

# SETS

In Mathematics, Set theory was developed by **George Cantor** (1845 – 1918).

**Set:** A well defined collections of objects is called a **Set**.

Well defined means that

- (i) All the objects in the Set should have a common feature or property and
- (ii) It should be possible to decide whether any given objects belongs to the set or not.

We usually denote a set by capital letters and the elements of a set are represented by small letters.

**Ex:** Set of vowels in English language  $V = \{ a, e, i, o, u \}$

Set of even numbers  $E = \{ 2, 4, 6, 8, \dots \}$

Set of odd numbers  $O = \{ 1, 3, 5, 7, \dots \}$

Set of prime numbers  $P = \{ 2, 3, 5, 7, 11, 13, \dots \}$

Any element or object belonging to a set, then we use symbol ' $\in$ ' (belongs to), if it is not belonging to it is denoted by the Symbol ' $\notin$ ' (does not belongs to)

**Ex:** In Natural numbers Set  $N$ ,  $1 \in N$  and  $0 \notin N$

**Roaster Form:** All elements are written in order by separating commas and are enclosed with in curly brackets is called Roaster form. In the form elements should not repeated.

**Ex:** Set of prime numbers less than 13 is  $p = \{ 2, 3, 5, 7, 11 \}$

**Set Builder Form:** In set builder form, we use a symbol  $x$  (or any other symbol  $y, z$  etc.) for the element of the set. This is followed by a colon (or a vertical line), after which we write the characteristic property possessed within curly brackets.

**Ex:**  $P = \{ 2, 3, 5, 7, 11 \}$ . This is the set of all prime numbers less than 13. It can be represented in the set builders form as

$$P = \{ x: x \text{ is a prime numbers less than } 13 \}$$

**(Or)**

$$P = \{ x/x \text{ is a prime number less than } 13 \}$$

**Null Set:** A set which does not contain any element is called the empty set or the null set or a void set. It is denoted by  $\phi$  or  $\{ \}$

**Ex:**  $A = \{ x/ 1 < x < 2, x \text{ is a natural numbers} \}$

$$B = \{ x/ x^2 - 2 = 0 \text{ and } x \text{ is a rational number} \}$$

**Finite Set:** A set is called a finite set if it is possible to count the numbers of elements in it.

**Ex:**  $A = \{ x; x \in \mathbb{N} \text{ and } (x-1)(x-2) = 0 \} = \{ 1, 2 \}$

$$B = \{ x; x \text{ is a day in a week} \} = \{ \text{SUN, MON, TUS, WED, THU, FRI, SAT} \}$$

**Infinite Set:** A Set is called an infinite set if the number of cannot count the number of elements in it.

**Ex:**  $A = \{ x / x \in \mathbb{N} \text{ and } x \text{ is an odd number} \}$

$$= \{ 1, 3, 5, 7, 9, 11, \dots \}$$

$$B = \{ x/ x \text{ is a point on a straight line} \}$$

**Cardinal Number:** The number of elements in a Set is called the cardinal number of the set. If 'A' is a set then  $n(A)$  represents cardinal number.

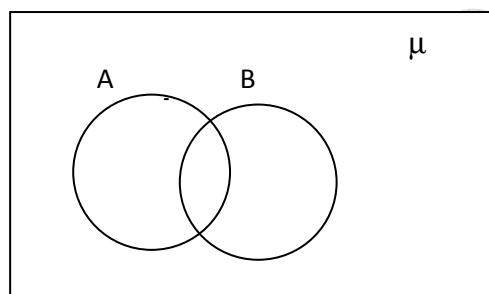
**Ex:** If  $A = \{ a, e, i, o, u \}$  then  $n(A) = 5$

If  $B = \{x; x \text{ is alter in the word INDIA}\}$

Then  $n(B) = 4$

$N(\phi) = 0$

**Universal Set:** Universal Set is denoted by ' $\mu$ ' or ' $U$ ' generally , universal set represented by rectangle.



**Subset:** If every element of a set A is also an element of set B, then the set A is said to be a subset of set B. It is represented as  $A \subset B$ .

**Ex:** If  $A = \{4, 8, 12\}$ ;  $B = \{2, 4, 6, 8, 10, 12, 14\}$  then

A is a subset of B (i.e.  $A \subset B$ )

- Every Set is a subset of itself ( $A \subset A$ )
- Empty Set is a subset of every set ( $\phi \subset A$ )
- If  $A \subset B$  and  $B \subset C$  then  $A \subset C$  (Transitive property)

**Equal Sets:** Two sets A and B are said to be 'equal' if every elements in A belongs to B and every elements in B belongs to A. If A and B are equal sets , then we write  $A = B$  .

**Ex:** The set of prime number less than 6,  $A = \{2, 3, 5\}$

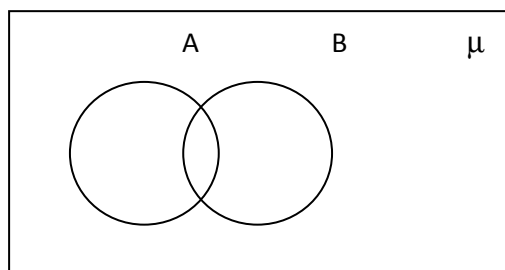
The prime factors of 30,  $B = \{2, 3, 5\}$

Since the elements of A are the same as the elements of B, therefore, A and B are equal.

- $A \subset B$  and  $B \subset A \Leftrightarrow A = B$  ( Ant symmetric property)

**Venn Diagrams:** Venn-Euler diagram or Simply Venn diagram is a way of representing the relationships between sets. These diagrams consist of rectangles and closed curves usually circles.

**Ex:**



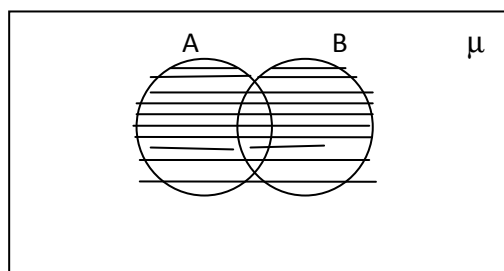
**Basic operations on Sets:** We know that arithmetic has operation of addition, subtraction and multiplication of numbers. Similarly in Sets, we define the operation of Union, Intersection and difference of Sets.

**Union of Sets:** The union of A and B is the Set which contains all the elements of A and also the elements of B and the common element being taken only once. The symbol 'U' is used to denote the union. Symbolically, we write  $A \cup B$  and read as 'A' union 'B'.

$$A \cup B = \{x/x \in A \text{ or } x \in B\}$$

**Ex:**  $A = \{1, 2, 3, 4, 5\}$  :  $B = \{2, 4, 6, 8, 10\}$

Then  $A \cup B = \{1, 2, 3, 4, 5, 6, 8, 10\}$



- $A \cup B = A$
- $A \cup \phi = A = \phi \cup A$  ( identity property)
- $A \cup \mu = \mu = \mu \cup A$
- If  $A \subset B$  then  $A \cup B = B$
- $A \cup B = B \cup A$  (Commutative property)

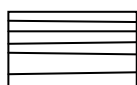
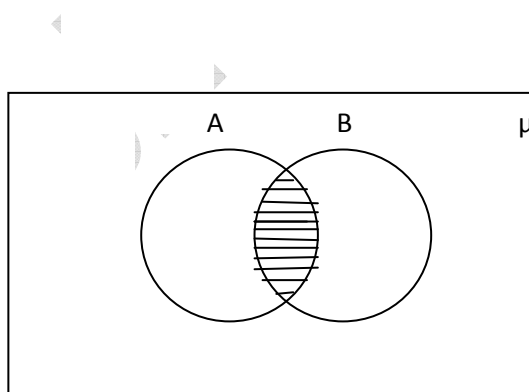
**Intersection of Sets:** The intersection of A and B is the Set in which the elements that are common to both A and B. The Symbol ' $\cap$ ' is used to denote the 'intersection'.

Symbolically we " $A \cap B$ " and read as " A intersection B".

$$A \cap B = \{ x / x \in A \text{ and } x \in B \}$$

**Ex:**  $A = \{ 1, 2, 3, 4, 5 \}$  and  $B = \{ 2, 4, 6, 8, 10 \}$

Then  $A \cap B = \{ 2, 4 \}$



Represents  $A \cap B$

- $A \cap B = A$
- $A \cap \phi = \phi = \phi \cap A$
- $A \cap \mu = A = \mu \cap A$  (identity property)
- If  $A \subset B$  then  $A \cap B = A$
- $A \cap B = B \cap A$  (Commutative property)

**Disjoint Sets:** If there are no common elements in A and B. Then the Sets are Known as disjoint sets.

If A, B are disjoint sets then  $A \cap B = \phi$

If  $A \cap B = \phi$  then  $n(A \cap B) = 0$

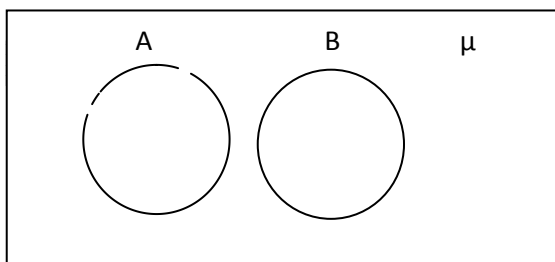
**Ex:**  $A = \{ 1, 3, 5, 7, \dots \} : B = \{ 2, 4, 6, 8, \dots \}$

Here A and B have no common elements

A and B are called disjoint Sets.

$\therefore$

i.e.  $A \cap B = \phi$



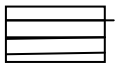
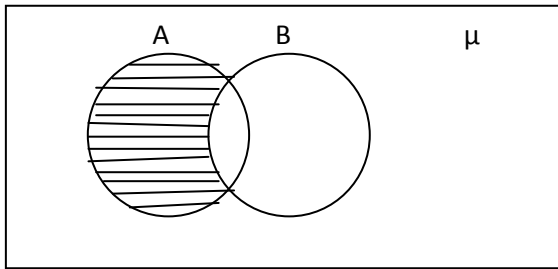
**Difference of Sets:** The difference of Sets A and B is the set of elements which belongs to A but do not belong to B. We denote the difference of A and B by  $A-B$  or simply “A minus B”

$$A - B = \{ x / x \in A \text{ and } x \notin B \}$$

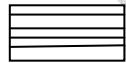
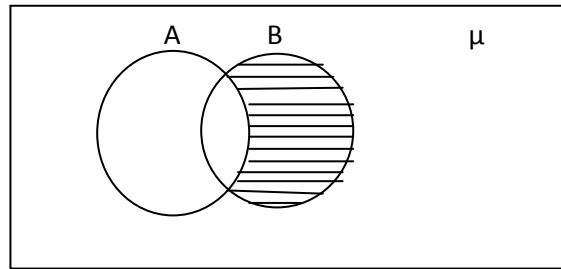
$$B - A = \{ x / x \in B \text{ and } x \notin A \}$$

**E**      **Ex:** If  $A = \{ 1, 2, 3, 4, 5 \}$  and  $B = \{ 4, 5, 6, 7 \}$  then

$$A - B = \{ 1, 2, 3 \}, \quad B - A = \{ 6, 7 \}$$



represents 'A - B'



represents B - A

- $A - B \neq B - A$
- $A - B$ ,  $B - A$  and  $A \cap B$  are disjoint Sets.
- $n(A \cup B) = n(A) + n(B) - n(A \cap B)$
- If A, B are disjoint sets then  $n(A \cup B) = n(A) + n(B)$

## Essay type Questions

**(1) Write the following sets in roster form. (Communication)**

- (i)  $A = \{ x : x \text{ is a two digital natural number such that the sum of its digits is } 8 \}$**
- (ii)  $B = \{ x : x \text{ is a natural number and } x^2 < 40 \}$**
- (iii)  $C = \{ x : x \text{ is a prime number which is a divisor of } 60 \}$**
- (iv)  $D = \{ x : x \text{ is an integers , } x^2 = 4 \}$**

**Solution:** Set builder form:

- (i).  $A = \{ x : x \text{ is a two digital natural number such that the sum of its digits is } 8 \}$

Roster form:

$$A = \{ 17, 26, 35, 44, 53, 62, 71, 80 \}$$

- (ii). Set builder form:

$$B = \{ x : x \text{ is a natural number and } x^2 < 40 \}$$

Roster form:

$$B = \{ 1, 2, 3, 4, 5, 6 \}$$

- (iii). Set builder form:

$$C = \{ x : x \text{ is a prime number which is a divisor of } 60 \}$$

Roster form:

$$C = \{ 2, 3, 5 \}$$

- (iv). Set builder form:

$$D = \{ x : x \text{ is an integers , } x^2 = 4 \}$$

Roster form:

$$D = \{ -2, 2 \}$$

(2). Write the following sets in the sets -builders form. (Communication)

(i)  $A = \{1, 2, 3, 4, 5\}$

(ii)  $B = \{5, 25, 125, 625\}$

(iii)  $C = \{1, 2, 3, 6, 7, 14, 21, 42\}$

(iv)  $D = \{1, 4, 9, \dots, 100\}$

**Solution:**

(i). Roster form:

$$A = \{1, 2, 3, 4, 5\}$$

Set builder form

$$A = \{x : x \text{ is a natural number } x < 6\}$$

(ii). Roster form:

$$B = \{5, 25, 125, 625\}$$

Set builder form:

$$B = \{x : x \text{ is a natural number and power of } 5, x < 5\}$$

(Or)

$$B = \{5^x : x \in \mathbb{N}, x \leq 4\}$$

(iii). Roster form:

$$C = \{1, 2, 3, 6, 7, 14, 21, 42\}$$

Set builder form:

$$C = \{x : x \text{ is a natural number which divides } 42\}$$

(iv). Roster form:

$$D = \{ 1, 4, 9, \dots, 100 \}$$

Set builder form:

$$D = \{ x: x \text{ is a square of a natural number and not greater than } 10 \}$$

(or)

$$= \{ x^2 : x \in \mathbb{N}, x \leq 10 \}$$

**(3). State which of the following Sets are finite or infinite. (Reasoning proof)**

**(i).  $\{x: x \in \mathbb{N} \text{ and } (x-1)(x-2) = 0\}$**

**(ii).  $\{x: x \in \mathbb{N} \text{ and } x < 100\}$**

**(iii).  $\{x: x \text{ is a straight line which is parallel to X – Axis}\}$**

**(iv). The Set of circles passing through the origin (0 ,0)**

**Solution:**

(i).  $\{x: x \in \mathbb{N} \text{ and } (x-1)(x-2) = 0\}$

x can take the values 1 or 2 in the given case . The set is  $\{ 1, 2 \}$  , Hence it is finite.

(ii).  $\{x: x \in \mathbb{N} \text{ and } x < 100\}$

$= \{ 1, 2, \dots, 100\}$ , The number of elements in this Set are countable . Hence it is finite.

(iii).  $\{x: x \text{ is a straight line which is parallel to } X - \text{Axis}\}$

Infinite straight lines are parallel to  $X - \text{axis}$

Hence, it is infinite Set

(iv). The Set of circles passing through the origin  $(0, 0)$

Infinite circles are passing through the origin  $(0, 0)$

Hence it is infinite Set

**(4) . Let  $A = \{3, 4, 5, 6, 7\}$ , and  $B = \{1, 6, 7, 8, 9\}$  Find**

**(i) .  $A \cup B$     (ii)  $A \cap B$     (iii)  $A - B$     (iv)  $B - A$     (Problem Solving )**

**Solution:**    Given  $A = \{3, 4, 5, 6, 7\}$ ,     $B = \{1, 6, 7, 8, 9\}$

(i)  $A \cup B = \{3, 4, 5, 6, 7, 8, 9\}$

(ii)  $A \cap B = \{6, 7\}$

(iii)  $A - B = \{3, 4, 5\}$

(iv)  $B - A = \{1, 8, 9\}$

(5) . (i) Illustrate  $A \cup B$  in Venn – diagrams where

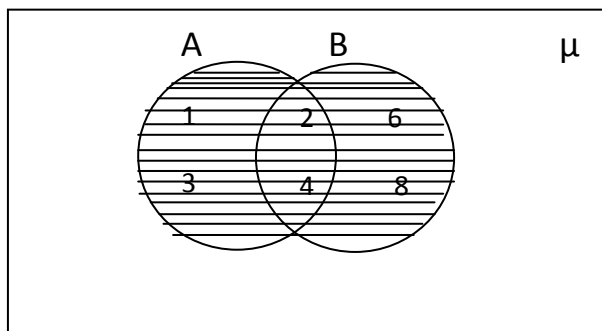
$$A = \{ 1, 2, 3, 4 \} \text{ and } B = \{ 2, 4, 6, 8 \}$$

(ii) Illustrate in the Venn –diagrams where

$$A = \{ 1, 2, 3 \} \text{ and } B = \{ 3, 4, 5 \} \quad (\text{visualization \& representation})$$

**Solution:** (i)  $A = \{ 1, 2, 3, 4 \}$

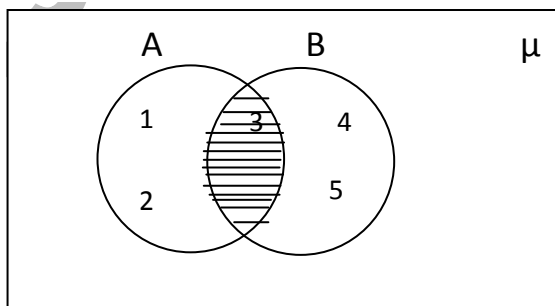
$$B = \{ 2, 4, 6, 8 \}$$



$$A \cup B = \{ 1, 2, 3, 4, 6, 8 \}$$

(iii)  $A = \{ 1, 2, 3 \}$

$$B = \{ 3, 4, 5 \}$$



$$A \cap B = \{ 3 \}$$

(6). If  $A = \{ 3, 4, 5, 6, 7 \}$  ,  $B = \{ 1, 6, 7, 8, 9 \}$  then find  $n(A)$ ,  $n(B)$ ,  $n(A \cap B)$  and  $n(A \cup B)$ . What do you observe ? (Reasoning Proof)

**Solution:**

$$A = \{ 3, 4, 5, 6, 7 \} , \quad n(A) = 5$$

$$B = \{ 1, 6, 7, 8, 9 \} \quad n(B) = 5$$

$$A \cup B = \{ 1, 3, 4, 5, 6, 7, 8, 9 \} \quad n(A \cup B) = 8$$

$$A \cap B = \{ 6, 7 \} \quad n(A \cap B) = 2$$

We observe that  $n(A \cup B) = n(A) + n(B) - n(A \cap B)$

(Or)

$$n(A \cap B) = n(A) + n(B) - n(A \cup B)$$

(Or)

$$n(A \cup B) + n(A \cap B) = n(A) + n(B)$$

(7). If  $A = \{ x: x \text{ is a natural number} \}$

$B = \{ x: x \text{ is an even natural number} \}$

$C = \{ x: x \text{ is an odd natural number} \}$

$D = \{ x: x \text{ is a prime number} \}$  Find  $A \cap B$ ,  $A \cap C$ ,  $A \cap D$ ,  $B \cap C$ ,

$B \cap D$ ,  $C \cap D$  (Problem solving)

**Solution:**  $A = \{ x: x \text{ is a natural number} \}$

$$= \{ 1, 2, 3, 4, \dots \}$$

$$B = \{ x: x \text{ is a even natural number } \}$$

$$= \{ 2, 4, 6, \dots \}$$

$$C = \{ x: x \text{ is a odd natural number } \}$$

$$= \{ 1, 3, 5, 7, \dots \}$$

$$D = \{ x: x \text{ is a prime number } \}$$

$$= \{ 2, 3, 5, 7, 11, 13, \dots \}$$

$$A \cap B = \{ 1, 2, 3, 4, \dots \} \cap \{ 2, 4, 6, \dots \} = \{ 2, 4, 6, \dots \} = B$$

$$A \cap C = \{ 1, 2, 3, 4, \dots \} \cap \{ 1, 3, 5, 7, \dots \} = \{ 1, 3, 5, 7, \dots \} = C$$

$$A \cap D = \{ 1, 2, 3, 4, \dots \} \cap \{ 2, 3, 5, 7, 11, 13, \dots \} = \{ 2, 3, 5, 7, \dots \} = D$$

$$B \cap C = \{ 2, 4, 6, \dots \} \cap \{ 1, 3, 5, 7, \dots \} = \{ \} = \phi$$

B and C are disjoint Sets

$$B \cap D = \{ 2, 4, 6, \dots \} \cap \{ 2, 3, 5, 7, 11, 13, \dots \} = \{ 2 \}$$

$$C \cap D = \{ 1, 3, 5, 7, \dots \} \cap \{ 2, 3, 5, 11, 13, \dots \} = \{ 3, 5, 7, 11, 13, \dots \}$$

**(8) . Using examples to show that  $A - B$ ,  $B - A$  and  $A \cap B$  are mutually disjoint Sets .**

**(Reasoning proof)**

**Solution:**

$$\text{Let } A = \{ 1, 2, 3, 4, 5 \}, \quad B = \{ 4, 5, 6, 7 \}$$

$$A \cap B = \{ 4, 5 \}$$

$$A - B = \{ 1, 2, 3 \}$$

$$B - A = \{ 6, 7 \}$$

We observe that the Sets  $A \cap B$ ,  $A - B$ ,  $B - A$  are mutually disjoint Sets.

## Short Answer Questions

### (1) Match roster forms with the Set builder form. (Connection)

- |                               |                                                                        |
|-------------------------------|------------------------------------------------------------------------|
| (1) $\{ 2, 3 \}$              | (a) $\{ x: x \text{ is a positive integer and is a divisor of } 18 \}$ |
| (2) $\{ 0 \}$                 | (b) $\{ x: x \text{ is an integer and } x^2 - 9 = 0 \}$                |
| (3) $\{ 1, 2, 3, 6, 9, 18 \}$ | (c) $\{ x: x \text{ is an integer and } x+1 = 1 \}$                    |
| (4) $\{ 3, -3 \}$             | (d) $\{ x: x \text{ is prime number and divisor of } 6 \}$             |

**Answers:** (1) d (2) c (3) a (4) b

### (2) State which of the following Sets are empty and which are not ? (Reasoning proof)

- (i)  $A = \{ x: x^2 = 4 \text{ and } 3x = 9 \}$
- (ii) Sets of even prime numbers
- (iii)  $B = \{ x: x^2 - 2 = 0 \text{ and } x \text{ is a rational number} \}$
- (iv) Set of odd numbers divisible by 2

#### Solution:

- (i)  $A = \{ x: x^2 = 4 \text{ and } 3x = 9 \}$

Solution of  $x^2 = 4$  are  $x = \pm 2$  and  $3x = 9$  is  $x = 3$

There is no real number satisfies both equation  $x^2 = 4$  and  $3x = 9$

$\therefore A = \{ x: x^2 = 4 \text{ and } 3x = 9 \}$  is an empty Set.

- (ii) Sets of even prime numbers

2 is a only even prime number

$\therefore$  Hence given Set is not empty set.

(iii).  $B = \{ x: x^2 - 2 = 0 \text{ and } x \text{ is a rational number} \}$

The solution of  $x^2 - 2 = 0$  is  $x = \pm \sqrt{2}$ , but

$-\sqrt{2}, \sqrt{2}$  are not rational numbers.

$\therefore B = \{ x: x^2 - 2 = 0 \text{ and } x \text{ is a rational number} \}$  is an empty set.

(iv). Set of odd numbers divisible by 2

Set of odd number =  $\{ 1, 3, 5, 7, \dots \}$

Odd number are not divisible by 2

$\therefore$  Given Set is an empty Set.

**(3) Let A be the Set of prime numbers less than 6 and P the Set of prime factors of 30. Check if A and P are equal . (Reasoning Proof)**

**Solution:** The Set of Prime number less than 6 ,  $A = \{ 2, 3, 5 \}$

The Prime factors of 30,  $P = \{ 2, 3, 5 \}$

Since the element of A are the same as the elements of P ,  $\therefore$  A and P are equal.

**(4) List all the subsets of the Set  $A = \{ 1, 4, 9, 16 \}$  (Communication)**

**Solution:** We know that empty set ( $\phi$ ) and itself (A) are the subsets of every set.

$\therefore$  All the subsets of the set  $A = \{ 1, 4, 9, 16 \}$

Are  $\phi, \{ 1 \}, \{ 4 \}, \{ 9 \}, \{ 16 \}$

$\{ 1, 4 \}, \{ 1, 9 \}, \{ 1, 16 \}, \{ 4, 9 \}, \{ 4, 16 \}, \{ 9, 16 \}$

$\{1, 4, 9\}, \{1, 4, 16\}, \{1, 9, 16\}, \{4, 9, 16\}$  and  $\{1, 4, 9, 16\}$

Total number of subsets of the set  $A = \{1, 4, 9, 16\}$  are 16

**Note:** If  $n(A) = n$  then the total number of Subsets are  $2^n$

Here for  $A = \{1, 4, 9, 16\}$ ,  $n(A) = 4$

$\therefore$  Total number of subsets of  $A = 2^4 = 16$

(5) If  $A = \{1, 2, 3, 4\}$ ;  $B = \{1, 2, 3, 4, 5, 6, 7, 8\}$  then find  $A \cup B$ ,  $A \cap B$ .

**What do you notice about the results? (Problem solving)**

**Solution:** Given  $A = \{1, 2, 3, 4\}$

$B = \{1, 2, 3, 4, 5, 6, 7, 8\}$

$A \cup B = \{1, 2, 3, 4\} \cup \{1, 2, 3, 4, 5, 6, 7, 8\} = \{1, 2, 3, 4, 5, 6, 7, 8\} = B$

$A \cap B = \{1, 2, 3, 4\} \cap \{1, 2, 3, 4, 5, 6, 7, 8\} = \{1, 2, 3, 4\} = A$

We observe that if  $A \subset B$  then  $A \cup B = B$ ,  $A \cap B = A$

(6) If  $A = \{2, 3, 5\}$ , find  $A \cup \phi$ ,  $\phi \cup A$  and  $A \cap \phi$ ,  $\phi \cap A$  and compare.

**(Problem Solving)**

**Solution:** Given  $A = \{2, 3, 5\}$ ,  $\phi = \{\}$

$A \cup \phi = \{2, 3, 5\} \cup \{\} = \{2, 3, 5\} = A$

$\phi \cup A = \{\} \cup \{2, 3, 5\} = \{2, 3, 5\} = A$

$\therefore A \cup \phi = \phi \cup A = A$

$A \cap \phi = \{2, 3, 5\} \cap \{\} = \{\} = \phi$

$$\phi \cap A = \{ \} \cap \{ 2, 3, 5 \} = \{ \} = \phi$$

$$\therefore A \cap \phi = \phi \cap A = A \cap B$$

(7) If  $A = \{ 2, 4, 6, 8, 10 \}$ ,  $B = \{ 3, 6, 9, 12, 15 \}$  then find  $A - B$  and  $B - A$ .

Are they equal? Are they disjoint Sets. (Problem solving)

**Solution:** Given  $A = \{ 2, 4, 6, 8, 10 \}$ ,  $B = \{ 3, 6, 9, 12, 15 \}$

$$A - B = \{ 2, 4, 8, 10 \},$$

$$B - A = \{ 3, 6, 9, 12, 15 \}$$

We observe that  $A - B \neq B - A$  and  $A - B$ ,  $B - A$  are disjoint Sets.

(8) Illustrate  $A - B$  and  $B - A$  in Venn – diagrams.

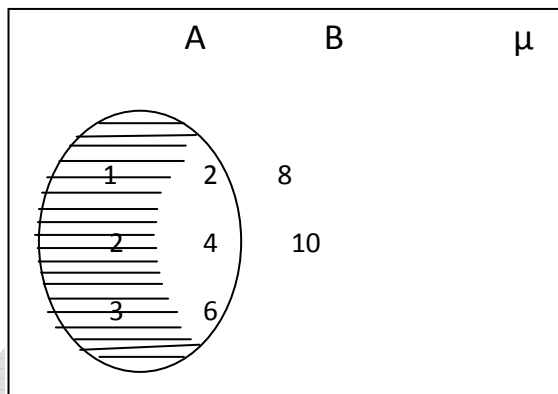
where  $A = \{ 1, 2, 3, 4, 5, 6 \}$  and  $B = \{ 2, 4, 6, 8, 10 \}$

(Visualization & Representation)

**Solution:** Given  $A = \{ 1, 2, 3, 4, 5, 6 \}$ ;  $B = \{ 2, 4, 6, 8, 10 \}$

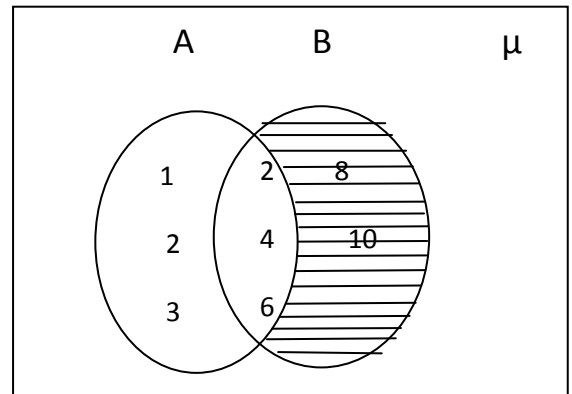
$$A - B = \{ 1, 3, 5 \}, B - A = \{ 8, 10 \}$$

The Venn diagram of  $A - B$



$$A - B = \{ 1, 3 \}$$

The Venn diagram of  $B - A$



$$B - A = \{ 8, 10 \}$$

## Very Short Answer Questions

**(1) Give example for a set (communication)**

**Solution:**  $A = \{ 2, 3, 5, 7, 11 \} = \{ x: x \text{ is a prime number less than } 13 \}$

**(2) Given example for an infinite and finite set (communication)**

**Solution:**  $A = \{ x: x \text{ is a multiple of } 7 \}$

$$= \{ 7, 14, 21, 28, \dots \}$$

$B = \{ x: x \text{ is a multiple of } 4 \text{ between } 17 \text{ and } 61 \text{ which are divisible by } 7 \}$

$$= \{ 28, 56 \} \text{ is a finite set}$$

**(3) Given example for an empty set and a non – empty set**

**Solution:**  $A = \{ x: 1 < x < 2, x \text{ is a natural number} \} = \{ \} \text{ is an empty set.}$

$$B = \{ x: x \in \mathbb{N}, x < 5 \text{ and } x > 7 \} = \{ 1, 2, 3, 4, 8, 9, \dots \}$$

Is a non – empty set.

**(4) Show that the sets A and B are equal.**

$A = \{ x: x \text{ is a letter in the word "ASSASSINATION"} \}$

$B = \{ x: x \text{ is a letter in the word "STATION"} \} \quad (\text{Reasoning proof})$

**Solution:** In roster form A and B can be written as

$$A = \{ A, S, I, N, T, O \}$$

$$B = \{ A, S, I, N, T, O \}$$

So , the elements of A and B are same

$\therefore$  A, B are equal Sets.

(5)  $A = \{ \text{quadrilaterals} \}$  ,  $B = \{ \text{Square , rectangle, trapezium, rhombus} \}$

**State whether  $A \subset B$  or  $B \subset A$ . Justify your answer.**

**Solution:** Given  $A = \{ \text{quadrilaterals} \}$

$B = \{ \text{Square , rectangle, trapezium, rhombus} \}$

All quadrilaterals need not be square or rectangle or trapezium or rhombus.

Hence  $A \not\subset B$

Square, rectangle ,trapezium and rhombus are quadrilaterals.

Hence  $B \subset A$ .

(6) If  $A = \{ 5, 6, 7, 8 \}$  and  $B = \{ 7, 8, 9, 10 \}$  then find  $n(A \cap B)$  and  $n(A \cup B)$   
( Problem solving)

**Solution :** Given  $A = \{ 5, 6, 7, 8 \}$   
 $B = \{ 7, 8, 9, 10 \}$

$$A \cap B = \{ 7, 8 \}$$

$$A \cup B = \{ 5, 6, 7, 8, 9, 10 \}$$

$$n(A \cap B) = 2$$

$$n(A \cup B) = 6$$

(7) If  $A = \{ 1, 2, 3, 4 \}$  ;  $B = \{ 1, 2, 3, 5, 6 \}$  then find  $A \cap B$  and  $B \cap A$  . Are they equal? (Problem Solving)

**Solution:** Given  $A = \{ 1, 2, 3, 4 \}$

$B = \{ 1, 2, 3, 5, 6 \}$

$$A \cap B = \{ 1, 2, 3, 4 \} \cap \{ 1, 2, 3, 5, 6 \} = \{ 1, 2, 3 \}$$

$$B \cap A = \{ 1, 2, 3, 5, 6 \} \cap \{ 1, 2, 3, 4 \} = \{ 1, 2, 3 \}$$

We observe that  $A \cap B = B \cap A$

**(8). Write the set builder form of  $A \cup B$ ,  $A \cap B$  and  $A - B$  (communication)**

**Solution:**

$$A \cup B = \{ x: x \in A \text{ or } x \in B \}$$

$$A \cap B = \{ x: x \in A \text{ and } x \in B \}$$

$$A - B = \{ x: x \in A \text{ and } x \notin B \}$$

**(9). Give example for disjoint sets. (Communication)**

**Solution:**

The Set of even number and the Set of odd number are disjoint sets,

**Note:** If  $A \cap B = \phi$  then A, B are disjoint sets.

## Object Type Question

(1) The symbol for a universal Set ..... [    ]

(A)  $\mu$                       (B)  $\phi$                       (C)  $\subset$                       (D)  $\cap$

(2) If  $A = \{a, b, c\}$ , the number of subsets of A is ..... [    ]

(A) 3                      (B) 6                      (C) 8                      (D) 12

(3) Which of the following sets are equal ..... [   ]

(A)  $A = \{1, -1\}, B = \{1^2, (-1)^2\}$       (B)  $A = \{0, a\}, B = \{b, 0\}$

(C)  $A = \{ 2, 4, 6 \}$ ,  $B = \{ 1, 3, 5 \}$       (D)  $A = \{ 1, 4, 9 \}$ ,  $B = \{ 1^1, 2^2, 3^2 \}$

(4) Which of the following Set is not null Set ? ..... [   ]

(A)  $\{x: 1 < x < 2, x \text{ is a natural number} \}$

( B )  $\{x: x^2 - 2 = 0 \text{ and } x \in \mathbb{Q}\}$

(C)  $\{x: x^2 = 4, x \text{ is odd}\}$

(D)  $\{x: x \text{ is a prime number divisible by } 2\}$

(5) which of the following Set is not infinite ? ..... [    ]

(A)  $\{1, 2, 3, \dots, 100\}$       (B)  $\{x: x^2 \text{ is positive}, x \in \mathbb{Z}\}$

(c)  $\{x: x \in \mathbb{N}, x \text{ is prime}\}$       (D)  $\{3, 5, 7, 9, \dots\}$

( 6 ) Which of the following set is not finite ..... [   ]

(A)  $\{ x : x \in \mathbb{N}, x < 5 \text{ and } x > 7 \}$       (B)  $\{ x : x \text{ is even prime} \}$

( C )  $\{ x : x \text{ is a factor of } 42 \}$       ( D )  $\{ x : x \text{ is a multiple of } 3, x < 40 \}$

( 7 ) The set builder form of  $A \cap B$  is ..... [   ]

( A )  $\{ x : x \in A \text{ and } x \notin B \}$       ( B )  $\{ x : x \in A \text{ or } x \in B \}$

( C )  $\{ x : x \in A \text{ and } x \in B \}$       ( D )  $\{ x : x \in B \text{ and } x \notin A \}$

( 8 ) For ever set  $A$ ,  $A \cap \phi =$  ..... [   ]

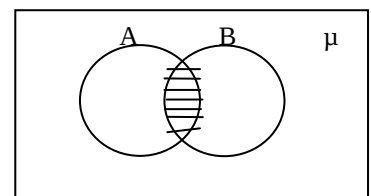
( A )  $A$       ( B )  $\phi$       ( C )  $\mu$       ( D )  $0$

( 9 ). Two Sets  $A$  and  $B$  are said to be disjoint if ..... [   ]

( A )  $A - B = \phi$     ( B )  $A \cup B = \phi$     ( C )  $A \cap B = B \cap A$     ( D )  $A \cap B = \phi$

(10) The Shaded region in the adjacent figure is ..... [   ]

( A )  $A - B$     ( B )  $B - A$     ( C )  $A \cap B$     ( D )  $A \cup B$



(11)  $A = \{ x : x \text{ is a circle in a give plane} \}$  is ..... [   ]

( A ) Null Set    ( B ) Finite Set    ( C ) Infinite Set    ( D ) Universal Set

(12)  $n(A \cup B) = \dots\dots\dots$  [    ]

(A)  $n(A) + n(B)$  (B)  $n(A) + n(B) - n(A \cap B)$

(C)  $n(A) - n(B)$  (D)  $n(A) + n(B) + n(A \cap B)$

(13) If A is subset of B, then  $A - B = \dots\dots\dots$  [    ]

(A)  $\phi$  (B) A (C) B (D)  $A \cap B$

(14) If  $A = \{ 1, 2, 3, 4, 5 \}$  then the cardinal number of A is  $\dots\dots\dots$  [    ]

(A)  $2^5$  (B) 5 (C) 4 (D)  $5^2$

(15)  $A = \{ 2, 4, 6, 8, 10 \}$ ,  $B = \{ 1, 2, 3, 4, 5 \}$  then  $B - A = \dots\dots\dots$  [    ]

(A)  $\{ 6, 8, 10 \}$  (B)  $\{ 1, 3, 5 \}$  (C)  $\{ 2, 4 \}$  (D) All the above

(16) Which Statement is true  $\dots\dots\dots$  [    ]

(A)  $A - B$ ,  $B - A$  are disjoint sets

(B)  $A - B$ ,  $A \cap B$  are disjoint sets

(C)  $A \cap B$ ,  $B - A$  are disjoint sets

(D) All the above

(17)  $A \subset B$  then  $A \cap B = \dots\dots\dots$  [    ]

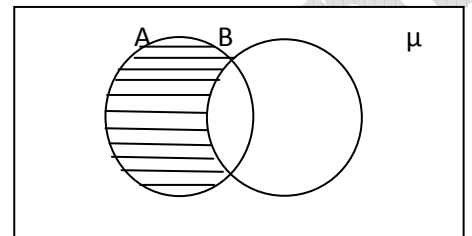
(A) A (B) B (C)  $\phi$  (D)  $A \cup B$

(18)  $A \subset B$  then  $A \cup B = \dots\dots\dots$  [   ]

- (A)  $A$                       (B)  $B$                       (C)  $\phi$                       (D)  $A \cap B$

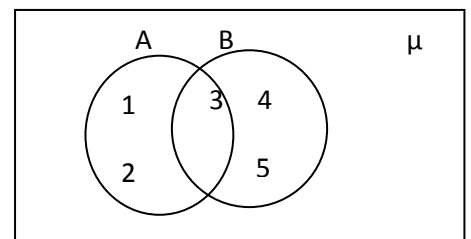
(19) The shaded region in the adjacent figure represents ..... [   ]

- (A)  $A - B$     (B)  $B - A$     (C)  $A \cap B$     (D)  $A \cup B$



(20) From the figure ..... [   ]

- (A)  $A - B = \{ 1, 2, \}$                       (B)  $A \cap B = \{ 3 \}$   
 (C)  $B - A = \{ 4, 5 \}$                       (D) All the above



**Key:**

1. **A**    2. **C**    3. **D**    4. **D**    5. **A**    6. **A**    7. **C**    8. **B**    9. **D**    10. **C**  
 11. **C**    12. **B**    13. **A**    14. **B**    15. **B**    16. **D**    17. **A**    18. **B**    19. **A**    20. **D**

## Fill in the Blanks

- (1) The Symbol for null set =  $\phi$
- (2) Roster form of  $\{x: x \in \mathbb{N}, 9 \leq x \leq 16\}$  is =  $\{9, 10, 11, 12, 13, 14, 15, 16\}$
- (3) If  $A \subset B$  and  $B \subset A$  then  $A = B$
- (4) If  $A \subset B$  and  $B \subset C$  then =  $A \subset C$
- (5)  $A \cup \phi =$   $A$
- (6) The Set theory was developed by = **George cantor**
- (7) If  $n(A) = 7$ ,  $n(B) = 8$ ,  $n(A \cap B) = 5$  then  $n(A \cup B) =$  **10**
- (8) A set is a **Well defined** collection of objects.
- (9) Every set is **Subset** of itself.
- (10) The number of elements in a set is called the **cardinal number** of the set.
- (11)  $A = \{2, 4, 6, \dots\}$ ,  $B = \{1, 3, 5, \dots\}$  then  $n(A \cap B) =$  **0**
- (12) A and B are disjoint sets then  $A - B =$  **A**
- (13) If  $A \cup B = A \cap B$  then **A = B**
- (14)  $A = \{x: x^2 = 4 \text{ and } 3x = 9\}$  is a **null set**
- (15)  $A = \{2, 5, 6, 8\}$  and  $B = \{5, 7, 9, 1\}$  then  $A \cup B =$   **$\{1, 2, 5, 6, 7, 8, 9\}$**  .
- (16) If  $A \subset B$ ,  $n(A) = 3$ ,  $n(B) = 5$ , then  $n(A \cap B) =$
- (17) If  $A \subset B$ ,  $n(A) = 3$ ,  $n(B) = 5$ , then  $n(A \cup B) =$   $\phi$
- (19)  $A = \{1, 2, 3, 4\}$  and  $B = \{2, 4, 6, 8\}$  then  $B - A =$   **$\{6, 8\}$**
- (20) Set builder form of  $A \cup B$  is =  **$\{x: x \in A \text{ or } x \in B\}$**