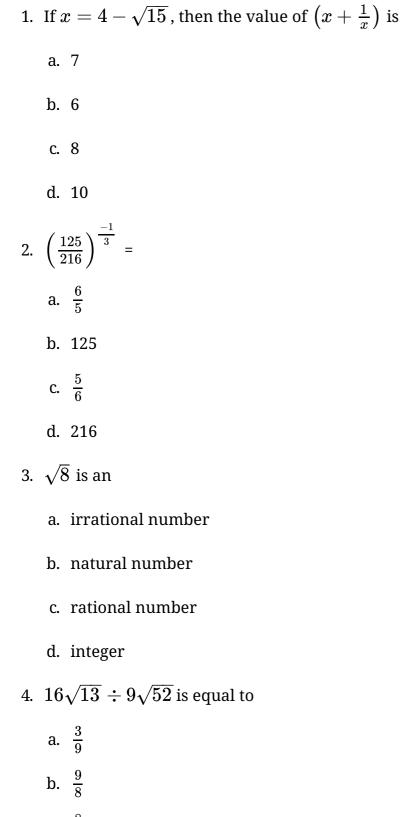
CBSE Test Paper 04 CH-1 Number Systems



c. $\frac{8}{9}$

- d. None of these
- 5. The value of $x^{a-b} imes x^{b-c} imes x^{c-a}$ is
 - a. 1
 - b. 2
 - с. х
 - d. 0
- 6. Fill in the blanks:
 - $\frac{5}{6}$ in the decimal form is _____.
- 7. Fill in the blanks:
 - Rational number $\frac{42}{100}$ in decimal form is _____.
- 8. Rationalise the denominator of $\frac{2+\sqrt{3}}{2-\sqrt{3}}$
- 9. Classify the following number as rational or irrational.0.3796
- 10. Prove $\sqrt{5}$ 2 is an irrational.
- 11. Is zero a rational number? Can you write it in the form $rac{p}{q}$, where p and q are integers and q
 eq 0?
- 12. Find the two rational numbers between $\frac{1}{2}$ and $\frac{1}{3}$
- 13. Prove that 1.101001000100001... is an irrational number.
- 14. Find the values of a and b in each of $rac{3-\sqrt{5}}{3+2\sqrt{5}}=a\sqrt{5}-rac{19}{11}$
- 15. If x = 2 + $\sqrt{3}$, find the value of x³ + $\frac{1}{x^3}$.

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Solution

1. (c) 8

Explanation:

$$x + \frac{1}{x} = \frac{x^2 + 1}{x}$$
Now, put x=4- $\sqrt{15}$

$$\Rightarrow \frac{(4 - \sqrt{15})^2 + 1}{4 - \sqrt{15}}$$

$$\Rightarrow \frac{16 + 15 - 8\sqrt{15} + 1}{4 - \sqrt{15}}$$

$$\Rightarrow \frac{32 - 8\sqrt{15}}{4 - \sqrt{15}}$$

$$\Rightarrow 8$$
2. (a) $\frac{6}{5}$
Explanation:

$$\left(\frac{125}{216}\right)^{\frac{-1}{3}} \Rightarrow \left(\frac{5}{6}\right)^{3 \times \frac{-1}{3}} \Rightarrow \left(\frac{5}{6}\right)^{-1} \Rightarrow \left(\frac{5}{6}\right)^{-1} \Rightarrow \frac{6}{5}$$

3. (a) irrational number

Explanation:

 $\sqrt{8}$ is an irrational number $\because \sqrt{4 imes 2} = 2\sqrt{2}$

4. (c) $\frac{8}{9}$ Explanation:

$$\begin{array}{l}
16\sqrt{13} \div 9\sqrt{52} \\
\frac{16\sqrt{13}}{9\sqrt{52}} = \frac{16}{9} \times \sqrt{\frac{13}{52}} = \frac{16}{9} \times \frac{1}{2} \\
= \frac{8}{9}
\end{array}$$

5. (a) 1

Explanation: a=b + c + b=c

$$egin{aligned} &x^{a-b} imes x^{b-c} imes x^{c-a}\ &\Rightarrow x^{a-b+b-c+c-a}\ &\Rightarrow x^0\ =&1 \end{aligned}$$

- 6. 0.8333
- 7. 0.<u>42</u>

8.
$$\frac{2+\sqrt{3}}{2-\sqrt{3}} = \frac{2+\sqrt{3}}{2-\sqrt{3}} \times \frac{2+\sqrt{3}}{2+\sqrt{3}}$$
$$= \frac{(2+\sqrt{3})^2}{(2)^2 - (\sqrt{3})^2} = \frac{4+3+4\sqrt{3}}{4-3}$$
$$= \frac{7+4\sqrt{3}}{1} = 7 + 4\sqrt{3}$$

- 9. .: The decimal expansion is terminating.
 - : 0.3796 is a rational number.
- 10. $\therefore \sqrt{5}$ is irrational and 2 is rational. $\therefore \sqrt{5}$ - 2 is irrational.

(:: The difference of a rational number and an irrational number is irrational.)

11. Consider the definition of a rational number.

A rational number is the one that can be written in the form of $\frac{p}{q}$, where p and q are integers and $q \neq 0$.

Zero can be written as $\frac{0}{1}$, $\frac{0}{2}$, $\frac{0}{3}$, $\frac{0}{4}$, $\frac{0}{5}$ So, we arrive at the conclusion that 0 can be written in form of $\frac{p}{q}$, where q is any integer. Therefore, zero is a rational number.

12. First rational number between
$$\frac{1}{2}$$
 and $\frac{1}{3}$

$$= \frac{1}{2} \left[\frac{1}{2} + \frac{1}{3} \right] \Rightarrow \frac{1}{2} \left[\frac{3+2}{6} \right] \Rightarrow \frac{5}{12}$$

$$= \frac{1}{2}, \frac{5}{12} \text{ and } \frac{1}{3}$$
Second rational number between $\frac{1}{2}$ and $\frac{1}{3}$

$$= \frac{1}{2} \left[\frac{1}{2} + \frac{5}{12} \right] \Rightarrow \frac{1}{2} \left[\frac{6+5}{12} \right] \Rightarrow \frac{11}{24}$$

$$=rac{5}{12} ext{ and } rac{11}{24}$$
 are two rational number between $rac{1}{2}$,and $rac{1}{3}$

13. We can observe that the number 1.101001000100001.... is a non-terminating on recurring decimal.

We know that non terminating and non-recurring decimals cannot be converted into $\frac{p}{q}$ form.

Therefore, we conclude that 1.101001000100001.... is an irrational number.

14. LHS =
$$\frac{3-\sqrt{5}}{3+2\sqrt{5}} = \frac{3-\sqrt{5}}{3+2\sqrt{5}} \times \frac{3-2\sqrt{5}}{3-2\sqrt{5}}$$

= $\frac{(3-\sqrt{5})(3-2\sqrt{5})}{(3)^2-(2\sqrt{5})^2}$
= $\frac{9-6\sqrt{5}-3\sqrt{5}+10}{9-20} = \frac{19-9\sqrt{5}}{-11}$
Now, $\frac{19-9\sqrt{5}}{-11} = a\sqrt{5} - \frac{19}{11}$
 $\Rightarrow \frac{-19}{11} + \frac{9}{11}\sqrt{5} = a\sqrt{5} - \frac{19}{11}$
 $\Rightarrow \frac{9}{11}\sqrt{5} - \frac{19}{11} = a\sqrt{5} - \frac{19}{11}$
Hence, $a = \frac{19}{11}$.

15. We have,

$$\begin{aligned} \mathbf{x} &= 2 + \sqrt{3} \\ \therefore \frac{1}{x} = \frac{1}{2 + \sqrt{3}} = \frac{1}{2 + \sqrt{3}} \times \frac{2 - \sqrt{3}}{2 - \sqrt{3}} \\ &= \frac{2 - \sqrt{3}}{(2 + \sqrt{3})(2 - \sqrt{3})} \\ &= \frac{2 - \sqrt{3}}{(2)^2 - (\sqrt{3})^2} \\ &= \frac{2 - \sqrt{3}}{4 - 3} = \frac{2 - \sqrt{3}}{1} \\ &\Rightarrow \frac{1}{x} = 2 - \sqrt{3} \\ &\text{Now, } \mathbf{x}^3 + \frac{1}{x^3} = (\mathbf{x} + \frac{1}{x}) \left[\mathbf{x}^2 - \mathbf{x} \times \frac{1}{x} + (\frac{1}{x})^2 \right] \\ &= (2 + \sqrt{3} + 2 - \sqrt{3}) \left[(2 + \sqrt{3})^2 - 1 + (2 - \sqrt{3})^2 \right] \\ &= 4 \left[(2)^2 + (\sqrt{3})^2 + 2 \times 2 \times \sqrt{3} - 1 + (2)^2 + (-\sqrt{3})^2 - 2 \times 2 \times \sqrt{3} \right] \\ &= 4 \left[4 + 3 + 4\sqrt{3} - 1 + 4 + 3 - 4\sqrt{3} \right] \\ &= 4 \left[13 \right] \\ &= 52 \end{aligned}$$