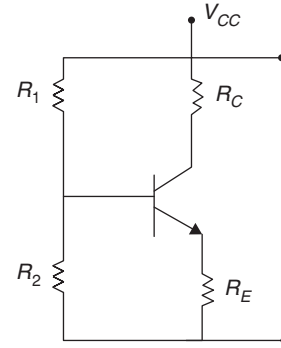
$$\Rightarrow 4.8 = I_D [R + 1 \text{ k}\Omega]$$

$$\Rightarrow 4.8 = 2 \text{ mA} [R + 1 \text{ k}\Omega]$$

$$\Rightarrow R = 1.4 \text{ k}\Omega.$$

Solved Examples

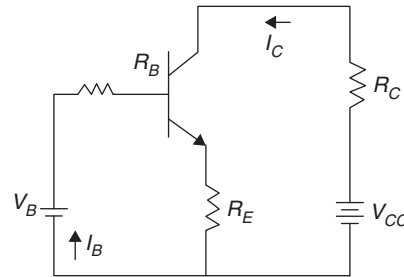
Example 1: A common emitter amplifier has a potential divider bias using $V_{CC} = 12$ V. If $R_C = 4 \text{ k}\Omega$, $R_E = 1 \text{ k}\Omega$, $R_1 = 20 \text{ k}\Omega$, $R_2 = 5 \text{ k}\Omega$, $V_{BE} = 0.6$ V, $\beta = 100$, then, the operating point is _____.



- (A) 5 V and 1 mA (B) 4 V and 1.4 mA
(C) 5.14 V and 1.2 mA (D) 3.41 V and 1.71 mA

Solution (D)

$$V_B = \frac{R_2}{R_1 + R_2} \times V_{CC} = \frac{5}{20 + 5} \times 12 = 2.4 \text{ V}$$



Writing KVL for the base emitter loop

$$V_B = I_B \cdot R_B + V_{BE} + (I_B + I_C) R_E$$

$$R_B = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{20 \times 5}{20 + 5} = 4 \text{ k}\Omega, I_B = \frac{I_C}{\beta}$$

$$2.4 = \frac{I_C}{100} \times 4 + 0.6 + \left(\frac{I_C}{100} + I_C \right) \times 1$$

$$1.8 = \frac{21}{20} \cdot I_C \Rightarrow I_C = 1.714 \text{ mA}$$

Writing KVL for the collector loop

$$V_{CC} = I_C \cdot R_C + V_{CE} + (I_C + I_B) R_E$$

$$12 = 1.714 \times 4 + V_{CE} + \left(1.714 + \frac{1.714}{100} \right) \times 1$$

$$V_{CE} = 3.41 \text{ V}$$

Example 2: When β is doubled, what are the operating point and stability factor in the previous problem?

- (A) 1.756 mA, 3.21 V and 4.9
(B) 1.71 mA, 3.14 V and 4.9
(C) 1.71 mA, 3.21 V and 4.81
(D) 1.756 mA, 3.21 V and 4.81

3.164 | Analog and Digital Electronics

Solution: (A)

$$V_B = 2.4 \text{ V}, R_B = 4 \text{ k}\Omega, I_B = \frac{I_C}{\beta} = \frac{I_C}{200}$$

Writing KVL for the base emitter loop

$$V_B = I_B \cdot R_B + V_{BE} + (I_B + I_C)R_E$$

$$\begin{aligned} 2.4 &= \frac{I_C}{200} \times 4 + 0.6 + \left(\frac{I_C}{200} + I_C \right) \times 1 \\ &= \frac{5}{200} I_C + I_C + 0.6 \end{aligned}$$

$$1.8 = 1.025 I_C \Rightarrow I_C = 1.756 \text{ mA}$$

Writing KVL for the collector loop

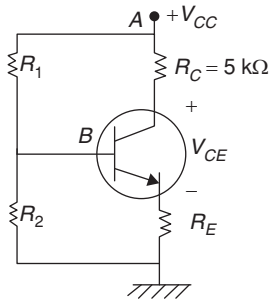
$$V_{CC} = I_C + R_C + V_{CE} + (I_C + I_B)R_E$$

$$12 = 1.756 \times 4 + V_{CE} + \left(\frac{1.756}{200} + I_C \right) \times 1$$

$$V_{CE} = 3.21 \text{ V}$$

$$S_1 = (\beta + 1) \frac{1'}{1 + \frac{\beta R_E}{R_B + R_E}} = \frac{201}{1 + \frac{200}{4 + 1}} = 4.9024.$$

Example 3: A silicon transistor with $\beta = 100$ is to be used in the self biasing circuit, shown in figure such that the quiescent point corresponds to $V_{CE} = 10 \text{ V}$ and $I_C = 2 \text{ mA}$, find ' R_E ' if $V_{CC} = 24 \text{ V}$, $R_C = 5 \text{ k}\Omega$?



- (A) $2 \text{ k}\Omega$ (B) $1.98 \text{ k}\Omega$ (C) 980Ω (D) $R_1 || R_2$

Solution: (B)

By Applying KVL between V_{CC} and ground

$$V_{CC} = V_{RC} + V_{CE} + V_{RE}$$

$$= I_C \cdot R_C + V_{CE} + (I_B + I_C) R_E$$

$$24 \text{ V} = 2 \times 10^{-3} \times 5 \times 10^3 + 10 + \left(\frac{2 \times 10^{-3}}{100} + 2 \times 10^{-3} \right) \cdot R_E$$

$$\Rightarrow R_E = \frac{4}{2 \times 10^{-3} (1.01)} = 1.98 \text{ k}\Omega$$

Example 4: In the above question, it is desired to have $S \leq 3$, find the limiting value of R_1 and R_2 assuming $V_{BE(\text{active})} = 0.65 \text{ V}$.

- (A) $41.39 \text{ k}\Omega$ and $10.16 \text{ k}\Omega$
(B) $20.69 \text{ k}\Omega$ and $10.16 \text{ k}\Omega$

(C) $20.69 \text{ k}\Omega$ and $5.08 \text{ k}\Omega$

(D) $41.39 \text{ k}\Omega$ and $5.08 \text{ k}\Omega$

Solution: (C)

$$S = \frac{(\beta + 1)(R_B + R_E)}{R_B + R_E(\beta + 1)} = \frac{R_B + R_E}{R_E + \frac{R_B}{\beta + 1}}$$

$$3 = \frac{101(R_B + 1.98)}{R_B + 1.98(101)}$$

$$3R_B + 599.94 = 101R_B + 199.98$$

$$98 R_B = 3999.96 \Rightarrow R_B = 4.08 \text{ k}\Omega$$

$$R_B < 4.08 \text{ k}\Omega \text{ for } S \leq 3$$

$$R_B = \frac{R_1 R_2}{R_1 + R_2}, V_B = V_{CC} \cdot \frac{R_2}{R_1 + R_2}$$

By solving

$$R_1 = \frac{V_{CC} \cdot R_B}{V_B}, R_2 = \frac{R_1 V_B}{V_{CC} - V_B}$$

$$V_B = I_B \cdot R_B + V_{BE} + V_{RE}$$

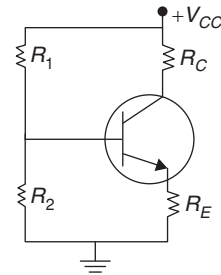
$$= 0.02 \times 10^{-3} \times 4.08 \times 10^3 + 0.65 + 4$$

$$= 4.7312 \text{ V}$$

$$R_1 = \frac{24 \times 4.08}{4.7312} = 20.69 \text{ k}\Omega$$

$$R_2 = \frac{20.69 \times 4.7312}{24 - 4.73} = 5.08 \text{ k}\Omega$$

Example 5: Consider the transistor circuit of figure where $V_{CC} = 24 \text{ V}$, $R_C = 5.6 \text{ k}\Omega$, $R_E = 1 \text{ k}\Omega$, $R_2 = 10 \text{ k}\Omega$, and $R_1 = 80 \text{ k}\Omega$, $\beta = 60$, $V_{BE} = 0.6 \text{ V}$, the transistor operates in the active region. The operating point of the transistor is



(A) 1.78 mA and 13.254 V

(B) 1.78 mA and 12.28 V

(C) 1.39 mA and 13.25 V

(D) 1.39 mA and 12.28 V

Solution: (B)

$$R_B = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{80 \times 10}{80 + 10} = 8.89 \text{ k}\Omega$$

The operating point can be found from the forward characteristics by writing the bias equation

$$I_B = \frac{I_C}{\beta} = \frac{I_C}{60}$$

$$V_B = I_B R_B + V_{BE} + I_E R_E$$

$$\frac{V_{CC} \cdot R_2}{R_1 + R_2} = I_B R_B + V_{BE} + (I_C + I_B) R_E$$

$$\frac{24 \times 10}{80 + 10} = I_B \times 8.89 + 0.6 + (60 + 1) I_B \times 1$$

$$2.67 = I_B (69.89) + 0.6$$

$$I_B = 0.0296 \text{ mA} \Rightarrow 29.6 \text{ } \mu\text{A}$$

$$I_C = 60 \times 29.6 \text{ } \mu\text{A} = 1.78 \text{ mA}$$

$$V_{CE} = V_{CC} - I_C R_C - (I_B + I_C) \cdot R_E = 12.23 \text{ V}$$

$$(I_{CQ}, V_{CEQ}) = (1.78 \text{ mA}, 12.23 \text{ V})$$

Example 6: The stability factor of the above transistor is

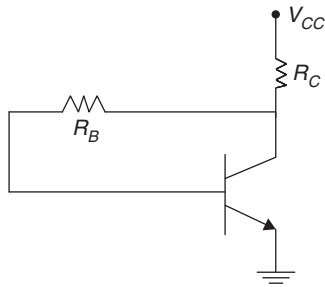
- (A) 1.99
(B) 3.13
(C) 6.31
(D) 8.63

Solution: (D)

$$S = \frac{R_B + R_E}{R_E + \frac{R_B}{\beta + 1}} = \frac{8.89 + 1}{1 + \frac{8.89}{61}} = 8.63$$

Example 7: The fixed bias circuit as shown is used as collector bias circuit, the value of R_B is?

Quiescent point (9.2 mA, 4.4 V), the transistor has DC current gain 115. $V_{BE} = 0.7 \text{ V}$, $V_{CC} = 9 \text{ V}$, $R_C = 500 \text{ } \Omega$.



- (A) 500 Ω (B) 45.75 k Ω
(C) 75.42 k Ω (D) 125.63 k Ω

Solution: (B)

$$V_{CC} = (I_B + I_C) R_C + I_B \cdot R_B + V_{BE}$$

$$9 = \left(\frac{9.2}{115} + 9.2 \right) \times 0.5 + \frac{9.2}{115} \times R_B + 0.7$$

$$R_B = \frac{3.66}{0.08} = 45.75 \text{ k}\Omega$$

Example 8: The stability factor and the thermal stability factor for the above circuit are

- (A) 62.81 and 0.525
(B) 51.71 and 0.446
(C) 42.36 and 0.345
(D) 33.81 and 0.824

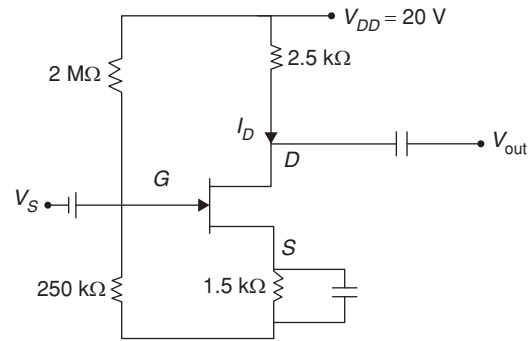
Solution: (B)

$$S = \frac{1 + h_{FE}}{1 + \frac{h_{FE} \cdot R_C}{R_C + R_B}} = \frac{1 + 115}{1 + \frac{115 \times 0.500}{0.5 + 45.75}} = 51.711$$

$$\text{Thermal stability factor } K = \frac{S}{1 + h_{FE}}$$

$$= \frac{51.7111}{116} = 0.446$$

Example 9: FET voltage divider bias is shown in given figure if $I_D = 4 \text{ mA}$, then V_{GS} and V_{DS} will be respectively



- (A) -3.78 V and 4 V
(B) 4 V and -3.78 V
(C) -3.78 V and -4 V
(D) -4 V and -3.78 V

Solution: (A)

$$V_G = \frac{20 \times 0.25}{2 + 0.25} = \frac{20}{9}$$

$$V_{GS} = V_G - I_D \cdot R_S = \frac{20}{9} - 4 \times 1.5 = -3.78 \text{ V}$$

$$V_{DS} = V_{DD} - I_D (R_S + R_D)$$

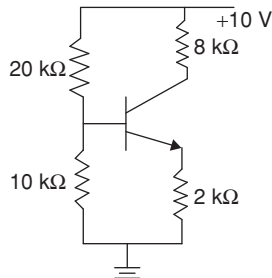
$$= 20 - 4 \times (1.5 + 2.5) = 4 \text{ V}$$

EXERCISES

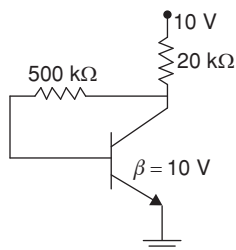
Practice Problems I

Directions for questions 1 to 25: Select the correct alternative from the given choices.

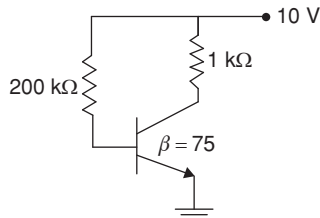
1. For the circuit showing in figure assume $\beta = 100$ for BJT, the transistor will be in



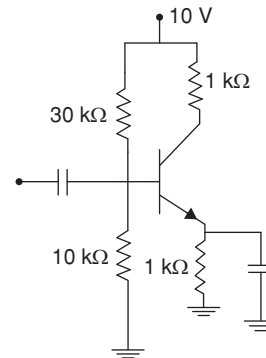
- (A) Cutoff region
(B) Active region
(C) Inverse active region
(D) Saturation region.
2. For the given biasing network, the stability factor 'S' is



- (A) 101
(B) 17.14
(C) 20.84
(D) 34
3. In a fixed bias circuit, $S = 51$ for $I_c = 2$ mA. Given $V_{cc} = 10$ V. The value of R_B is _____
- (A) 250 kΩ
(B) 250 Ω
(C) 25 kΩ
(D) 2.5 kΩ
4. In the given fixed bias circuit, $V_{CE(sat)} = 0$ V, the minimum value of I_B to saturate the transistor is _____

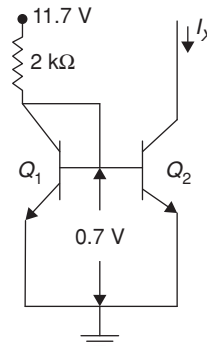


- (A) 10 mA
(B) 0.25 mA
(C) 0.133 mA
(D) 0.16 mA
5. For the given biasing network, β is taken as very large. Assume $V_{BE} = 0.2$ V, the value of I_E and V_{CE} are _____



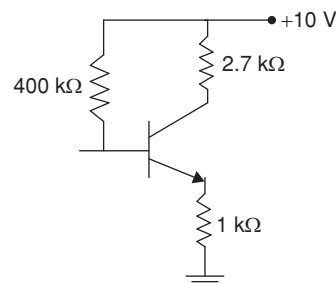
- (A) 2.3 mA and 0 V
(B) '0' mA and 10 V
(C) 10 mA and 5.4 V
(D) 2.3 mA and 5.4 V

6. A GE transistor is used in the self bias arrangement with $V_{CC} = 20$ V, $R_C = 2$ kΩ, $R_E = 500$ Ω. The Q-point is selected at $V_{CE} = 10$ V, $I_C = 5$ mA and $S = 12$. If $V_{BE} = 0.3$ V and $\beta = 60$, then the values of R_1 and R_2 are _____.
- (A) 40.65 kΩ and 8.24 kΩ
(B) 8.24 kΩ and 40.65 kΩ
(C) 40.65 kΩ and 18.6 kΩ
(D) 18.6 kΩ and 4.65 kΩ
7. In the BJT current mirror shown below, assume that the emitter area of Q_1 is double that of Q_2 . What is the value of I_x ?



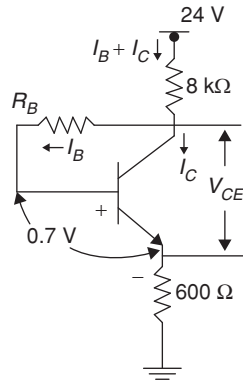
- (A) 5.5 mA
(B) 2.75 mA
(C) 6.2 mA
(D) 11 mA

8. The transistor has following parameters. $\beta = 50$ and $V_{BE} = 0.6$ V. If β is increased by 5% what is the change in V_{CE} ?



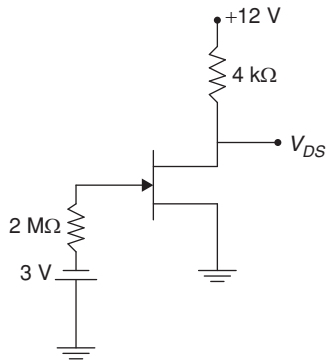
- (A) Increased by 4.57%
(B) Increased by 2.97%
(C) Decreased by 4.57%
(D) Decreased by 2.97%

9. A Si transistor with $\beta = 50$ at 50°C is used and it is desired that $V_{CE} = 8\text{ V}$. Consider I_{CO} varies from 0.5 to $10\text{ }\mu\text{A}$ when temperature changes from 50°C to 100°C .



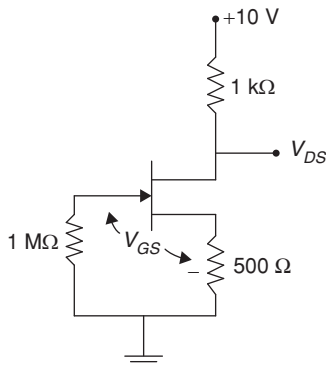
The values of R_B , stability factor, and I_c at 100°C are respectively _____

- (A) $200\text{ k}\Omega$, 51 and 2.5 mA
 (B) $20.5\text{ k}\Omega$, 50 and 1 mA
 (C) $200.5\text{ k}\Omega$, 16.7 and 1.98 mA
 (D) $2\text{ k}\Omega$, 10.4 and 1.75 mA
10. Given $I_{DSS} = 6\text{ mA}$ and $V_p = -4\text{ V}$ for the given FET biasing Network, the value of V_{DS} is _____



- (A) 12 V
 (B) 0 V
 (C) 10.5 V
 (D) 13.5 V

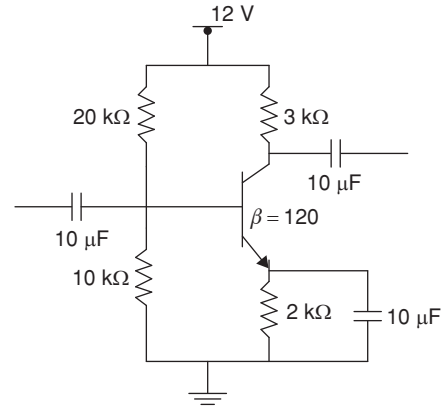
11. A self bias network with FET is given below; has $I_D = 5\text{ mA}$



What are the values of V_{GS} and V_{DS} ?

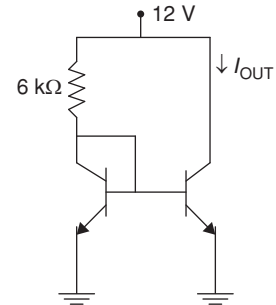
- (A) -2.5 V and -2.5
 (B) -2.5 V and 2.5 V
 (C) -5 V and 0 V
 (D) 0 V and -5 V

12. For the given biasing network, calculate I_B and V_{CE} (assume $V_{BE} = 0.7\text{ V}$)



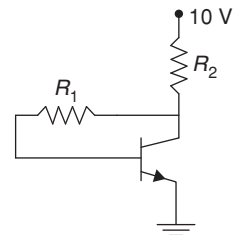
- (A) $13.4\text{ }\mu\text{A}$ and 3.95 V
 (B) $13.4\text{ }\mu\text{A}$ and 6 V
 (C) $1.34\text{ }\mu\text{A}$ and 3.95 V
 (D) $1.34\text{ }\mu\text{A}$ and 6 V

13. A constant current source using two matched npn transistors with $\beta = 100$ and $V_{BE} = 0.6\text{ V}$ is shown in the figure below. Calculate I_{out} .



- (A) 1.5 mA
 (B) 0.2 mA
 (C) 1.86 mA
 (D) 2 mA

14. A transistor with $V_{BE} = 0.7\text{ V}$ is shown. The values of R_1 and R_2 are such that the transistor is operating at $V_{CE} = 5\text{ V}$ and $I_C = 2\text{ mA}$ where $\beta = 100$. What is the operating point values for a transistor with $\beta = 200$.

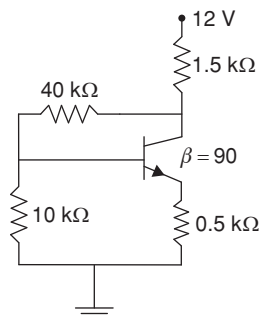


- (A) 3.78 V and 3.1 mA
 (B) 3.5 V and 2.6 mA
 (C) 5 V and 2.5 mA
 (D) 3.5 V and 1.25 mA

15. A transistor with $\beta = 100$ is used in CE mode. It is connected in collector to base bias mode with $\frac{R_B}{R_C} = 9$. Calculate the stability factor?

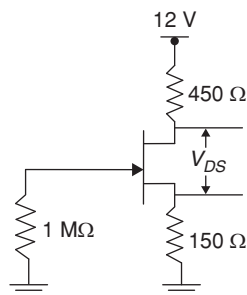
- (A) 99
 (B) 19.1
 (C) 20.86
 (D) 9.18

16. Calculate the stability factor for the given biasing network.



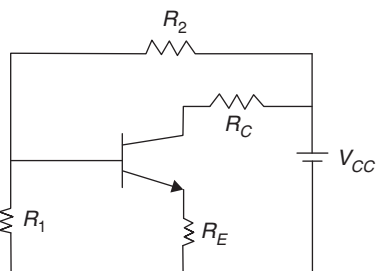
- (A) 10
(B) 6.2
(C) 4.8
(D) 1

17. For a given FET biasing network, $V_{DS} = \frac{1}{2}V_{DD}$, what are the values of I_D and V_{GS} ?



- (A) 1 mA and -1 V
(B) 10 mA and -1 V
(C) 1 mA and -1.5 V
(D) 10 mA and -1.5 V

18. The values of resistors R_C , R_E respectively, for $I_C = 5$ mA, $V_{CE} = 8$ V, $V_E = 6$ V and $S(I_{co}) = 10$, $h_{fe} = 200$ and $V_{CC} = 20$ V, are?



- (A) 1.194 kΩ and 1.2 kΩ
(B) 1.2 kΩ and 1.194 kΩ
(C) 10.3 kΩ and 17.43 kΩ
(D) 2.1 kΩ and 4.12 kΩ

19. The values of resistors R_1 and R_2 in the above circuit are
(A) 17.2 kΩ and 32.86 kΩ
(B) 12.8 kΩ and 23.6 kΩ
(C) 12.8 kΩ and 22.86 kΩ
(D) 17.2 kΩ, 32.86 kΩ

20. A pnp transistor uses potential divider bias $V_{BE} = -0.7$ V, and $\beta = 100$, the operating point is to be at $I_C = -1$ mA, and $V_{CE} = -5$ V, $V_{CC} = -20$ V, voltage drop across R_E is -3 V, for $SC(I_{co}) = 5$, the value of R_C and R_E are

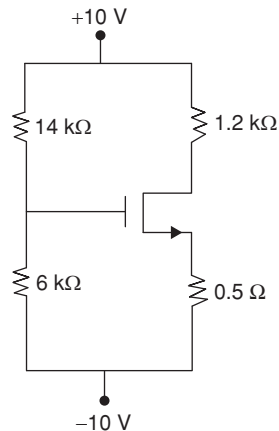
- (A) 12 kΩ and 3 kΩ
(B) 11.7 kΩ and 2.97 kΩ
(C) 11.7 kΩ and 3 kΩ
(D) 12 kΩ and 2.97 kΩ

21. The values of R_1 and R_2 (bias resistances) in the above problem are?

- (A) 4.2 kΩ and 12.4 kΩ
(B) 64.4 kΩ and 15.35 kΩ
(C) 42 kΩ and 12 kΩ
(D) 6.3 kΩ and 24 kΩ

Common Data for Questions for 22 to 24

22. In the current circuit, if the transistor parameters are $V_{th} = 2$ V, $k_n = 60 \mu\text{A/V}^2$, $\frac{W}{L} = 60$, and the transistor is in saturation, the value of V_{GS} is



- (A) 3.62 V
(B) -3.62 V
(C) 0.74 V
(D) -0.74 V

23. The value of I_D is

- (A) 12.5 mA
(B) 9.2 mA
(C) 6.3 mA
(D) 4.7 mA

24. The value of V_{DS} is

- (A) 12.95 V
(B) 11.9 V
(C) 9.3 V
(D) 7.5 V

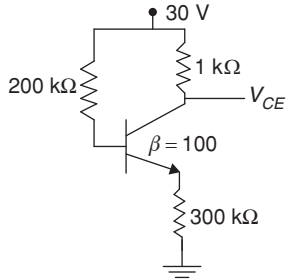
25. A BJT for which the manufacturer specifies $P_{D(\max)} = 125$ MW at 25°C free air temperature and max junction temperature is 150°C. The thermal resistance of BJT is _____.

- (A) 5°C/W
(B) 1°C/MW
(C) 1°C/W
(D) 10°C/MW

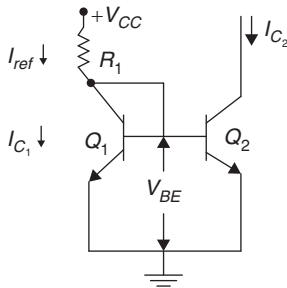
Practice Problems 2

Directions for questions 1 to 18: Select the correct alternative from the given choices.

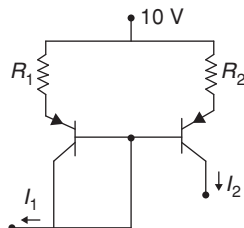
1. For the given biasing network, the collector to emitter voltage V_{CE} is _____ Volt.



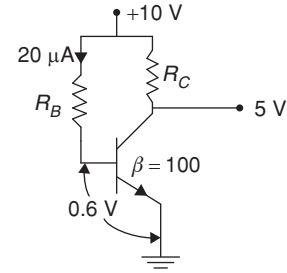
- (A) 0 V
(B) 30 V
(C) 15.2 V
(D) 13.1 V
2. A current mirror shown below, provide a 1.5 mA current with $V_{CC} = 12$ V. Assume $\beta = 150$ and $V_{BE} = 0.7$ V. What is R_1 .



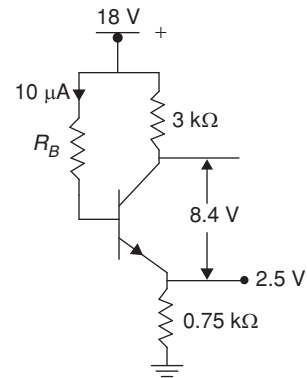
- (A) 9.25 kΩ
(B) 7.43 kΩ
(C) 7.53 kΩ
(D) 8.5 kΩ
3. In the figure given $I_1 = 10 \mu\text{A}$ and $I_2 = 40 \mu\text{A}$. What is the ratio R_1/R_2 .



- (A) 1
(B) 2
(C) $\frac{1}{2}$
(D) 4
4. In the given biasing network, the value of R_B and R_C are _____

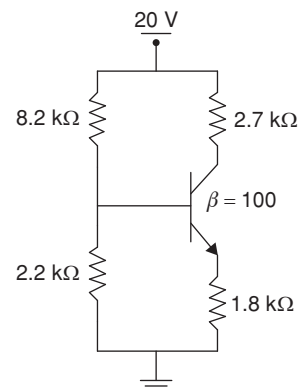


- (A) 470 kΩ and 2.5 kΩ
(B) 2.5 kΩ and 470 kΩ
(C) 4.7 kΩ and 250 Ω
(D) 470 kΩ and 25 kΩ
5. A transistor with emitter to base bias is given below.



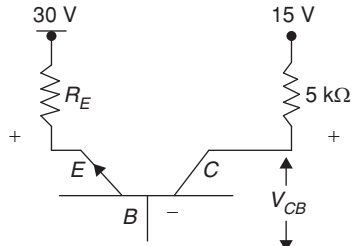
The values β of transistor, the base resistance R_B are

- (A) 100 and 155 kΩ
(B) 166 and 1.75 MΩ
(C) 333 and 1.55 MΩ
(D) 158 and 1.8 MΩ
6. The self bias Network is given below. Its stability factor (S) is _____



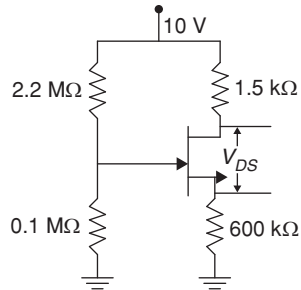
- (A) 101
(B) 9.5
(C) 58
(D) 2
7. The value of R_E which will saturate the transistor is nearly _____ kΩ.

3.170 | Analog and Digital Electronics



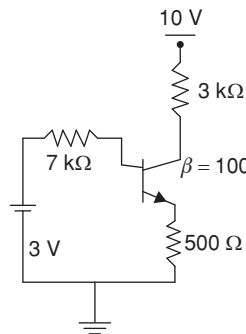
- (A) 5 (B) 25
(C) 10 (D) 20

8. Calculate I_D and V_{GS} for $V_{DS} = 2$ V



- (A) 4.6 mA and -1.85 V (B) 3.8 mA and -0.63 V
(C) 4.6 mA and -0.63 V (D) 3.8 mA and -1.85 V

9. Find the region of operation of transistor.

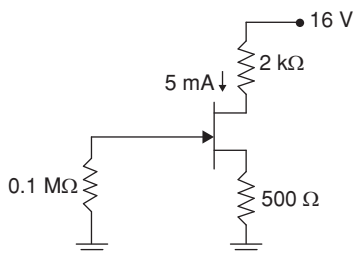


- (A) Saturation (B) Active
(C) Cut-off (D) None

10. A FET biasing network is used with following specifications.

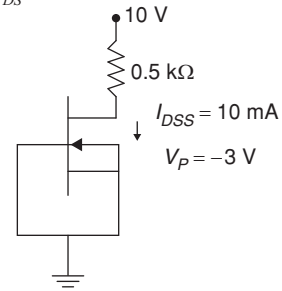
$$V_p = 5 \text{ V}, I_{DSS} = 8 \text{ mA}$$

Calculate g_m .



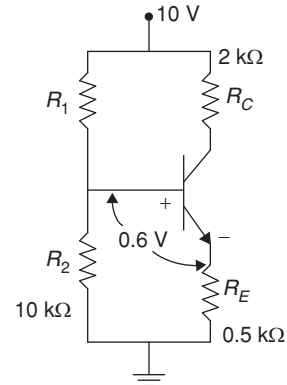
- (A) 1.6 mS (B) 2 mS
(C) 10 mS (D) 2.3 mS

11. The figure below shows a MOSFET biasing network. Calculate V_{DS} .



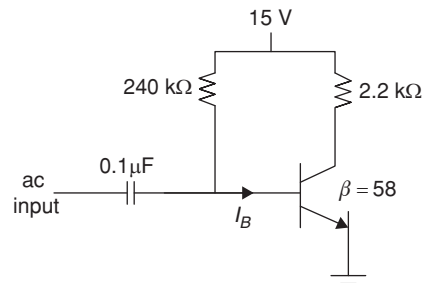
- (A) 5 V (B) 10 V
(C) 0 V (D) -5 V

12. A transistor with β is assumed to be very large is shown below. What is the value of R_1 required to make $I_C = 2.5$ mA.



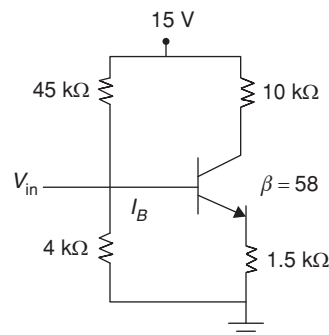
- (A) 2 kΩ (B) 10 kΩ
(C) 44 kΩ (D) 54 kΩ

13. I_B for a given circuit is



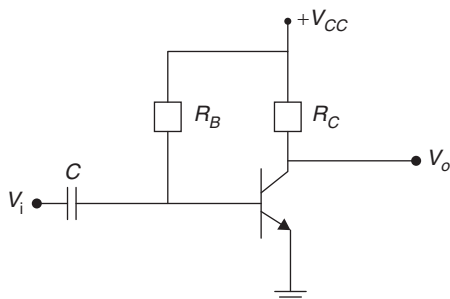
- (A) 59.6 μA (B) 49 μA
(C) 62.5 μA (D) 68.1 μA

14. The equivalent base resistance of the given circuit is



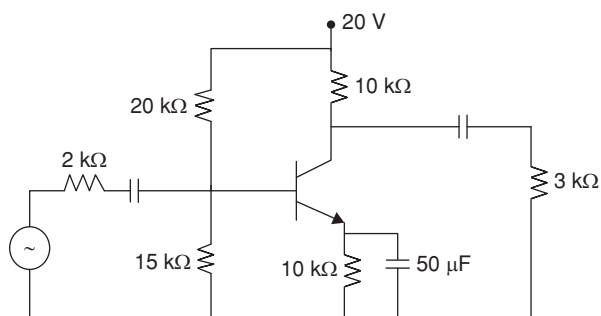
- (A) 49 k Ω (B) 45 k Ω
 (C) 4 k Ω (D) 3.67 k Ω

15. The circuit shown in figure is that of a fixed bias circuit. Estimate the values of the collector load resistor R_C and bias resistor R_B , if the quiescent collector current and voltage values are 10 mA and 5 V respectively. The transistor has a DC current gain of 110. V_{BE} is 0.7 V, $V_{CC} = 12$ V.



- (A) 500 Ω and 103.7 k Ω
 (B) 500 Ω and 124.3 k Ω
 (C) 700 Ω and 124.3 k Ω
 (D) 700 Ω and 103.7 k Ω
16. Calculate the thermal stability factor for the above circuit?
- (A) 111 (B) 1
 (C) 12 (D) 18

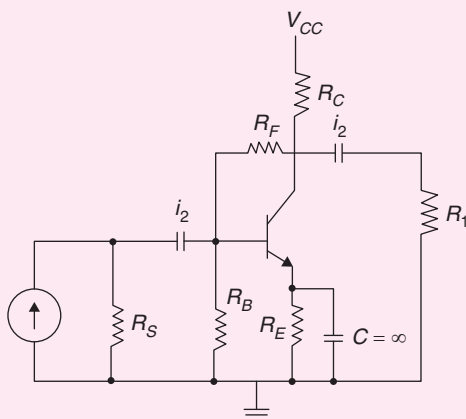
17. The circuit gives details for one stage of a transistor amplifier. Calculate the quiescent values of I_E , V_{CE} , $h_{fe} = 100$, $V_{BE} = 0$.



- (A) 0.857 mA and 2.959 V
 (B) 1.23 mA and 5.67 V
 (C) 1.11 mA and 7.69 V
 (D) -0.857 mA and 2.95 V
18. The thermal resistance of power transistor is 20°C/W. The ambient temperature is 40°C and junction temperature is 160°C. If $V_{CE} = 4.2$ V, the maximum the collector can carry without destruction is _____.
 (A) 1.2 A
 (B) 2.5 A
 (C) 1.66 A
 (D) 2 A

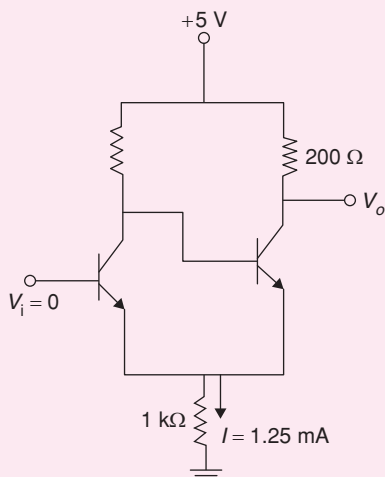
PREVIOUS YEARS' QUESTIONS

1. The feedback used in the circuit shown in figure can be classified as [2004]



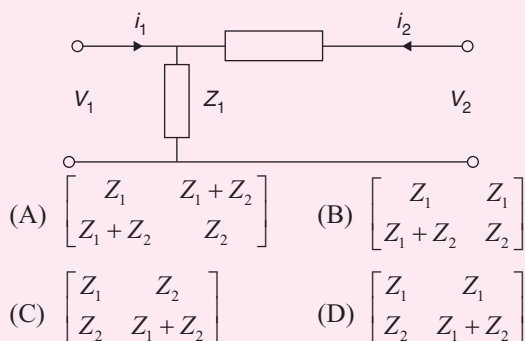
- (A) shunt-series feedback
 (B) shunt-shunt feedback

- (C) series-shunt feedback
 (D) series-series feedback
2. A bipolar junction transistor (BJT) is used as a power control switch by biasing it in the cut-off region (OFF state) or in the saturation region (ON state). In the ON state, for the BJT [2004]
 (A) Both the base-emitter and base-collector junctions are reverse biased.
 (B) The base-emitter junction is reverse biased, and the base-collector junction is forward biased.
 (C) The base-emitter junction is forward biased, and the base-collector junction is reverse biased.
 (D) Both the base-emitter and base-collector junctions are forward biased.
3. In the Schmitt trigger circuit shown in figure, if $V_{CE(sat)} = 0.1$ V, the output logic low level (V_{OL}) is [2004]

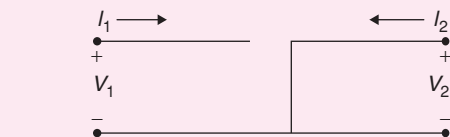


- (A) 1.25 V (B) 1.35 V
(C) 2.50 V (D) 5.00 V

4. For the two-port network shown in the Figure the Z-matrix given by [2005]



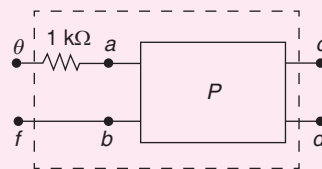
5. The parameter type and the matrix representation of the relevant two port parameters that describe the circuit shown are [2006]



- (A) z parameters, $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
(B) h parameters, $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
(C) h parameters, $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$
(D) z parameters, $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

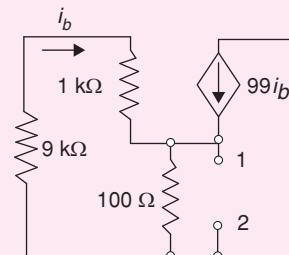
6. The two-port network P shown in the figure has ports 1 and 2, denoted by terminals (a, b) and (c, d) , respectively. It has an impedance matrix Z with parameters

denoted by z_{ij} . A 1Ω resistor is connected in series with the network at port 1 as shown in the figure. The impedance matrix of the modified two-port network (shown as a dashed box) is [2010]



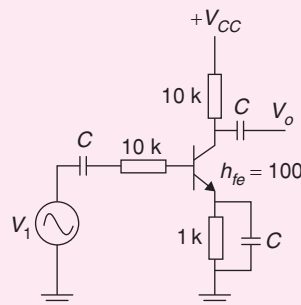
- (A) $\begin{bmatrix} z_{11} + 1 & z_{12} + 1 \\ z_{21} & z_{22} + 1 \end{bmatrix}$
(B) $\begin{bmatrix} z_{11} + 1 & z_{12} \\ z_{21} & z_{22} + 1 \end{bmatrix}$
(C) $\begin{bmatrix} z_{11} + 1 & z_{12} \\ z_{21} & z_{22} \end{bmatrix}$
(D) $\begin{bmatrix} z_{11} + 1 & z_{12} \\ z_{21} + 1 & z_{22} \end{bmatrix}$

7. The impedance looking into nodes 1 and 2 in the given circuit is [2012]



- (A) 50 Ω (B) 100 Ω
(C) 5 kΩ (D) 10.1 kΩ

8. The magnitude of the mid-point voltage gain of the circuit shown in figure is (assuming h_{fe} of the transistor to be 100) [2014]



- (A) 1
(B) 10
(C) 20
(D) 100

ANSWER KEYS**EXERCISES****Practice Problems 1**

- | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1. D | 2. C | 3. B | 4. C | 5. D | 6. A | 7. B | 8. D | 9. C | 10. C |
| 11. B | 12. A | 13. C | 14. B | 15. D | 16. C | 17. D | 18. B | 19. D | 20. D |
| 21. B | 22. A | 23. D | 24. B | 25. B | | | | | |

Practice Problems 2

- | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|
| 1. D | 2. B | 3. D | 4. A | 5. C | 6. D | 7. C | 8. D | 9. A | 10. A |
| 11. A | 12. C | 13. A | 14. D | 15. C | 16. A | 17. A | 18. C | | |

Previous Years' Questions

- | | | | | | | | |
|------|------|------|------|------|------|------|------|
| 1. B | 2. D | 3. B | 4. D | 5. C | 6. C | 7. A | 8. D |
|------|------|------|------|------|------|------|------|